



# Advances in the Development of Non-Utility-Maximizing Models of Choice Behavior in Transportation Research

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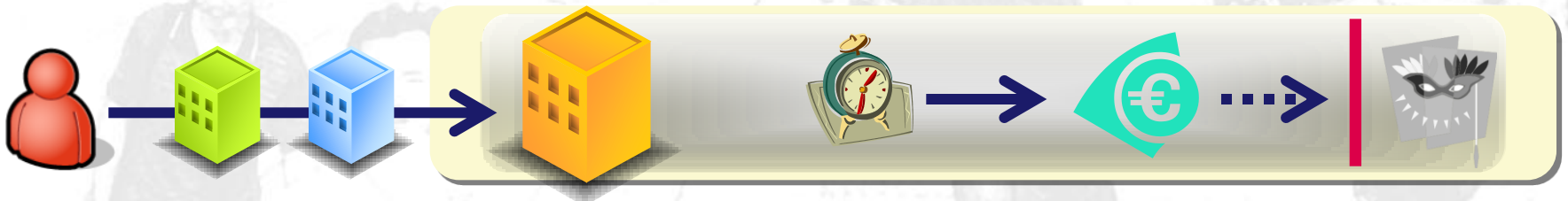
# Limitations

- Rational utility-maximising choice models may not sufficiently nor adequately represent real *decision processes* in that they assume
  - Evaluating utilities for each alternative
  - Trading off utilities of all factors
  - Choosing the alternative with the highest utility



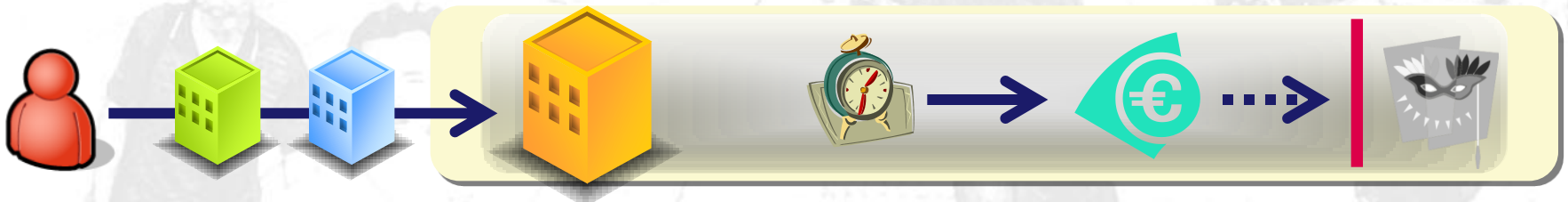
# Background

- Principles of bounded rationality could be more appropriate.
  - Limits in cognitive and computational ability
  - Satisficing behavior
  - Incomplete information
  - Simplifying (heuristic) decision rules
  - Non-cognitively driven choices



# Aim presentation

- Discuss some examples of recent work in our group to formulate, estimate and apply models of bounded rationality, mental representation and hybrid choice drivers.
  - Heterogeneous heuristic model (HHR model)
  - Mental representation
  - Hybrid affective-cognitive model







# HETEROGENEOUS HEURISTIC MODEL

# Behavioral Heterogeneity

Is usually captured in discrete choice models in terms of

(1) Unobservable utility  
(e.g., MNL)

$$u_i = \sum_j \beta_j x_{ij} + \varepsilon_i$$

(2) Parameter distribution  
(mixed logit)

$$u_i = \sum_j \beta_{j1} x_{ij} + \varepsilon_i \sim p_1$$

...

$$u_i = \sum_j \beta_{jN} x_{ij} + \varepsilon_i \sim p_N$$

(3) Latent class

$$\sum_n p_n = 1$$

# Specification Problems

Choose the alternative with the highest utility

$$i | \sum_j \beta_j x_{ij} + \varepsilon_i \geq \sum_j \beta_j x_{kj} + \varepsilon_k, \forall k \neq i$$

(1) Infinitely small **decision criterion** (utility difference) is used, little is considered about criterion variability.

(2) Comparisons are directly based on parametric utilities. However, preference was originally defined on **rank orders**.

# Heterogeneous Heuristic Model

1

## BR model

- To develop and test a model of travel behavior, based on principles of Bounded Rationality, using real-world behavioral data.

2

## Heterogeneity

- To develop a modeling approach that allows for decision heterogeneity in terms of individual decision *strategies*.

3

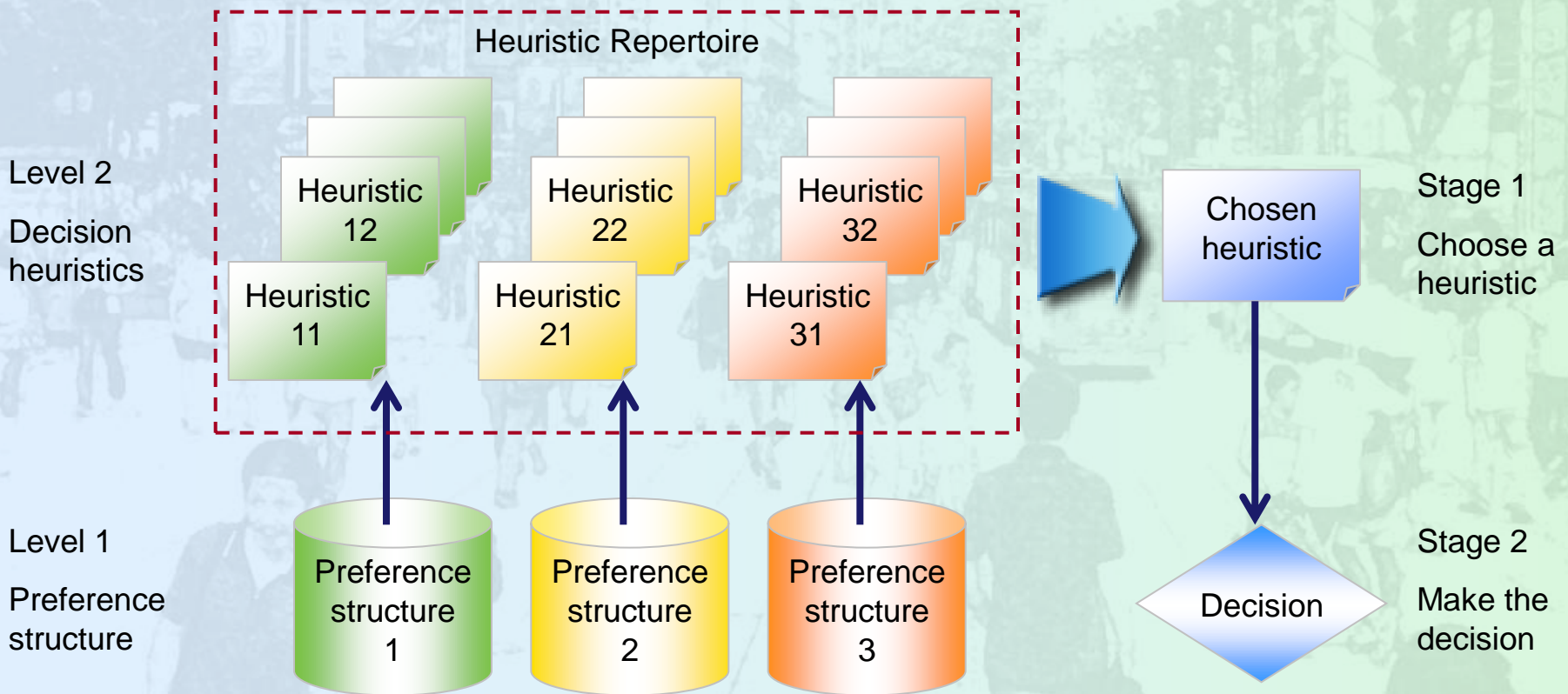
## Time

- To examine time-dependent aspects of travel behavior.



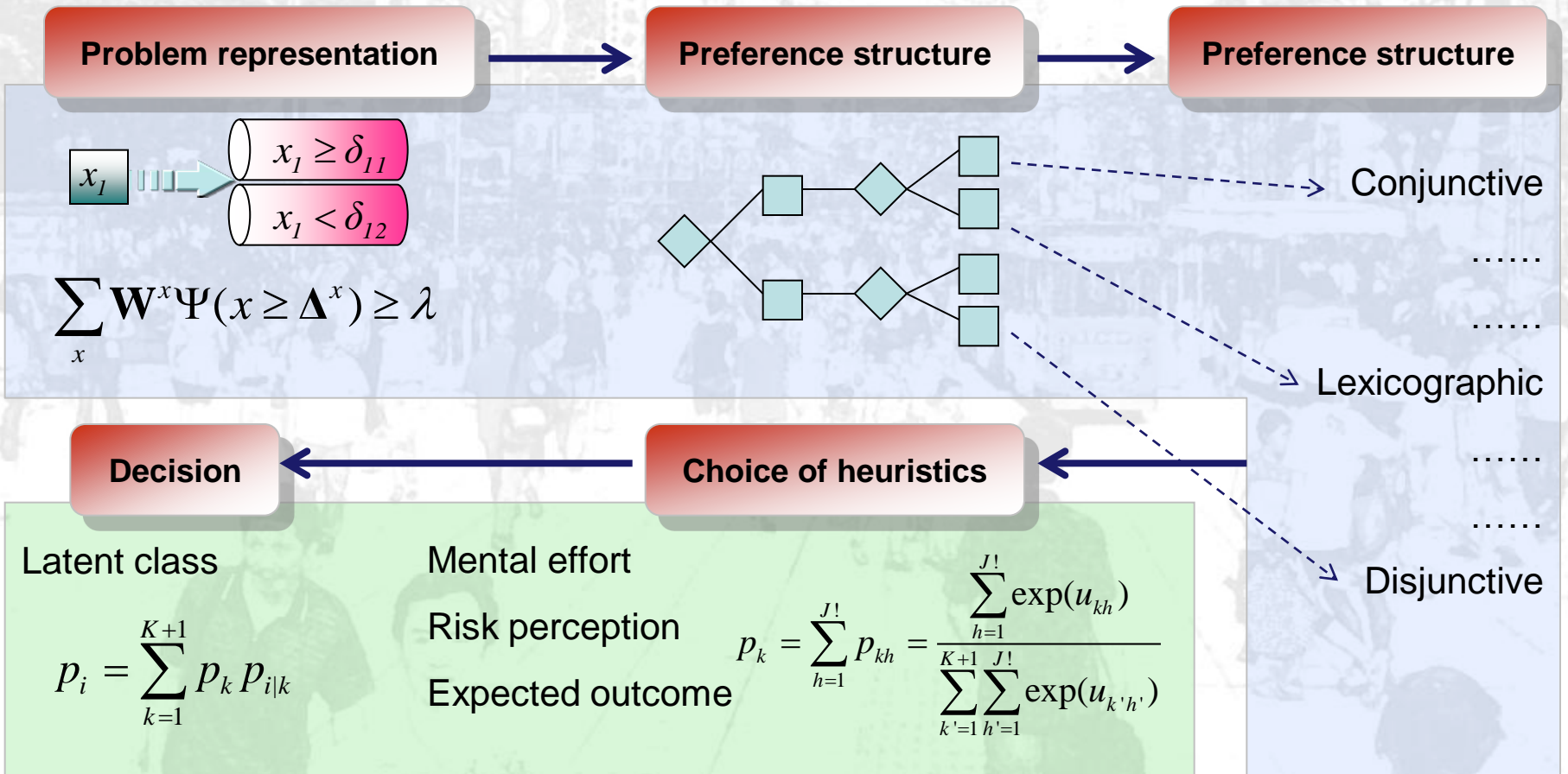
# Conceptual Framework

HHM is based on a two-level two-stage theoretical construct.



# Conceptual Framework

- For satisficing decision and comparative choice

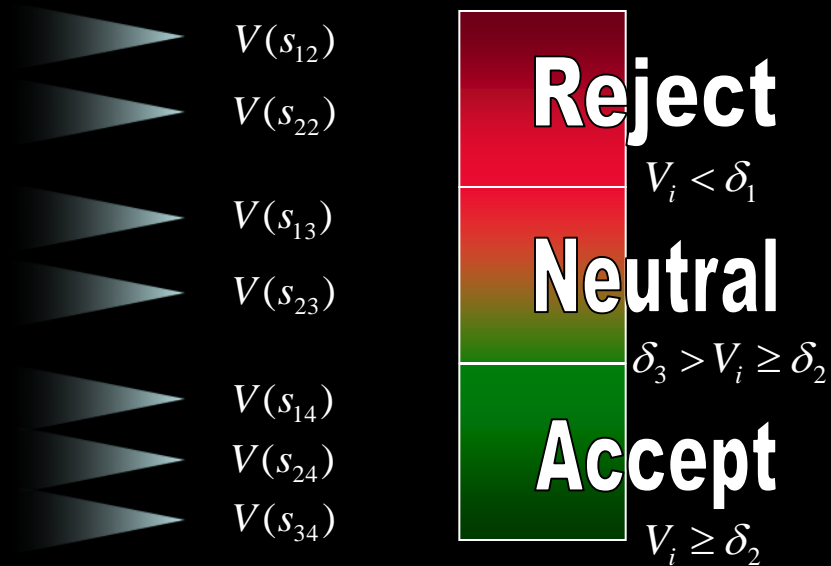
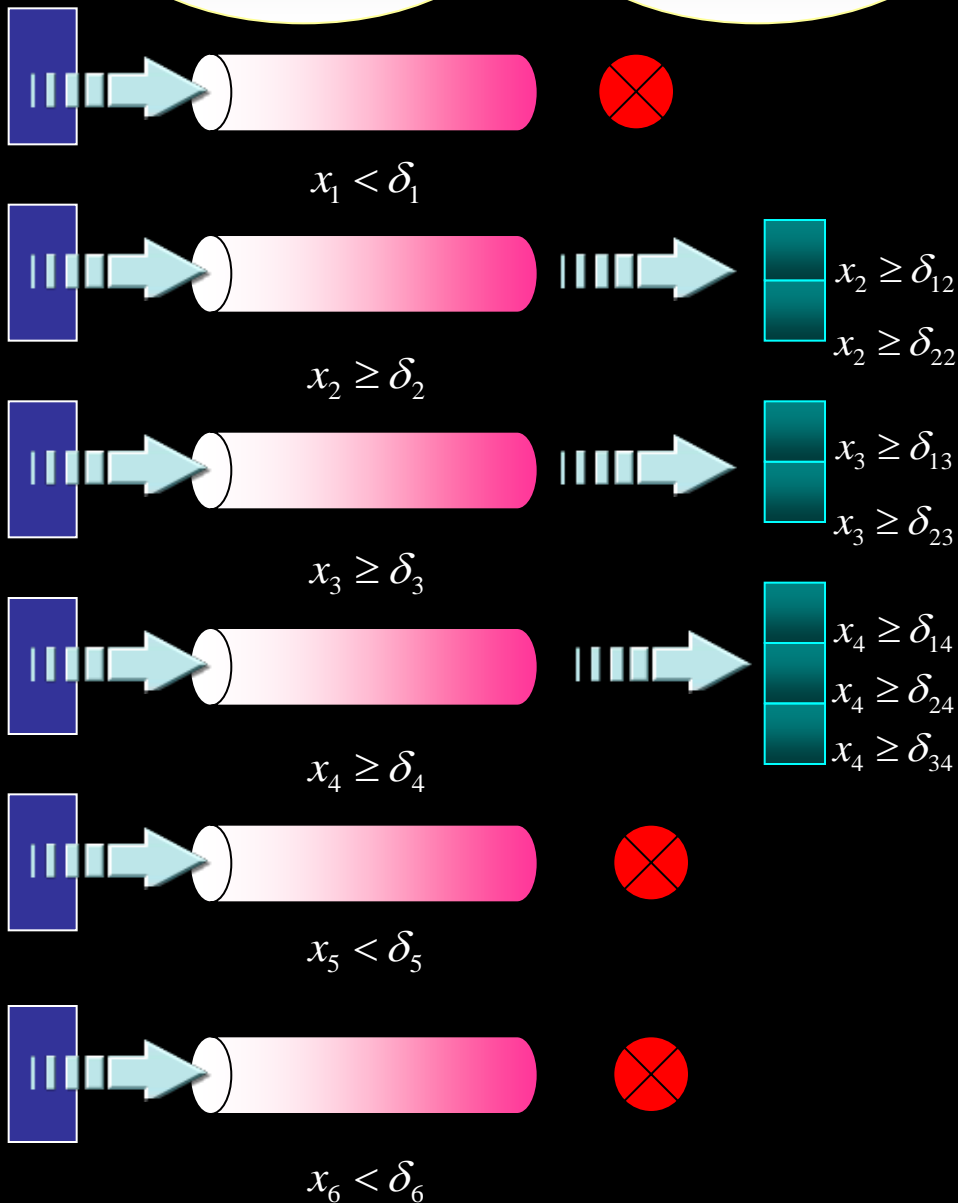


Factor activation

Factor representation

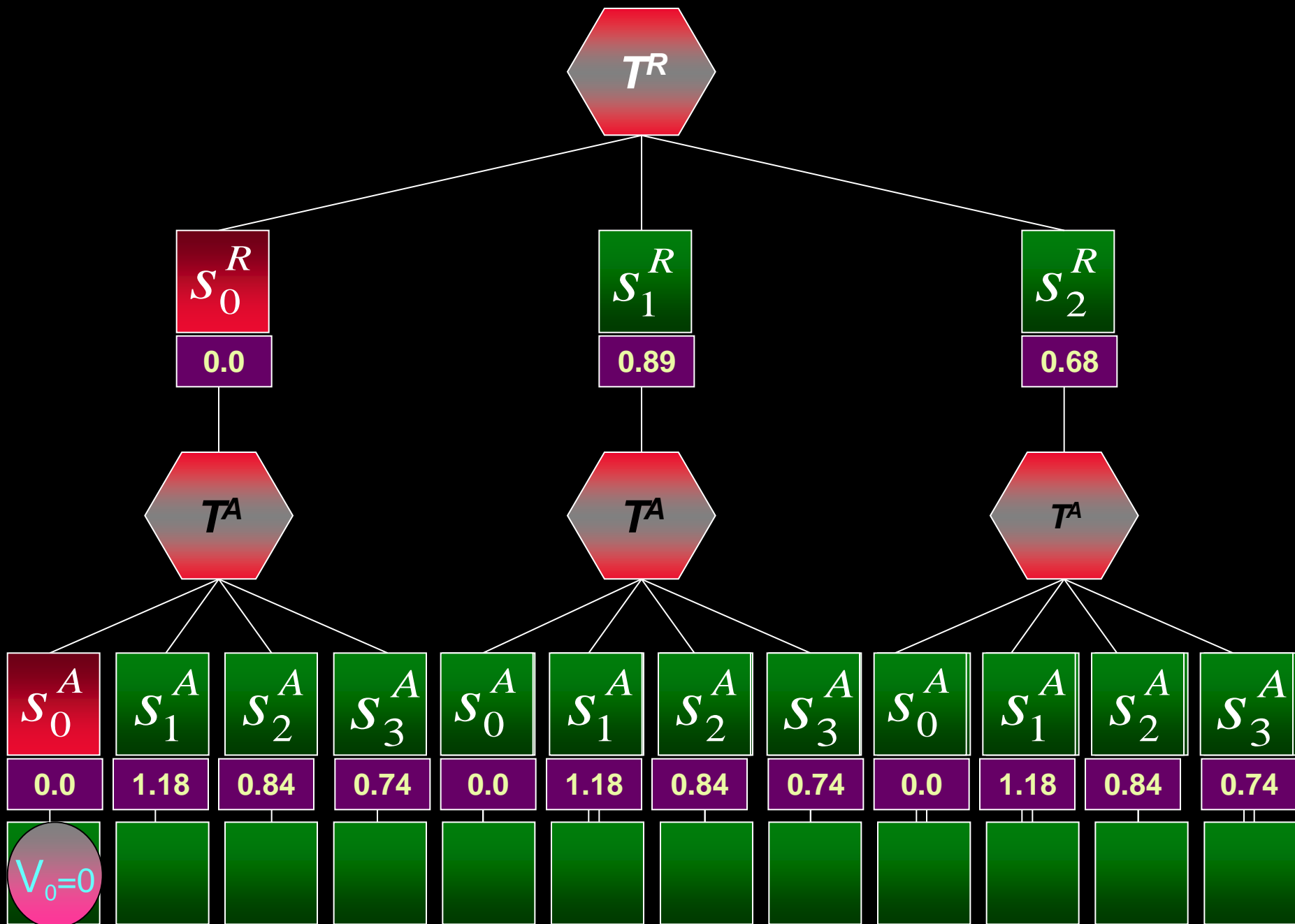
Factor state valuation

Ordered preference sets

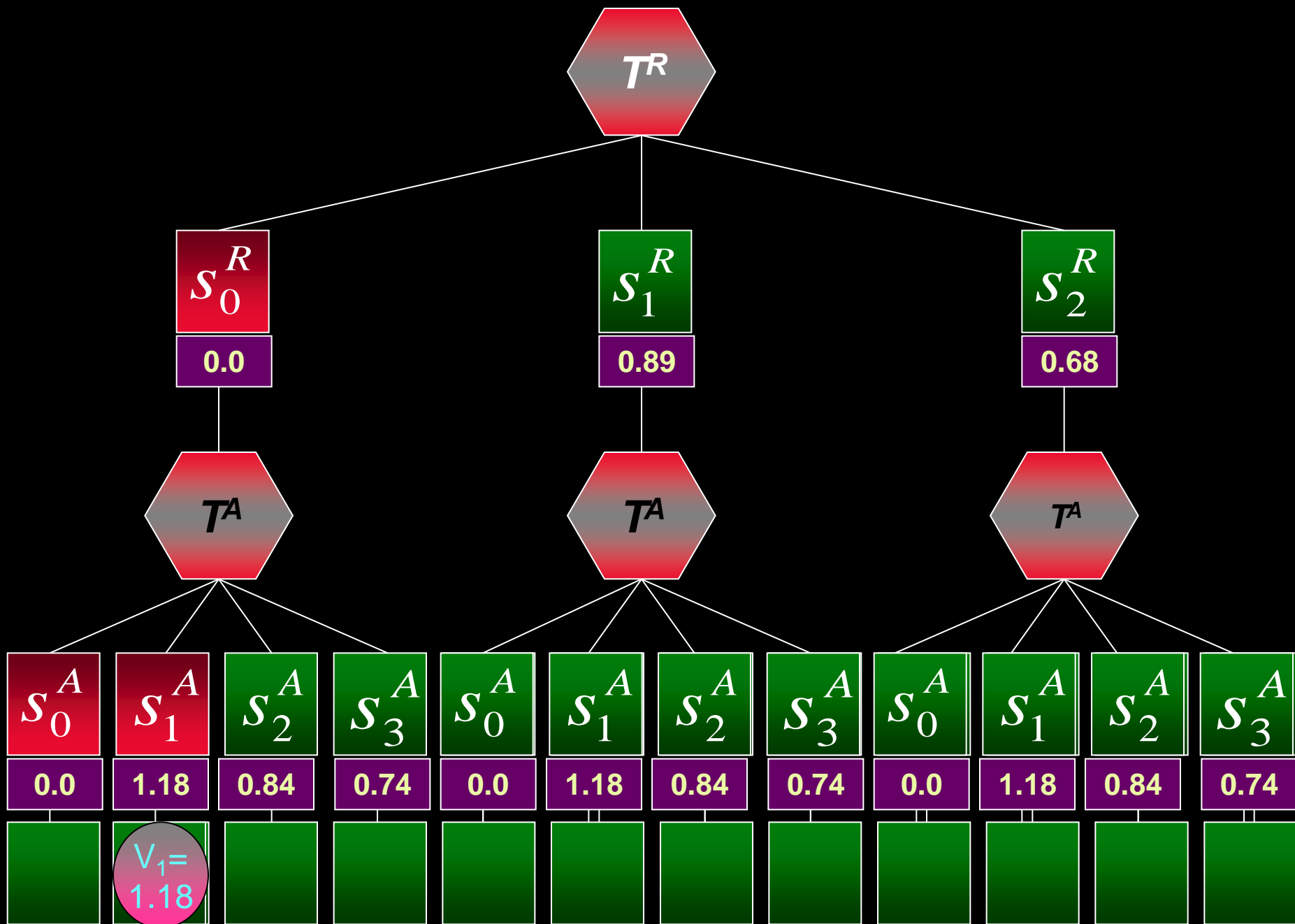


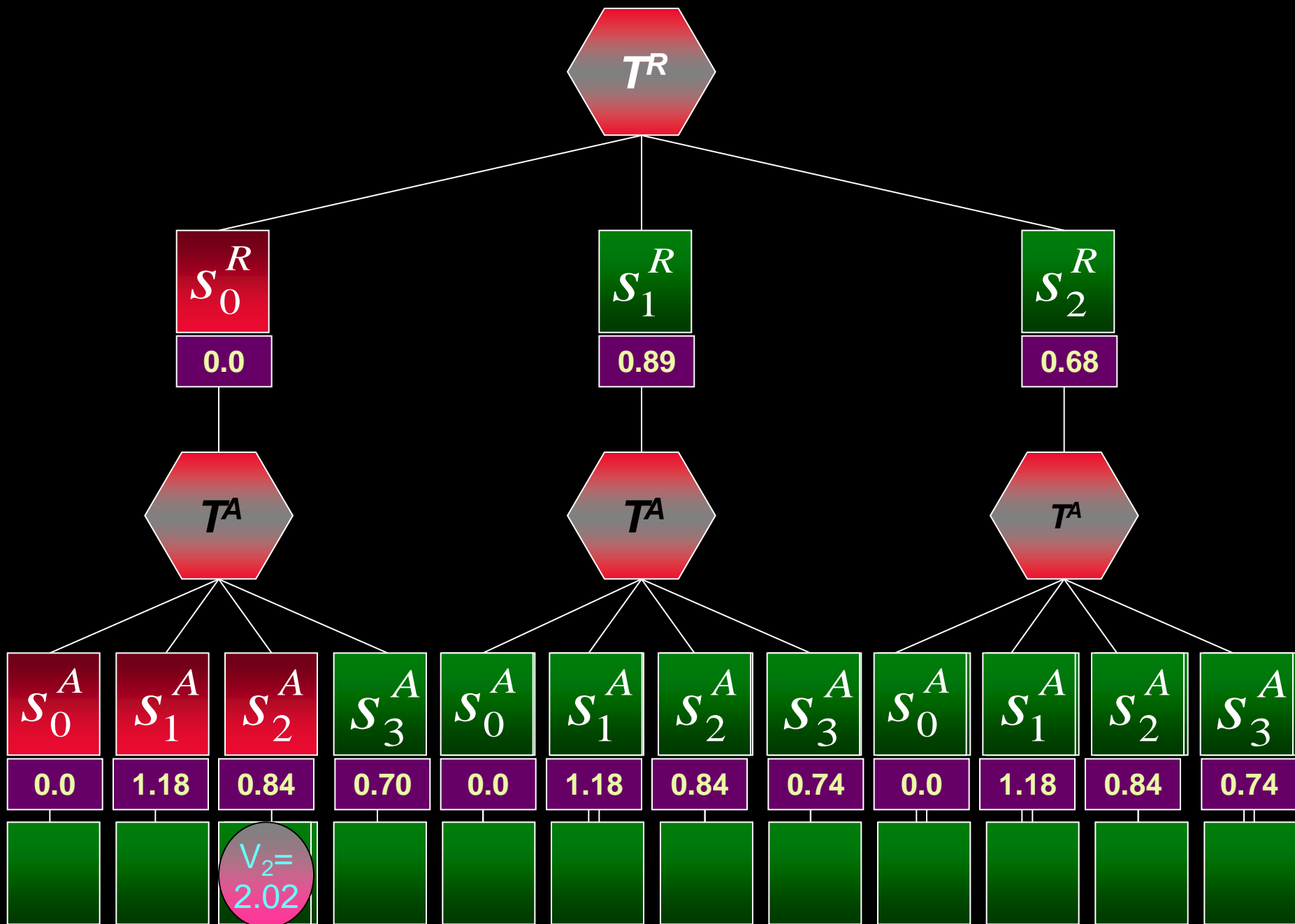
$$V_i = \sum_j \sum_n V(s_{nj})$$

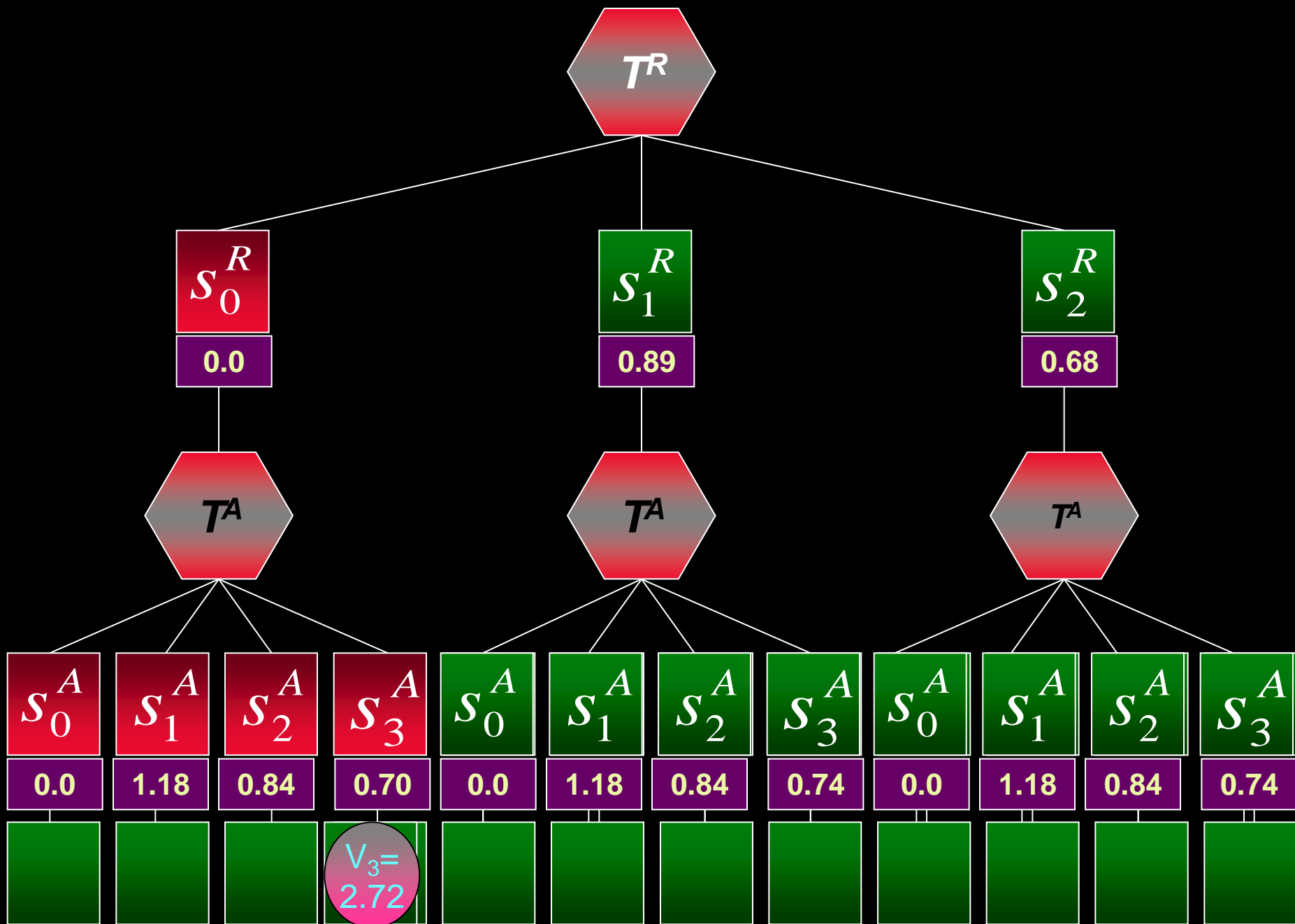
Alternative valuation

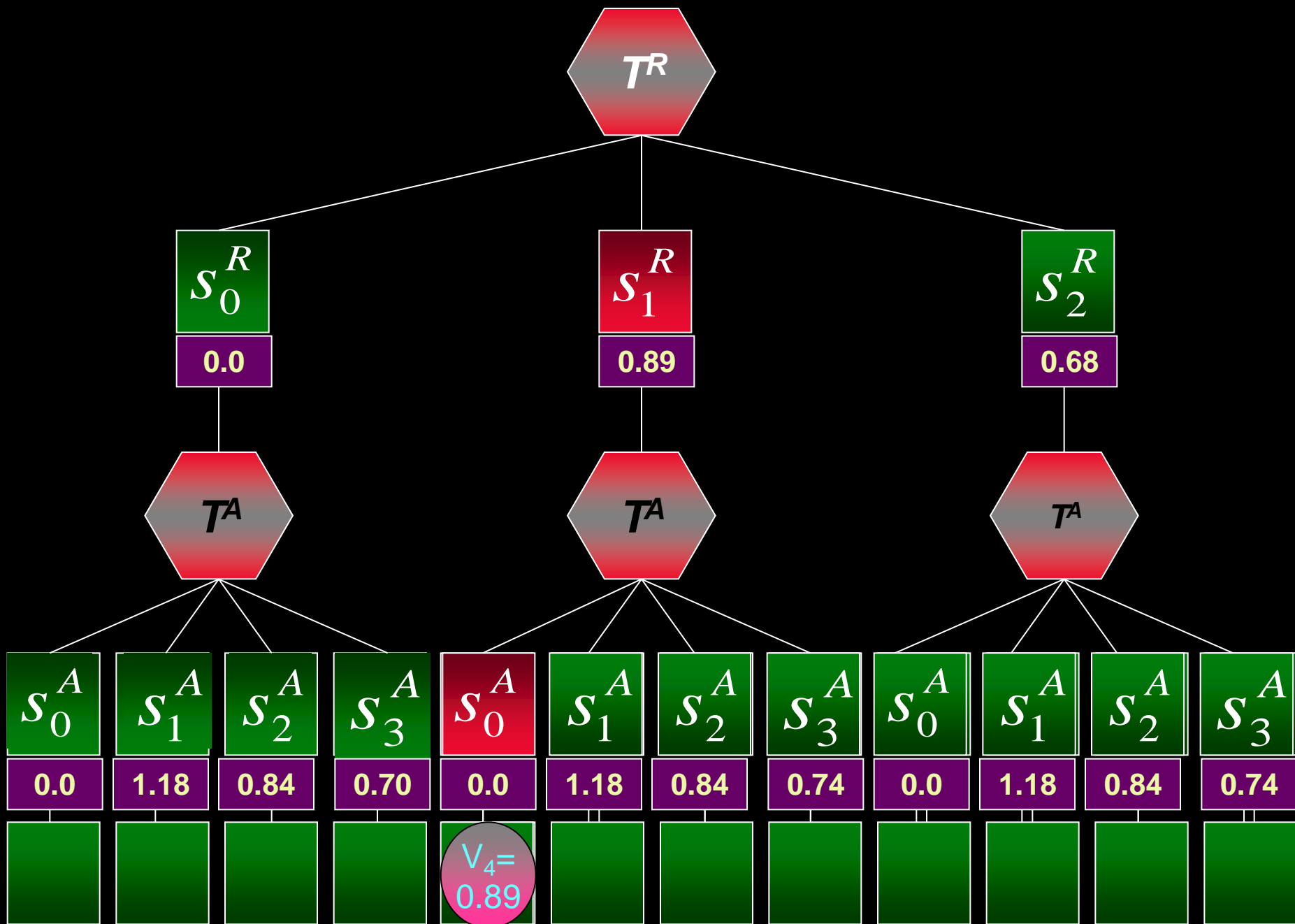




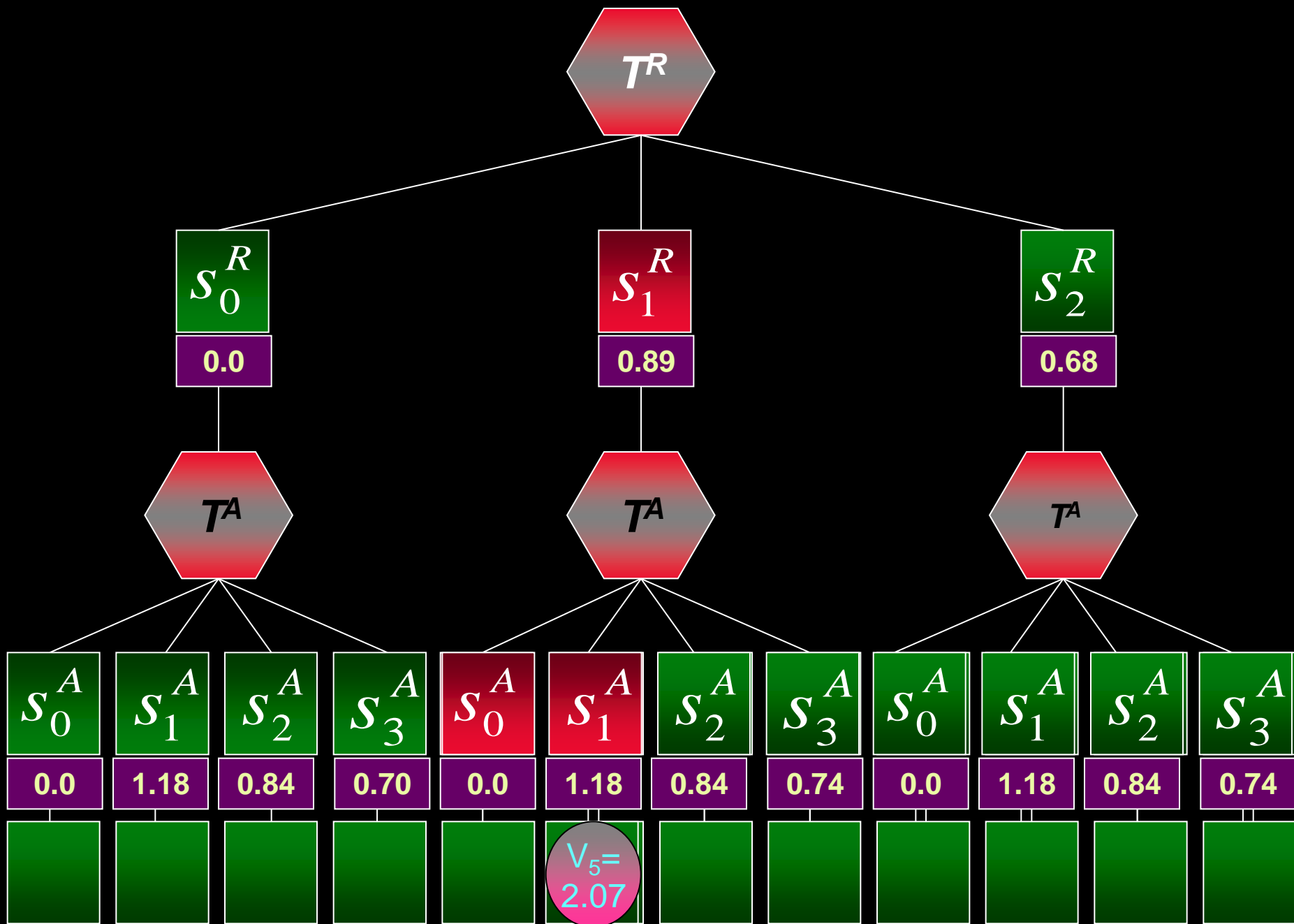


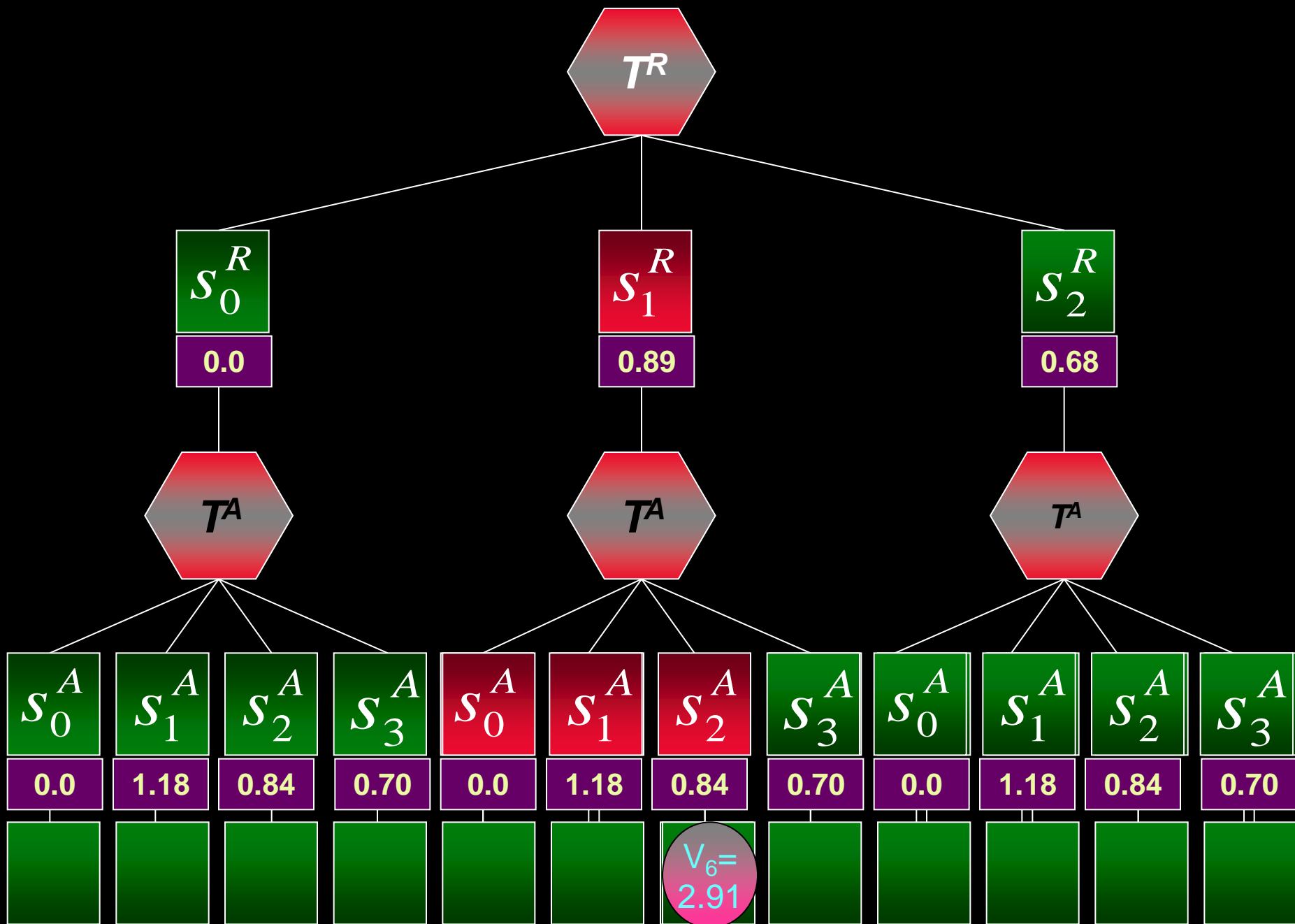


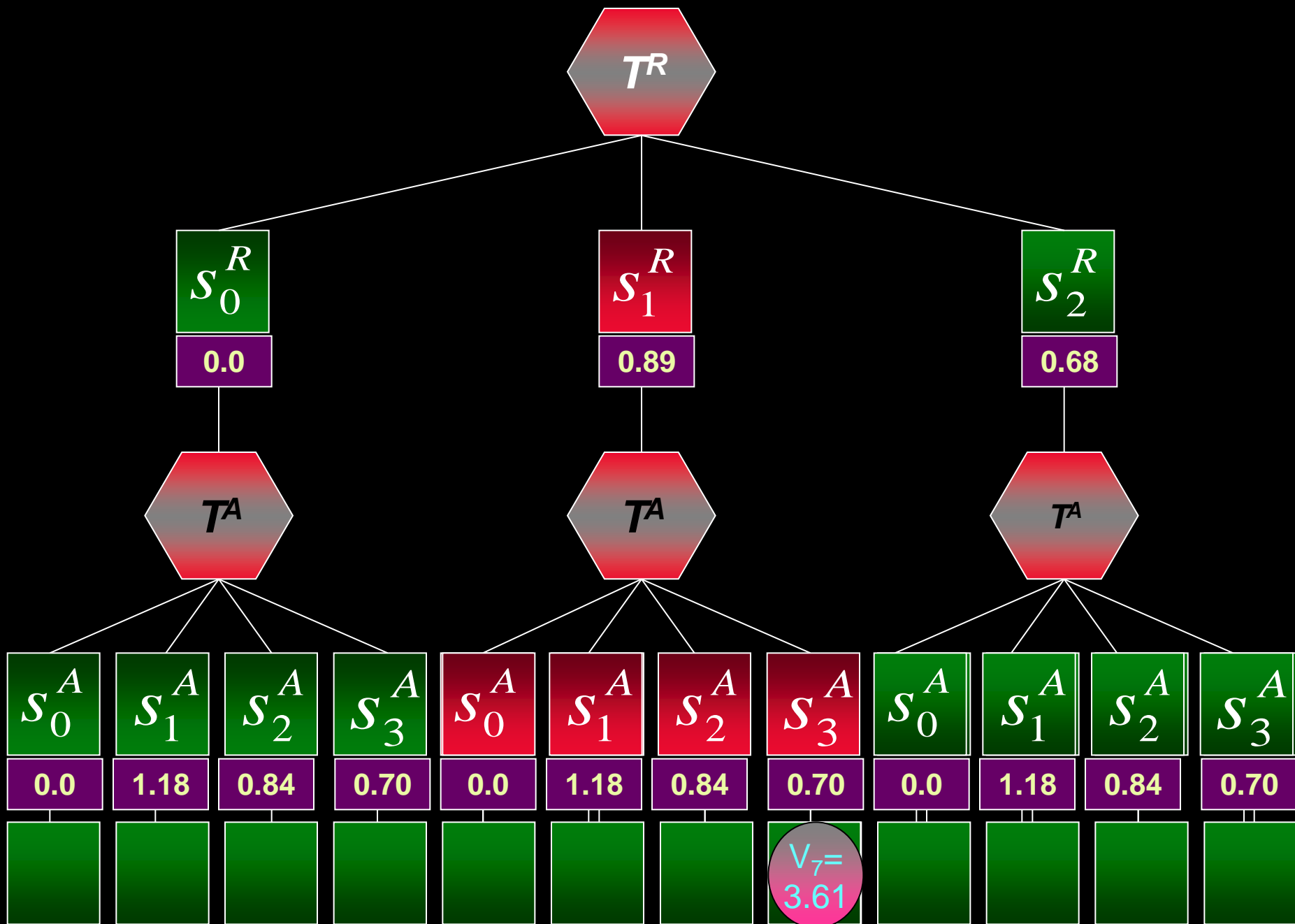


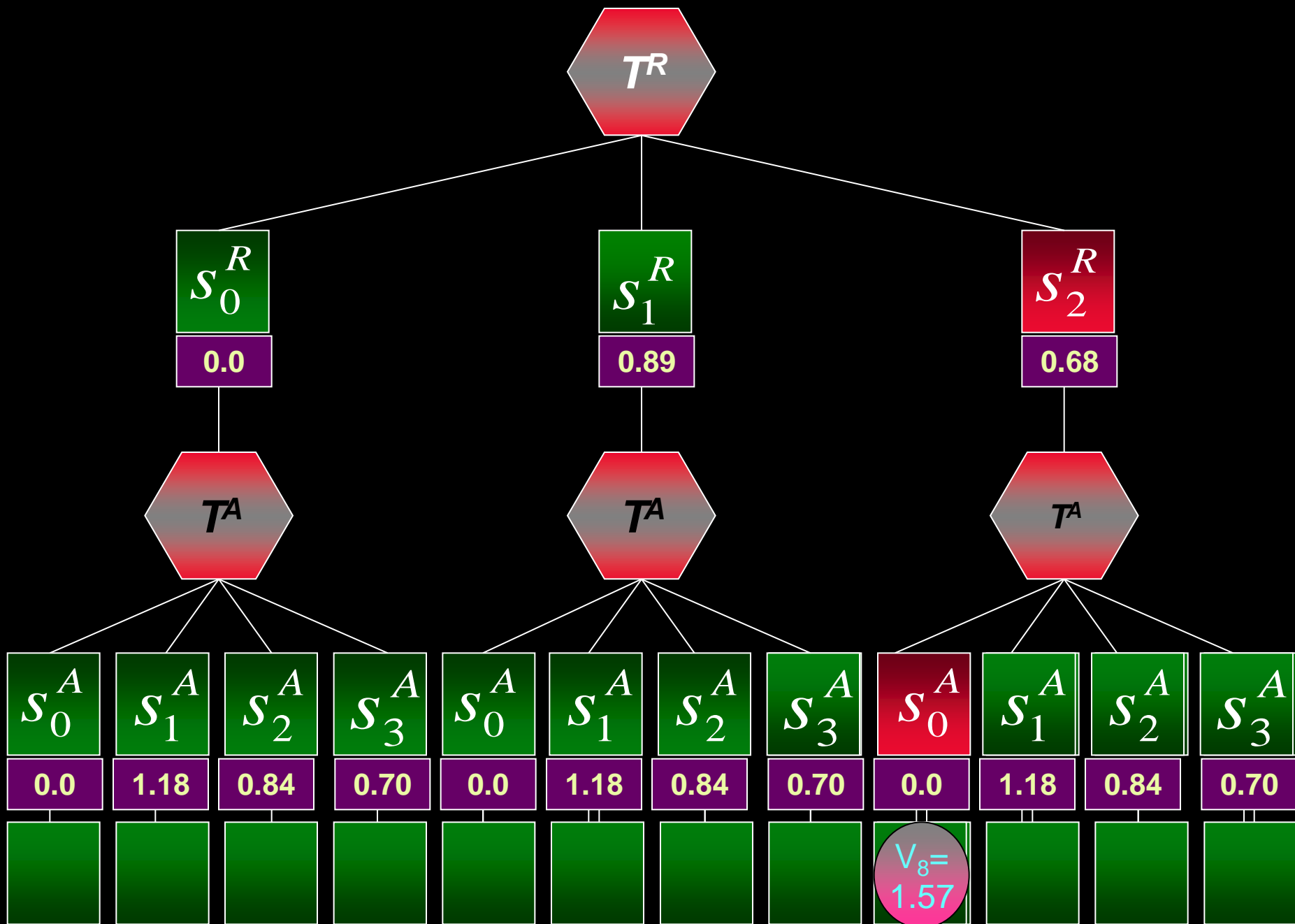




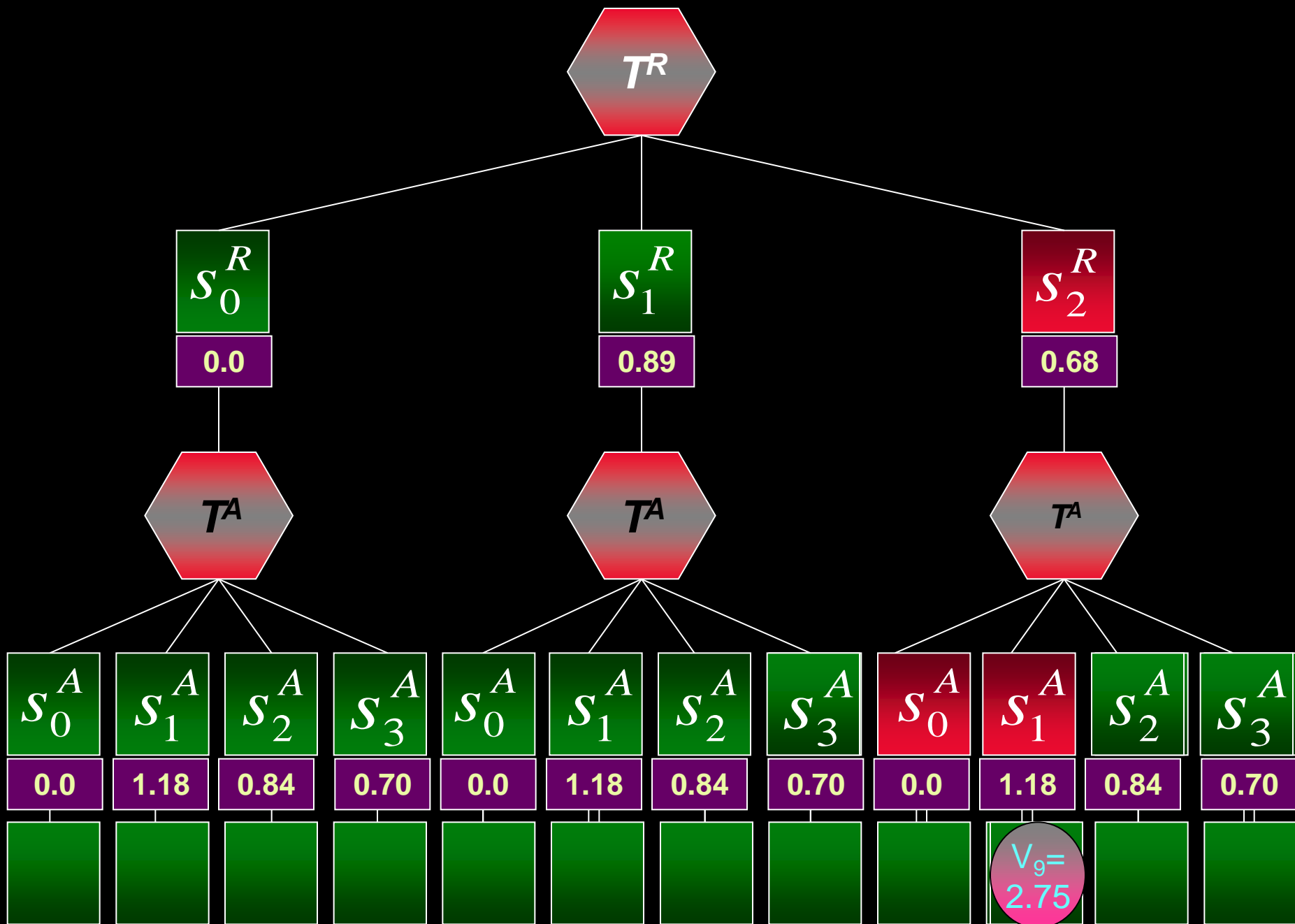


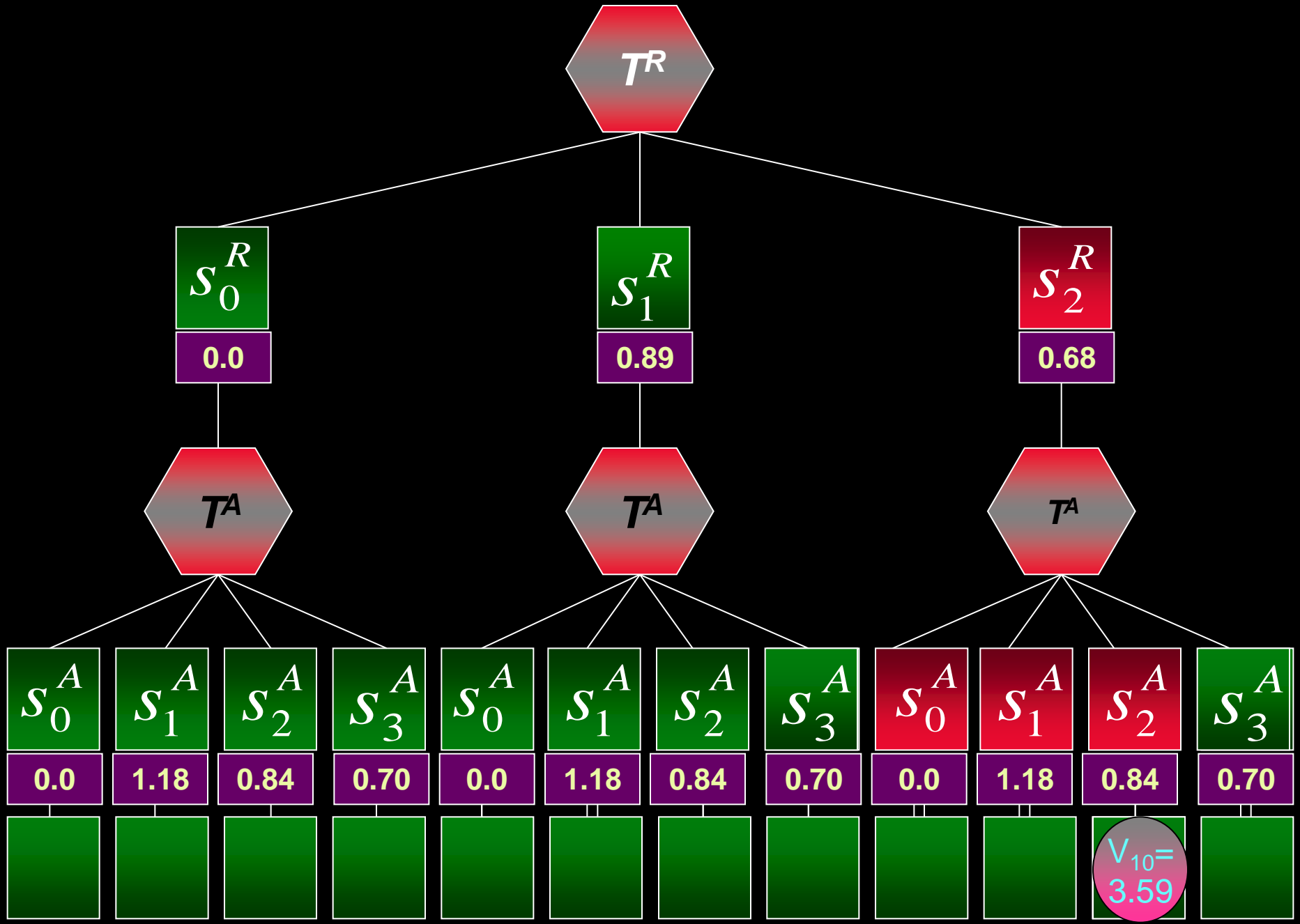


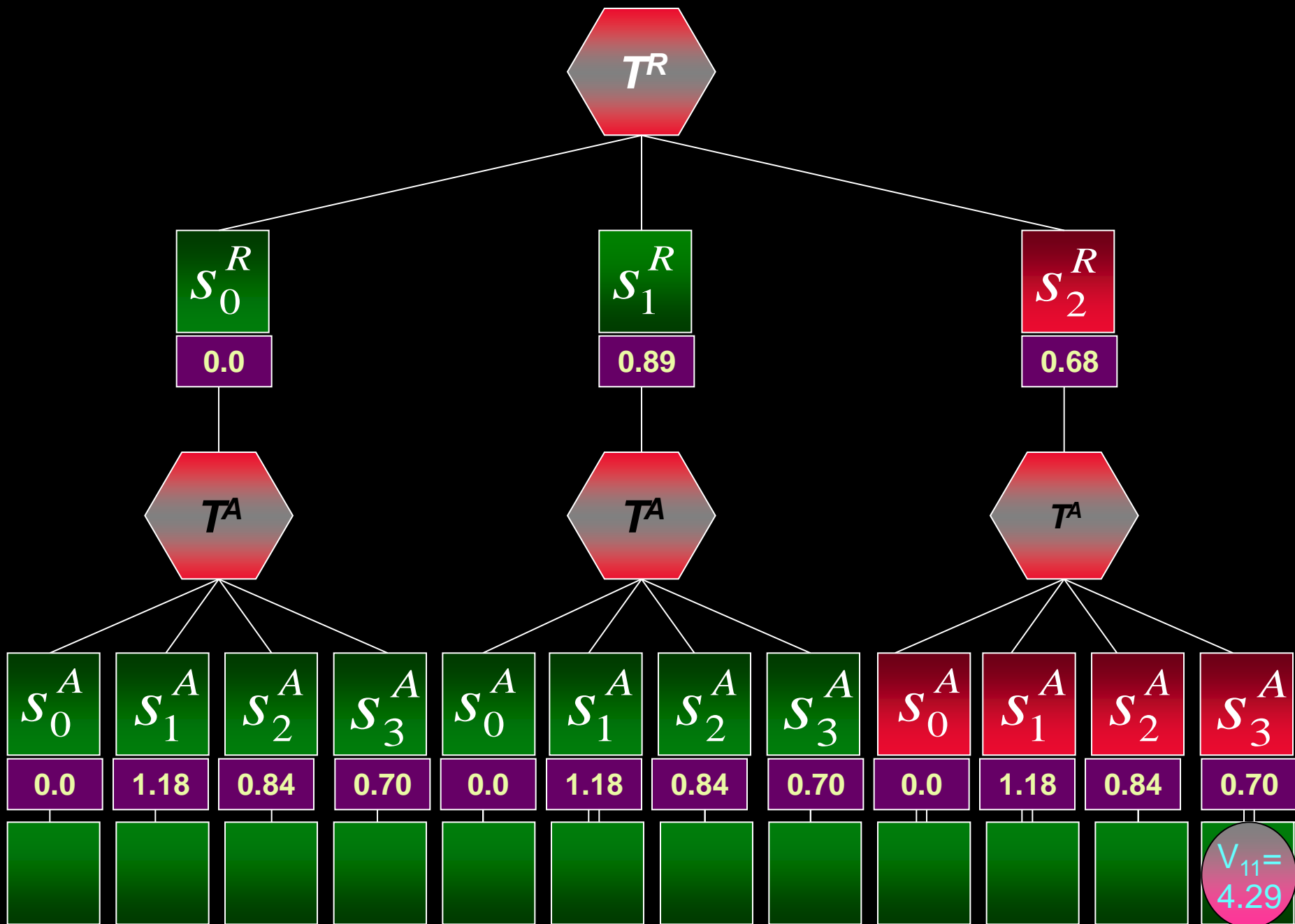




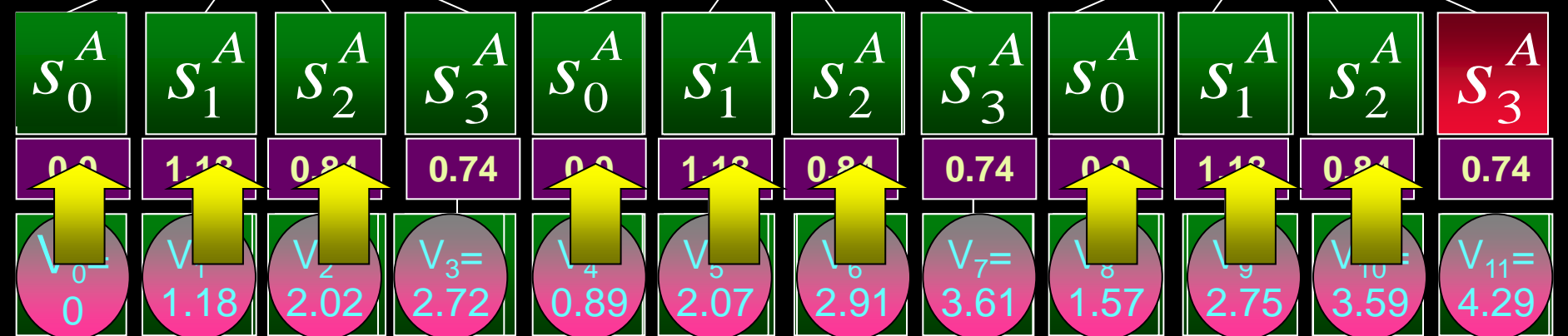
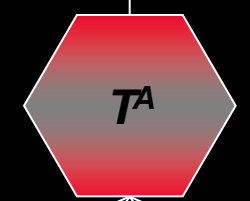
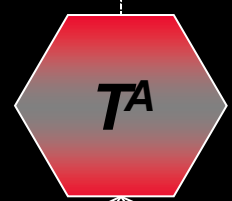
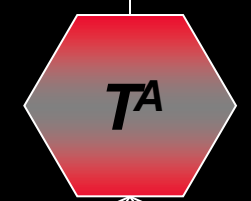
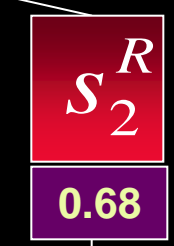
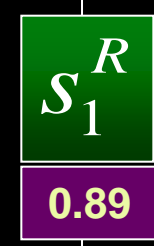
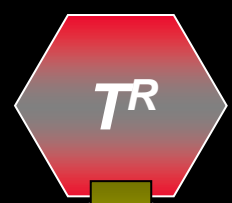




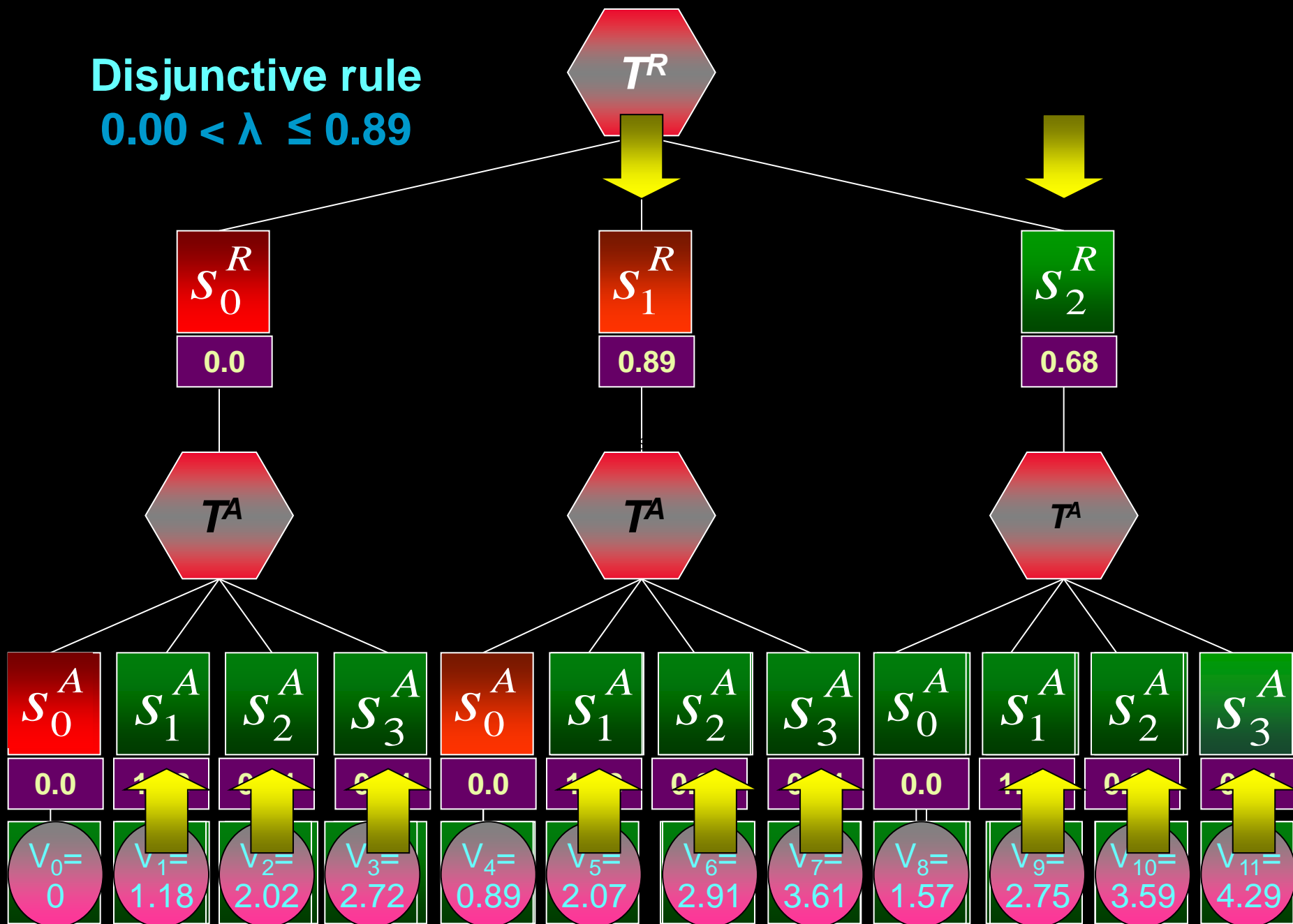




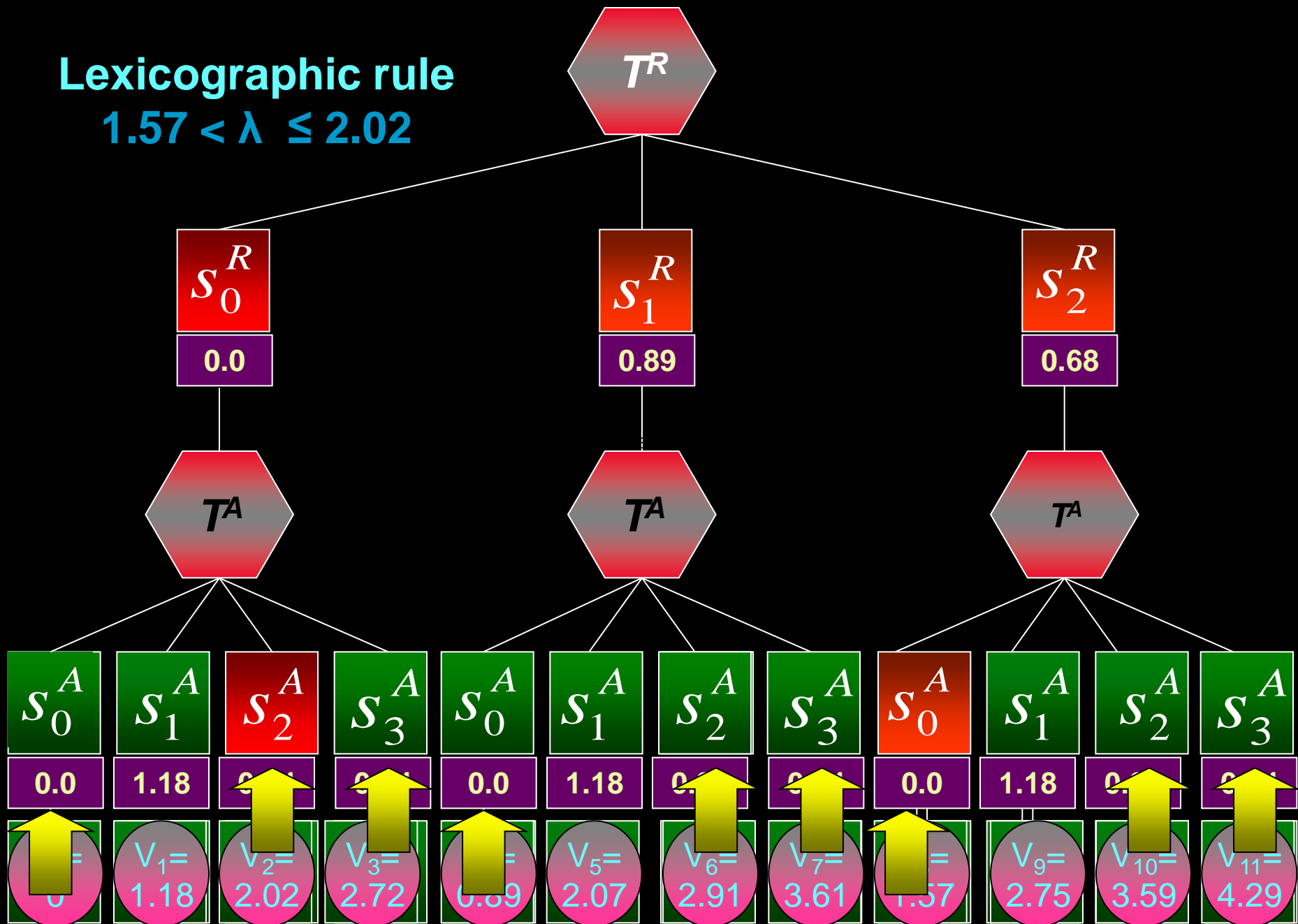
Conjunctive rule  
 $3.61 \leq \lambda \leq 4.29$



Disjunctive rule  
 $0.00 < \lambda \leq 0.89$

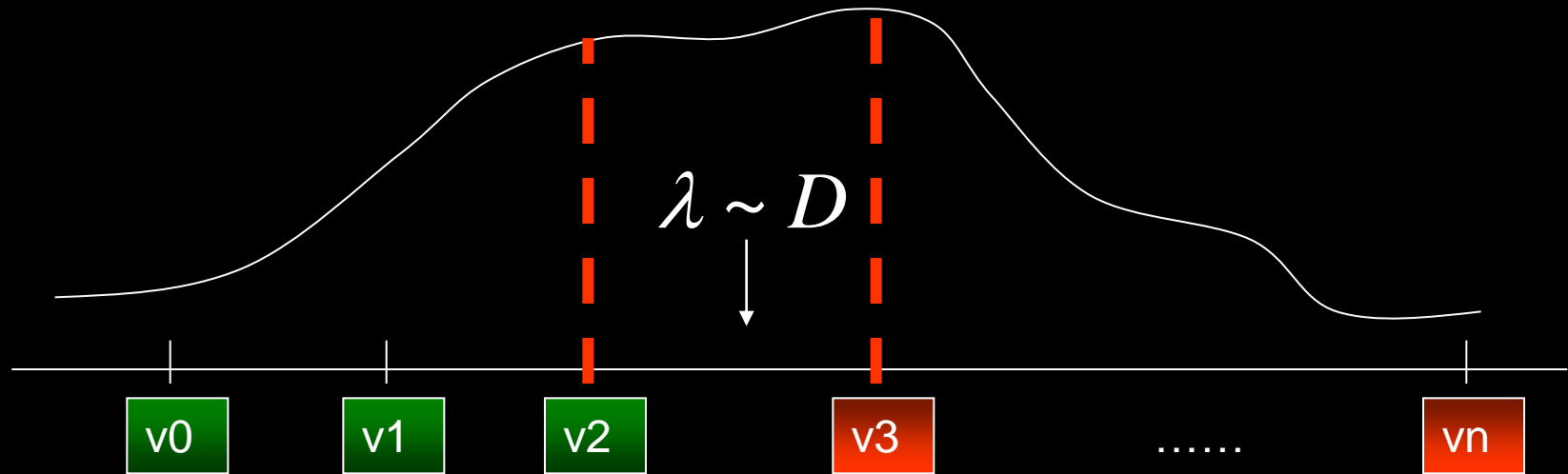


Lexicographic rule  
 $1.57 < \lambda \leq 2.02$



$$v_n + \varepsilon \geq \lambda \Leftrightarrow v_n \geq \lambda \sim D$$

Stochastic contextual factor



The probability of a preference is equivalent to the probability of  $\lambda$  being in the invariant range.

$$p_{k+1} = \int_{v_k}^{v_{k+1}} D \times dt$$



$s_0^R$	$s_1^R$	$s_2^R$	$s_0^A$	$s_1^A$	$s_2^A$	$s_3^A$
$s_0^R$	$s_1^R$	$s_2^R$	$s_0^A$	$s_1^A$	$s_2^A$	$s_3^A$
$s_0^R$	$s_1^R$	$s_2^R$	$s_0^A$	$s_1^A$	$s_2^A$	$s_3^A$
$s_0^R$	$s_1^R$	$s_2^R$	$s_0^A$	$s_1^A$	$s_2^A$	$s_3^A$
$s_0^R$	$s_1^R$	$s_2^R$	$s_0^A$	$s_1^A$	$s_2^A$	$s_3^A$
$s_0^R$	$s_1^R$	$s_2^R$	$s_0^A$	$s_1^A$	$s_2^A$	$s_3^A$
$s_0^R$	$s_1^R$	$s_2^R$	$s_0^A$	$s_1^A$	$s_2^A$	$s_3^A$
$s_0^R$	$s_1^R$	$s_2^R$	$s_0^A$	$s_1^A$	$s_2^A$	$s_3^A$
$s_0^R$	$s_1^R$	$s_2^R$	$s_0^A$	$s_1^A$	$s_2^A$	$s_3^A$
$s_0^R$	$s_1^R$	$s_2^R$	$s_0^A$	$s_1^A$	$s_2^A$	$s_3^A$
$s_0^R$	$s_1^R$	$s_2^R$	$s_0^A$	$s_1^A$	$s_2^A$	$s_3^A$
$s_0^R$	$s_1^R$	$s_2^R$	$s_0^A$	$s_1^A$	$s_2^A$	$s_3^A$

- $V_0 = 0$
- $V_1 = 1.18$
- $V_2 = 2.02$
- $V_3 = 2.72$
- $V_4 = 0.89$
- $V_5 = 2.07$
- $V_6 = 2.91$
- $V_7 = 3.61$
- $V_8 = 1.57$
- $V_9 = 2.75$
- $V_{10} = 3.59$
- $V_{11} = 4.29$

$s_0^R$	$s_1^R$	$s_2^R$	$s_0^A$	$s_1^A$	$s_2^A$	$s_3^A$
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$s_0^R$	$s_1^R$	$s_2^R$	$s_0^A$	$s_1^A$	$s_2^A$	$s_3^A$
$s_0^R$	$s_1^R$	$s_2^R$	$s_0^A$	$s_1^A$	$s_2^A$	$s_3^A$
$s_0^R$	$s_1^R$	$s_2^R$	$s_0^A$	$s_1^A$	$s_2^A$	$s_3^A$
$s_0^R$	$s_1^R$	$s_2^R$	$s_0^A$	$s_1^A$	$s_2^A$	$s_3^A$
$s_0^R$	$s_1^R$	$s_2^R$	$s_0^A$	$s_1^A$	$s_2^A$	$s_3^A$
$s_0^R$	$s_1^R$	$s_2^R$	$s_0^A$	$s_1^A$	$s_2^A$	$s_3^A$
$s_0^R$	$s_1^R$	$s_2^R$	$s_0^A$	$s_1^A$	$s_2^A$	$s_3^A$
$s_0^R$	$s_1^R$	$s_2^R$	$s_0^A$	$s_1^A$	$s_2^A$	$s_3^A$
$s_0^R$	$s_1^R$	$s_2^R$	$s_0^A$	$s_1^A$	$s_2^A$	$s_3^A$
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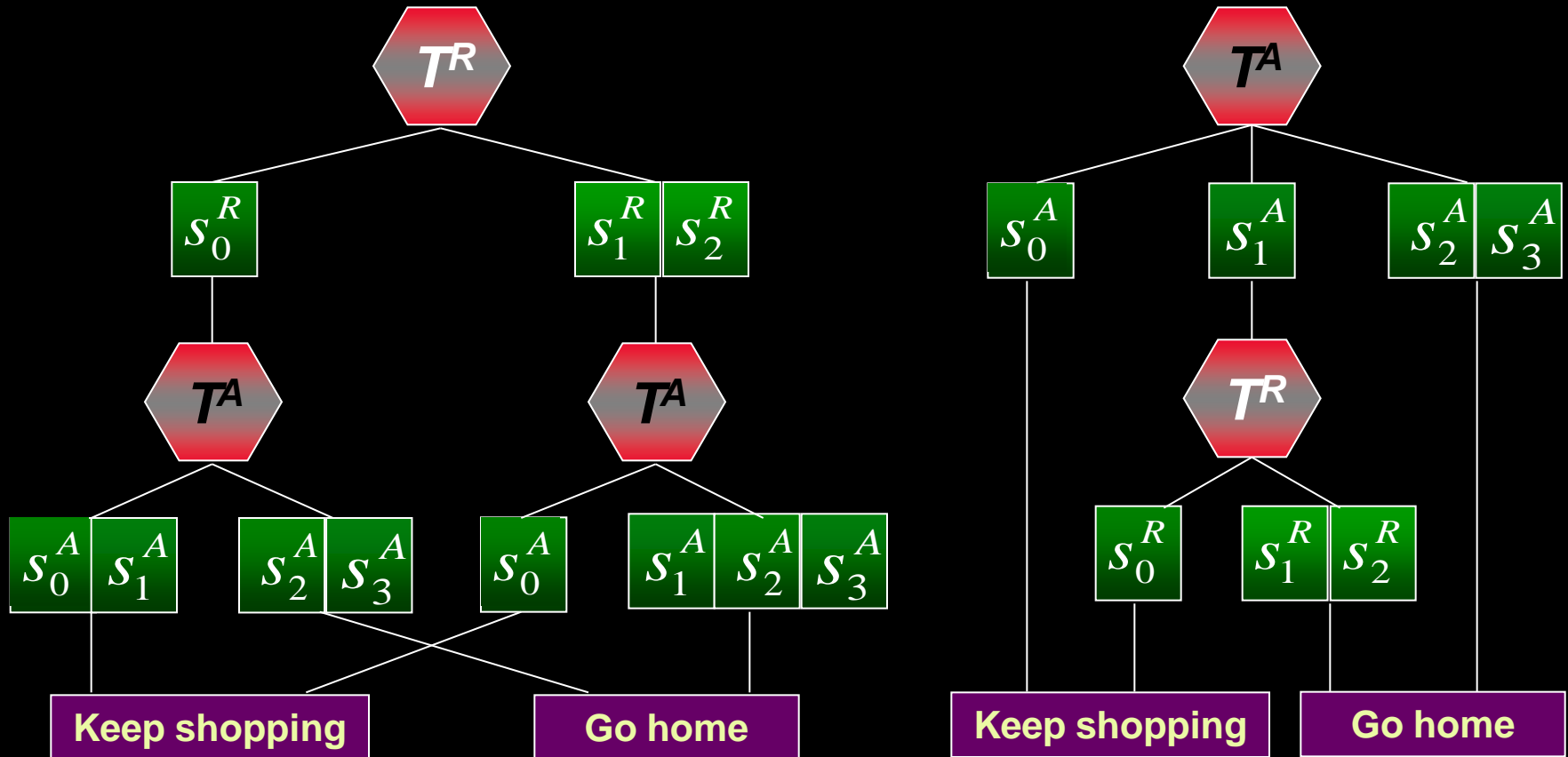
PREFERENCE TOLERANCE

# Mental effort

## Lexicographic rule

$$1.57 < \lambda \leq 2.02$$

Homogeneous responses do not necessitate further search



$$E_h^{RA} = e^R + (p_0^R + p_1^R + p_2^R) \times e^A = e^R + e^A$$

$$E_h^{AR} = e^A + p_1^A \times e^R$$

To generalize...



$$e^A + \sum_i E^B + E^C$$



$$E^B = p_i e^B I_{ij}$$

$$I_{ij} = \begin{cases} 0, & \text{if all } v_{ijk} | i \text{ are rejected or accepted} \\ 1, & \text{otherwise} \end{cases}$$



$$E^C = \sum_j p_{ij} e^C I_{ijk}$$

$$I_{ijk} = \begin{cases} 0, & \text{if all } v_{ijk} | i, j \text{ are rejected or accepted} \\ 1, & \text{otherwise} \end{cases}$$



$$E_h = e^A + \sum_i p_i e^B I_{ij} + \sum_j p_{ij} e^C I_{ijk}$$

$v_{ijk} < \lambda$  or  $v_{ijk} \geq \lambda$

$s_0^A$	$s_1^A$	$s_0^B$	$s_1^B$	$s_2^B$	$s_0^C$	$s_1^C$
$s_0^A$	$s_1^A$	$s_0^B$	$s_1^B$	$s_2^B$	$s_0^C$	$s_1^C$
$s_0^A$	$s_1^A$	$s_0^B$	$s_1^B$	$s_2^B$	$s_0^C$	$s_1^C$
$s_0^A$	$s_1^A$	$s_0^B$	$s_1^B$	$s_1^A$	$s_0^C$	$s_1^C$
$s_0^A$	$s_1^A$	$s_0^B$	$s_1^B$	$s_2^B$	$s_0^C$	$s_1^C$
$s_0^A$	$s_1^A$	$s_0^B$	$s_1^B$	$s_2^B$	$s_0^C$	$s_1^C$
$s_0^A$	$s_1^A$	$s_0^B$	$s_1^B$	$s_2^B$	$s_0^C$	$s_1^C$
$s_0^A$	$s_1^A$	$s_0^B$	$s_1^B$	$s_2^B$	$s_0^C$	$s_1^C$
$s_0^A$	$s_1^A$	$s_0^B$	$s_1^B$	$s_2^B$	$s_0^C$	$s_1^C$
$s_0^A$	$s_1^A$	$s_0^B$	$s_1^B$	$s_2^B$	$s_0^C$	$s_1^C$
$s_0^A$	$s_1^A$	$s_0^B$	$s_1^A$	$s_2^B$	$s_0^C$	$s_1^C$
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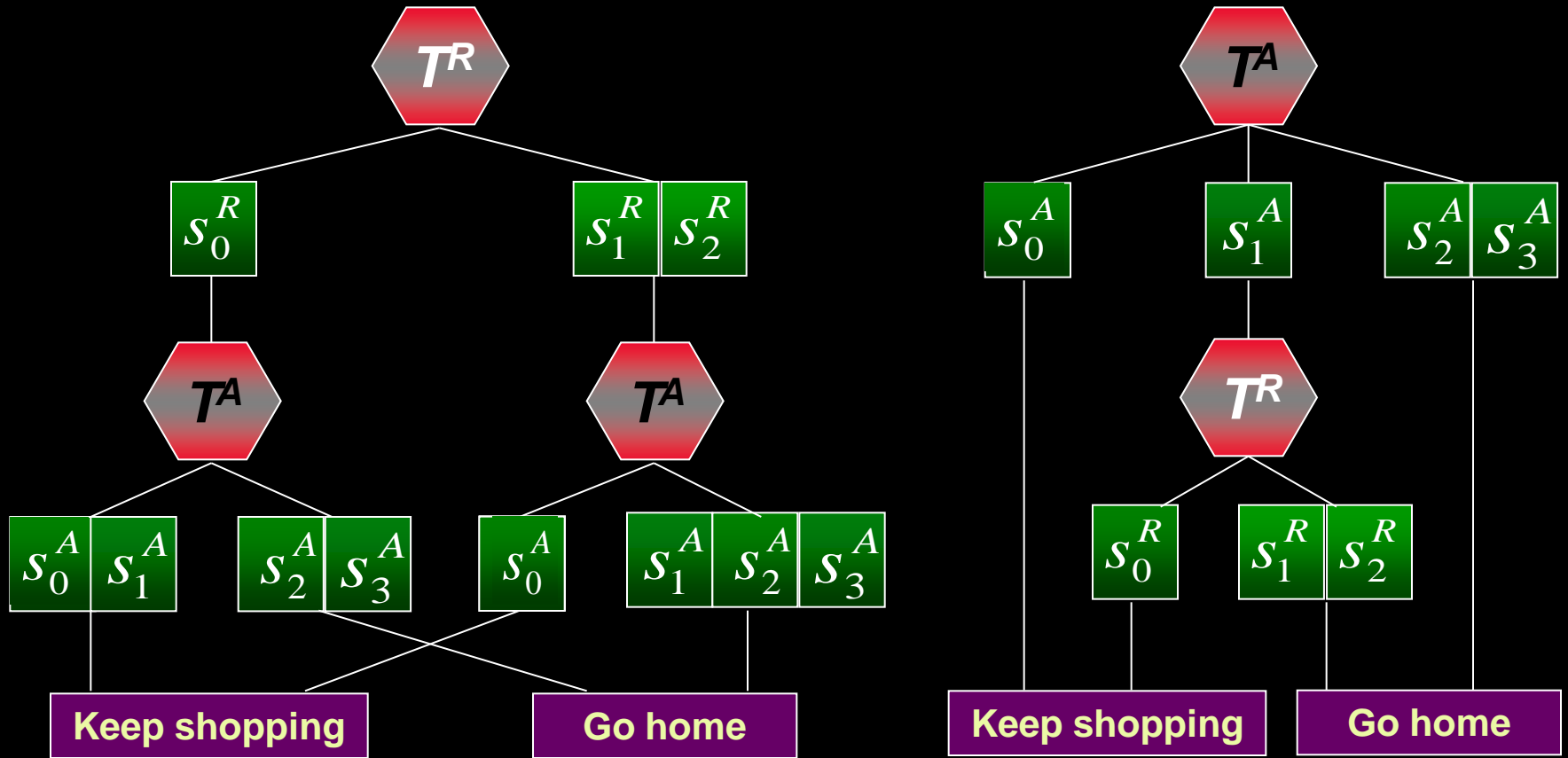
Mental effort						
e	p	e	i	p	e	i
e	p	e	i	p	e	i
e	p	e	i	p	e	i
e	p	e	i	p	e	i
e	p	e	i	p	e	i
e	p	e	i	p	e	i
e	p	e	i	p	e	i
e	p	e	i	p	e	i
e	p	e	i	p	e	i
e	p	e	i	p	e	i
e	p	e	i	p	e	i
e	p	e	i	p	e	i

?

# Risk attitude

$$R_h = -R_h^+ \log_2(R_h^+) - R_h^- \log_2(R_h^-)$$

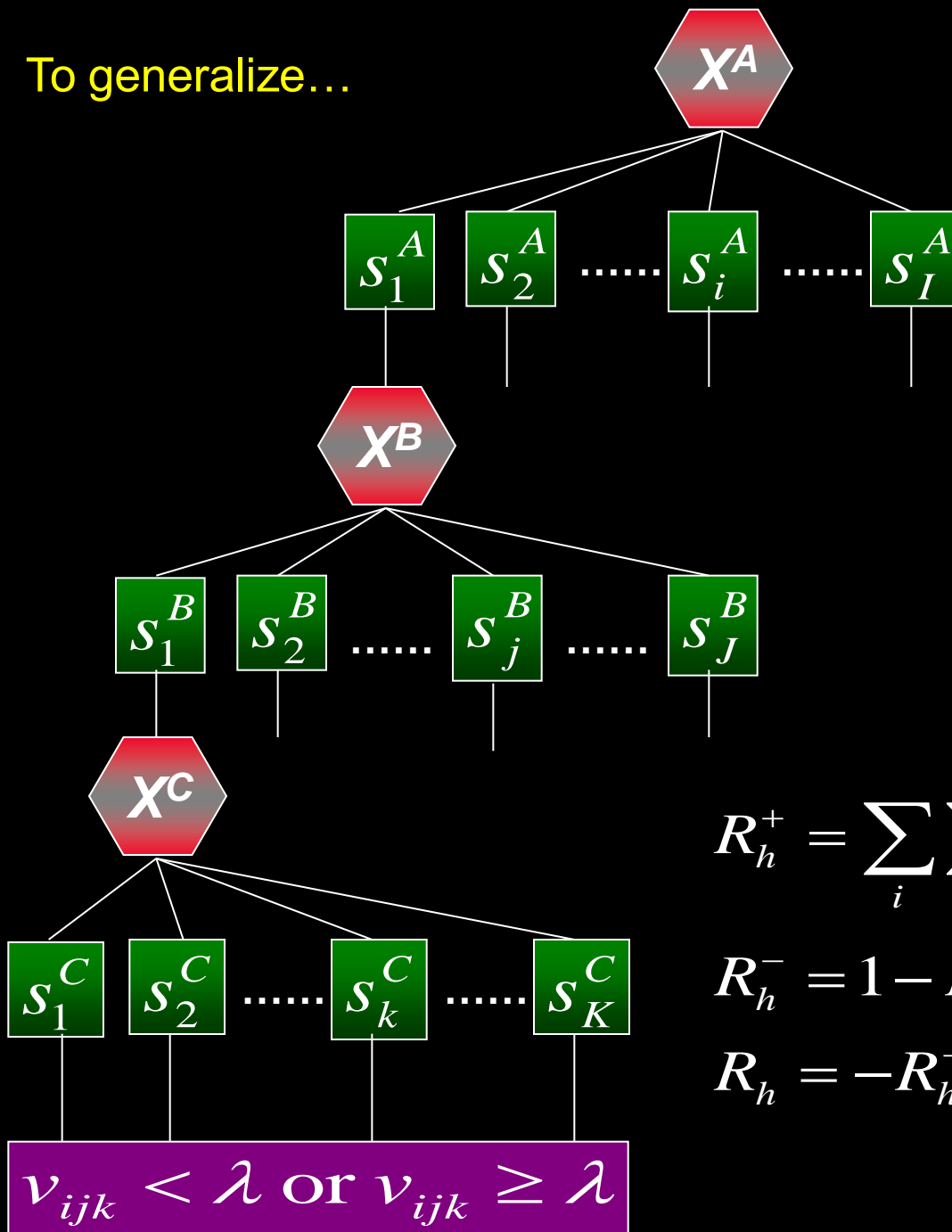
Shannon's Information Entropy as a measure of heuristic uncertainty



$$R_h^+ = p_0^R (p_2^A + p_3^A) + (p_1^R + p_2^R) (p_1^A + p_2^A + p_3^A) = p_1^A (p_1^R + p_2^R) + p_2^A + p_3^A$$

$$R_h^- = 1 - R_h^+$$

To generalize...

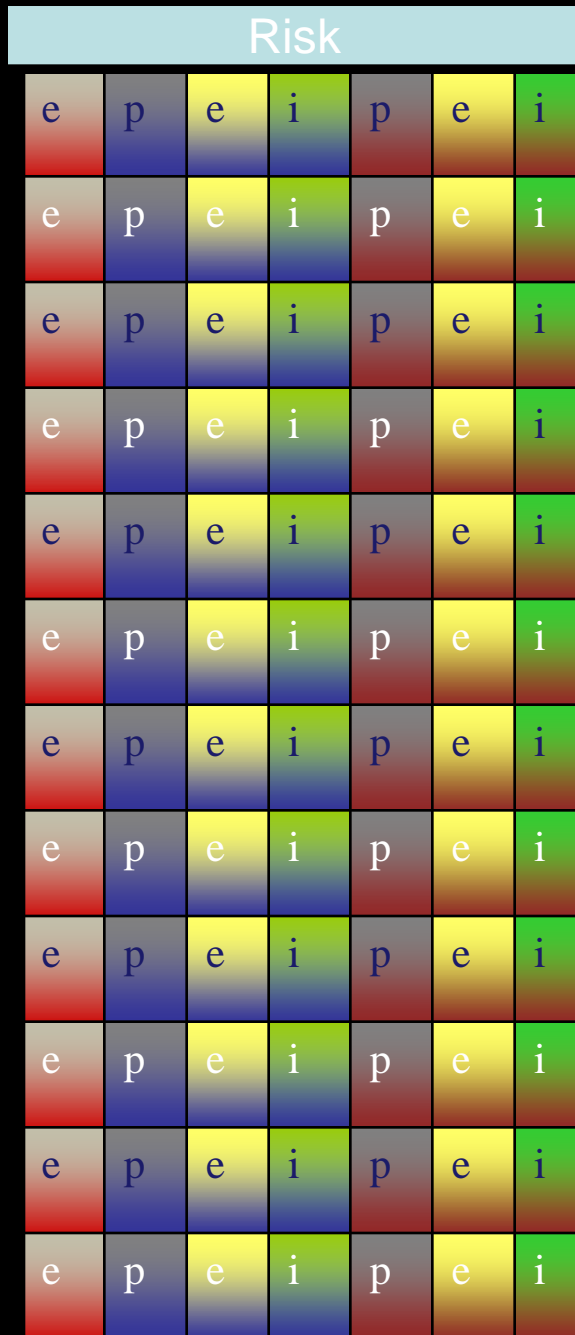


$$R_h^+ = \sum_i \sum_j \sum_k p_{ijk} \mid v_{ijk} \geq \lambda$$

$$R_h^- = 1 - R_h^+$$

$$R_h = -R_h^+ \log_2(R_h^+) - R_h^- \log_2(R_h^-)$$

$s_0^A$	$s_1^A$	$s_0^B$	$s_1^B$	$s_2^B$	$s_0^C$	$s_1^C$
$s_0^A$	$s_1^A$	$s_0^B$	$s_1^B$	$s_2^B$	$s_0^C$	$s_1^C$
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$s_0^A$	$s_1^A$	$s_0^B$	$s_1^B$	$s_2^B$	$s_0^C$	$s_1^C$
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$s_0^A$	$s_1^A$	$s_0^B$	$s_1^A$	$s_2^B$	$s_0^C$	$s_1^C$



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# Utility of heuristic



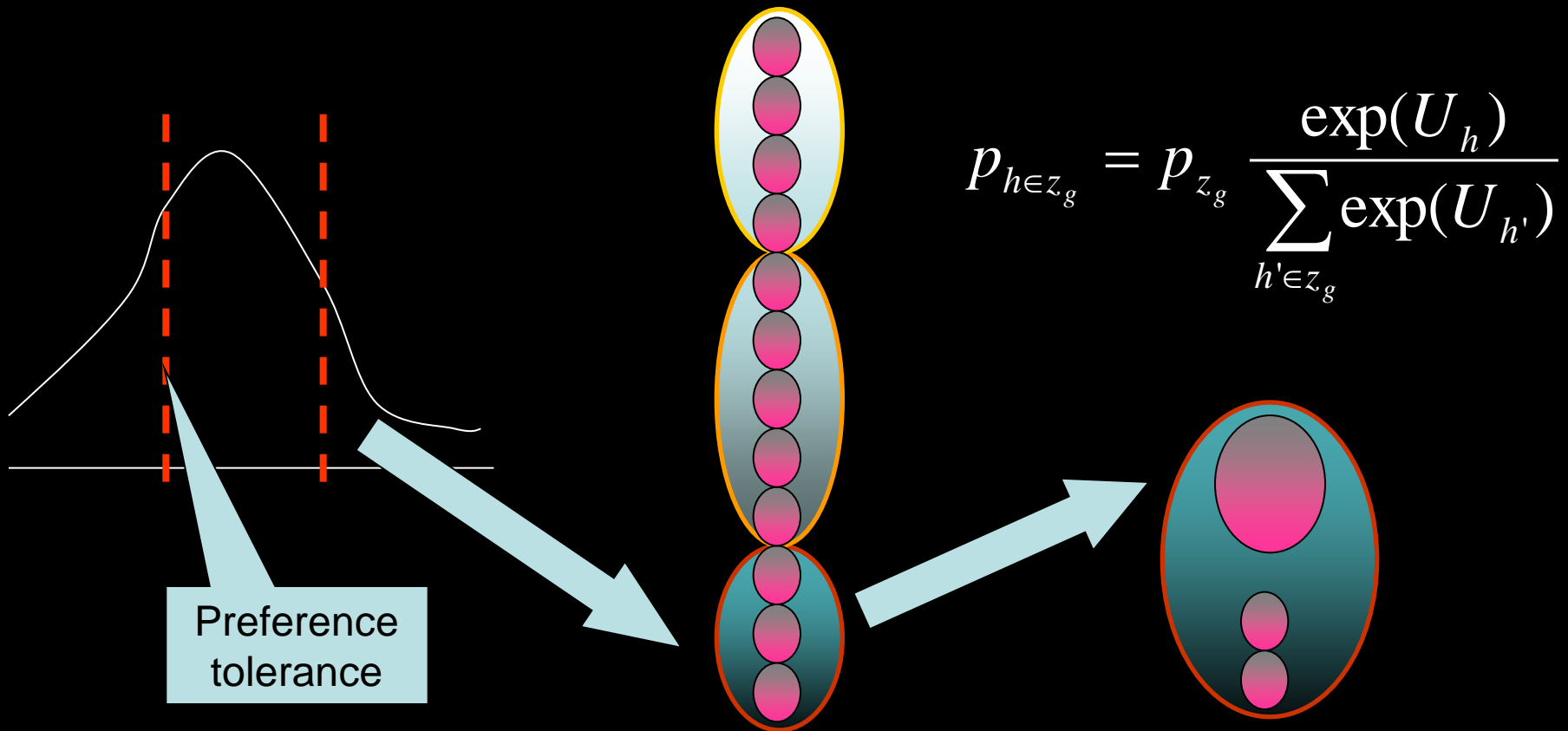
$$U_h = \beta_E E_h + \beta_R R_h$$

# Choice of heuristic

Step1: Discretize context

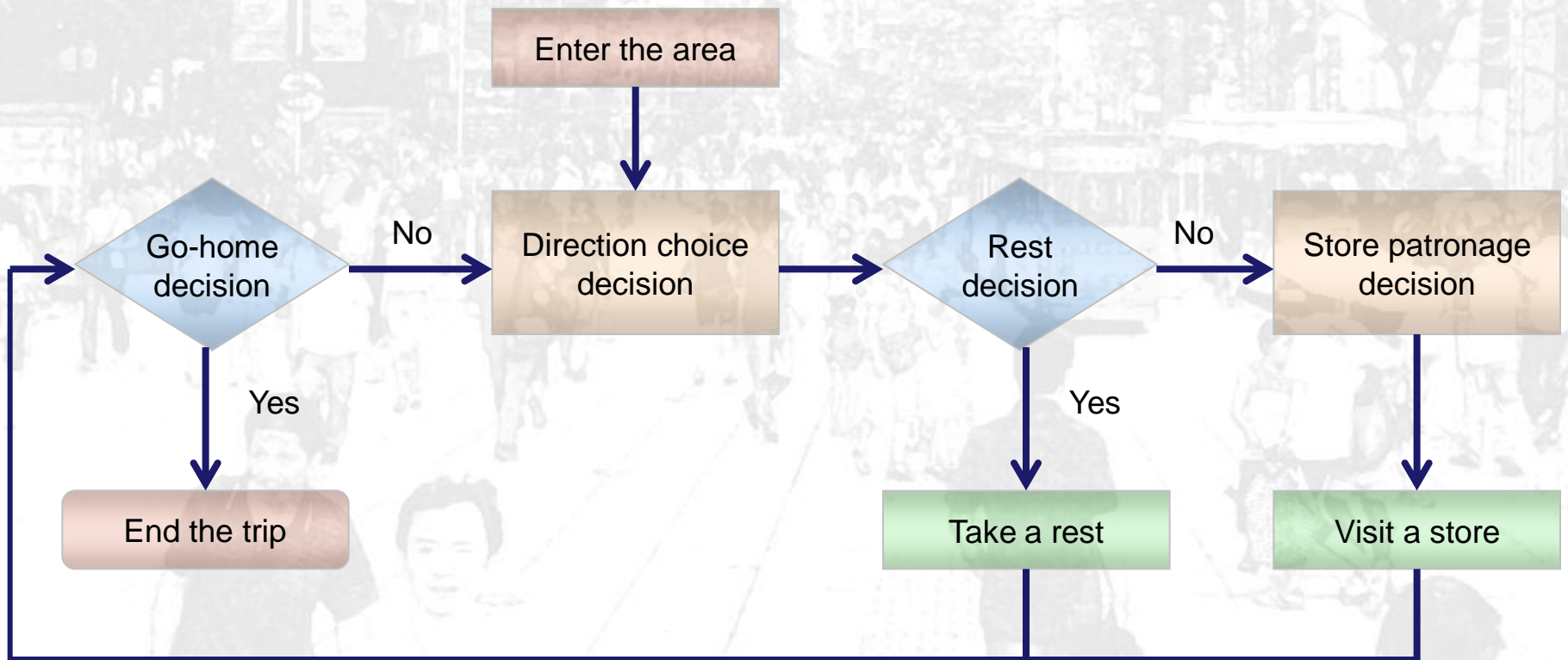
Step2: Identify preference group

Step3: Choose heuristic



# Conceptual Framework

- Decisions to model
  - Go home, direction choice, rest, store patronage



# Conceptual Framework

- Three model prototypes for comparison

MNL

- As the representative of rational choice models and a benchmark

PH

- Heuristic models with probabilistic threshold specifications

HHM

- The Heterogeneous Heuristic Model, which is the major methodological contribution of the thesis



# Problem Representation

- Concepts

- Attribute

$$X = \{x_j \mid j = 1, \dots, J\}$$

- Attribute threshold

$$\Delta_j = \{\delta_{j1} < \delta_{jn} < \delta_{jN}\}$$

- Attribute state

$$S_{jn} = \begin{cases} 0 & \text{if } x_j < \delta_{jn} \\ 1 & \text{if } x_j \geq \delta_{jn} \end{cases}$$

- State utility

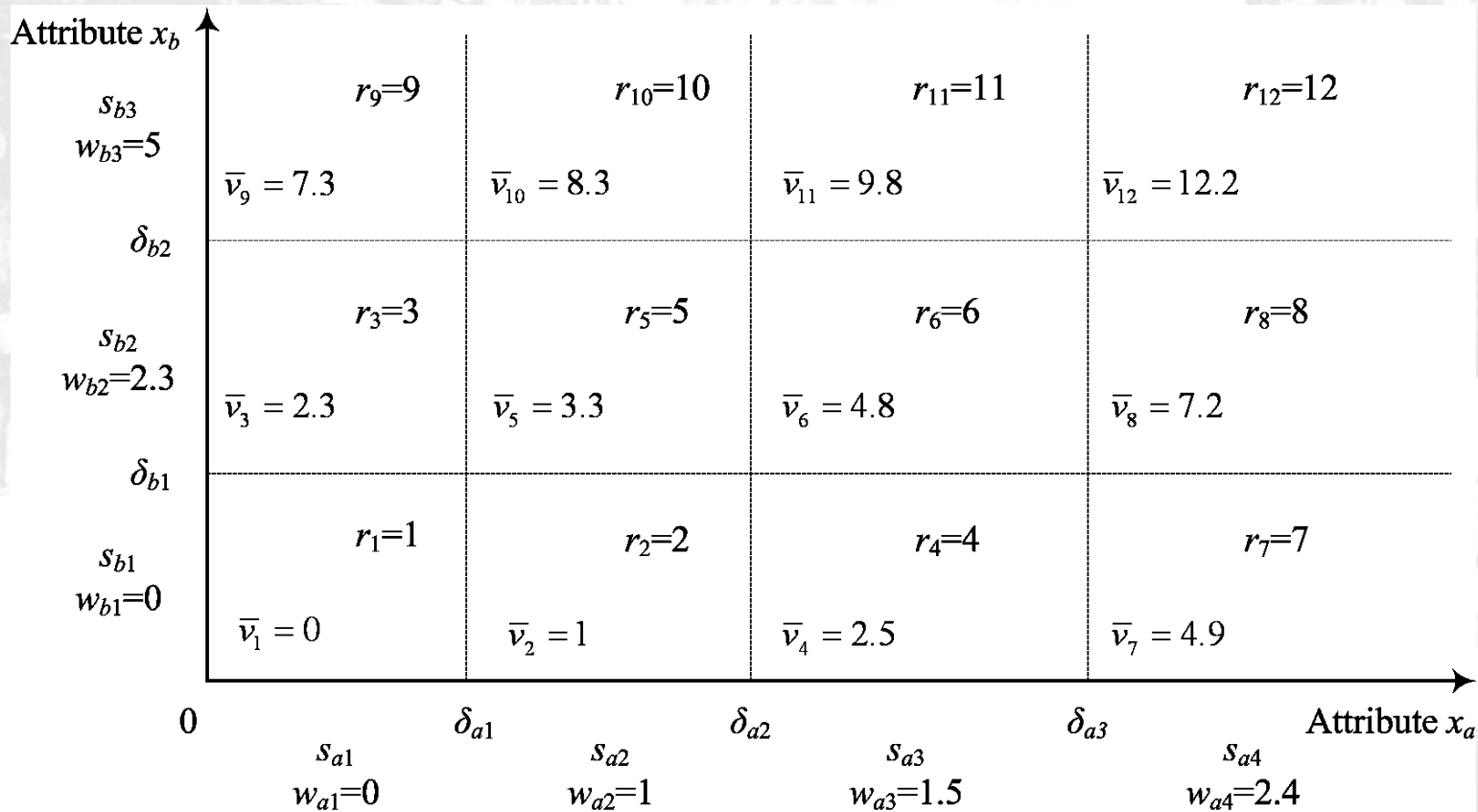
$$u_{jn} = w_{jn} S_{jn}$$

- Overall utility

$$v_i = \sum_j \sum_n u_{ijn}$$

# An Example

- Two-attribute representation





# Satisficing Decision

- A preference is a function of
  - Alternative rank
  - Reference rank
  - Decision criterion (discriminant threshold)

 $r_i$  $r_\varepsilon$  $\lambda_k$ 

$$d_i = \begin{cases} 1 & \text{if } r_i - r_\varepsilon \geq \lambda_k \quad \lambda_k \in [1, K] \\ 0 & \text{if } r_i - r_\varepsilon \leq -\lambda_k \\ 0.5 & \text{otherwise} \end{cases}$$



# Behavioral Heterogeneity

- We focus on the variation of decision criteria, because it is more common and easier to change criteria than representation.
- Using a latent class structure

- A decision criterion is selected based on its value  $d_i = \sum_{k=1}^K p_k d_{i|k}$

$$p_k = \frac{\exp(u_k)}{\sum_{k'=1}^K \exp(u_{k'})}$$

# Factors of Criterion Value

- Consistency

- Preference based on the criterion
- Preferences based on other criteria
- To what extent they are consistent?
- So that current choice is also robust in the future

Value of having consistent preferences

$$\psi_{l|k} = \sum_{k'=1}^K \eta_{k'} \mathbf{I}(d_{l|k'} = d_{l|k})$$

$$\eta_{k'|k} = \exp(\beta_{\psi} |k' - k|)$$

Positive: expecting different future preferences  
Negative: expecting similar future preferences

Probability belief of attribute state

$$p_l = \prod_j p_{jn}$$

Probability of overall state

$$\psi_k = \sum_l p_l \psi_{l|k}$$

# Factors of Criterion Value

- Definiteness
  - The probability of getting a definite result (clear discrimination between alternatives)

$$\gamma_k = \sum_l p_l \gamma_{l|k}$$

$$\gamma_{l|k} = I(d_{l|k} \neq 0.5)$$

- In total

$$u_k = \psi_k + \beta_\gamma \gamma_k$$

# What to Estimate?

- Attribute thresholds

$$\Delta_j = \{\delta_{j1}, \dots, \delta_{jN}\}$$

- Attribute utilities

$$W_j = \{w_{j1} = 0, w_{j2}, \dots, w_{jN+1}\}$$

- Reference rank

$$r_\varepsilon$$

- Parameters in criterion choice

$$\beta_\psi, \beta_\gamma$$

Technical problems in estimation

(1) Thresholds are non-continuous; numbers are estimated

(2) Attribute utilities are non-unique

(3) Conventional significance tests do not apply; using CAIC instead



# Illustration

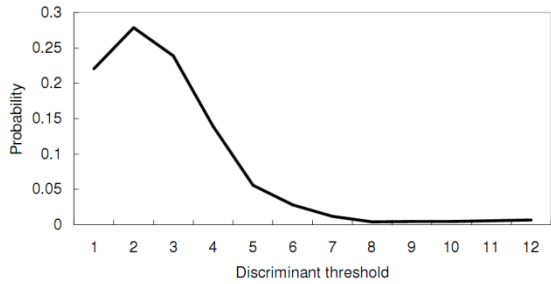
- Go-home decision: pedestrians' decision to end a shopping trip
- Three datasets of pedestrian shopping diary
  - East Nanjing Road, Shanghai (2003, 2007)
  - Wang Fujing Street, Beijing (2004)
- Attributes
  - Relative time ( $t^R$ ), absolute time ( $t^A$ )

# Parameter Estimates

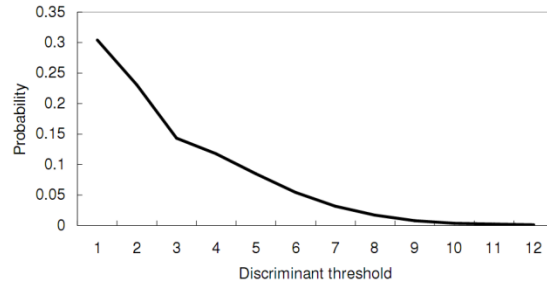
Parameter	ENR-03 Estimate	WFS-04 Estimate	ENR-07 Estimate
$\delta_1^R$	180 minutes	90 minutes	70 minutes
$\delta_2^R$	480 minutes	180 minutes	240 minutes
$[w_1^R]$	1	1	1
$w_2^R$	0.720	0.561	0.104
$\delta_1^A$	14:30	14:00	14:30
$\delta_2^A$	17:00	16:00	19:30
$\delta_3^A$	20:00	19:00	-
$w_1^A$	5.860	7.143	0.504
$w_2^A$	0.274	0.664	1.019
$w_3^A$	0.734	0.337	-
$r_\epsilon$	8	10	7
$\theta_\psi$	0.023	-0.253	0.188
$\theta_\gamma$	9.610	6.822	6.410

# Use of Criteria

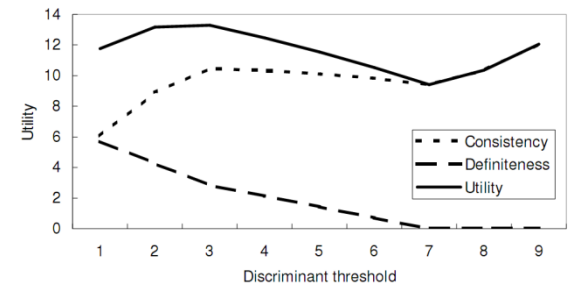
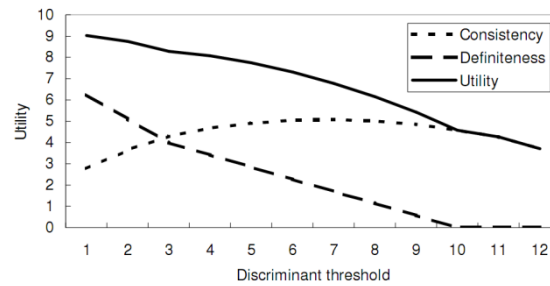
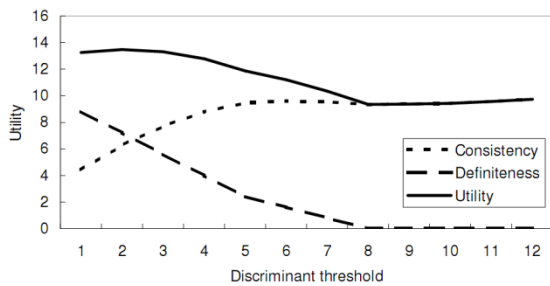
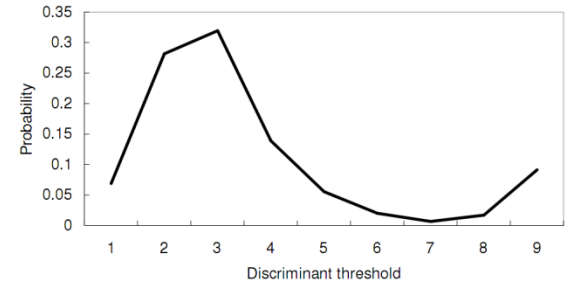
ENR-03



WFS-04



ENR-07





# Goodness-of-fits

Parameter	ENR-03			WFS-04			ENR-07		
	Proposed	MNL	Mixed	Proposed	MNL	Mixed	Proposed	MNL	Mixed
LL	-730	-789	-788	-1037	-1085	-1079	-402	-410	-409
$N_C$	1926	1926	1926	2741	2741	2741	808	808	808
$N_p$	12	3	6	12	3	6	10	3	6
CAIC	1562	1603	1628	2181	2197	2211	880	843	866

LL: log-likelihood

$N_C$ : number of cases

$N_p$ : number of parameters

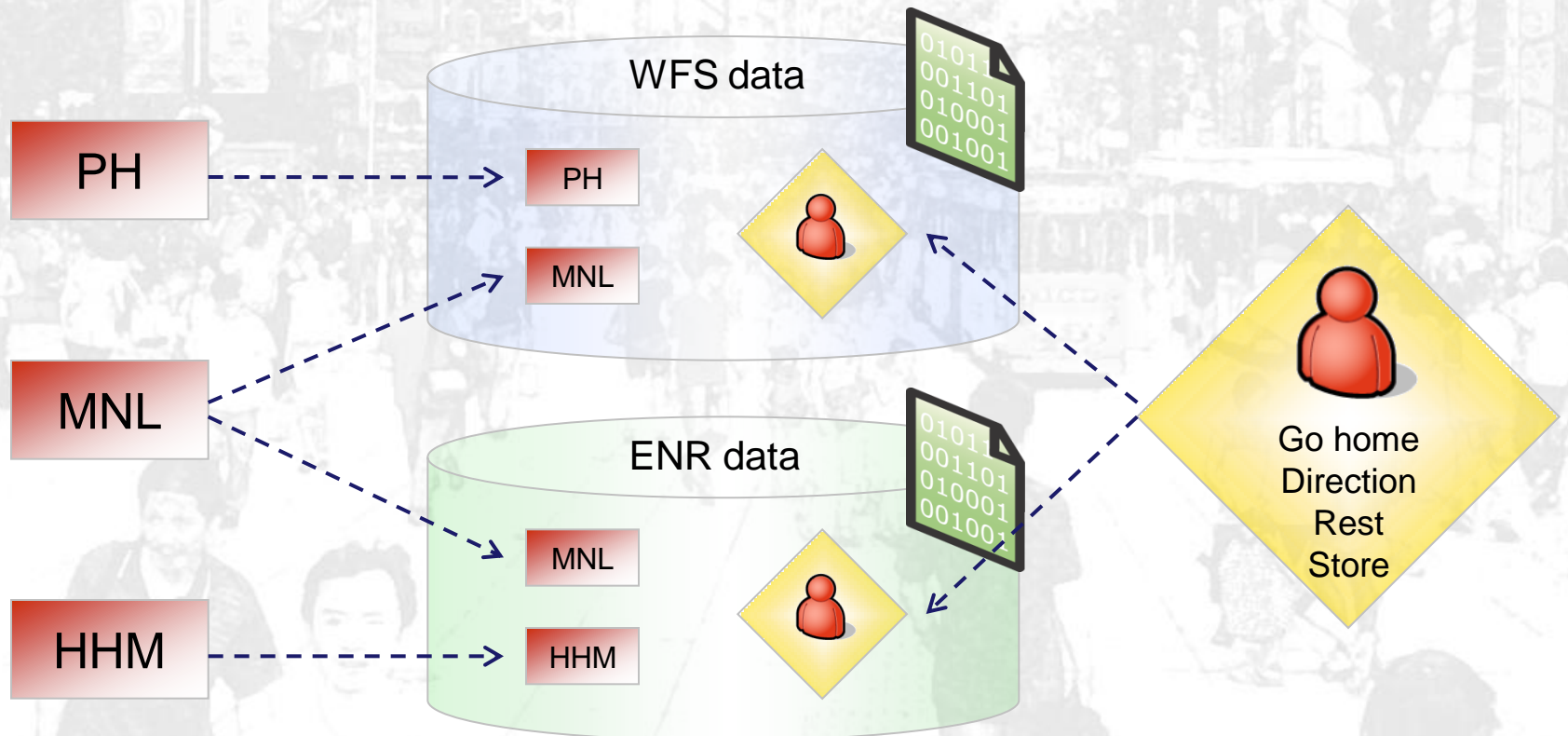
CAIC: Consistent Akaike Information Criterion

# Conclusion

- **Theoretical**
  - Model behavioral heterogeneity by explicitly taking into account the variation of decision criteria
  - Choice of criteria explained by consistency and definiteness
- **Empirical**
  - Definiteness is the dominant factor; pedestrians prefer using relaxed criteria
  - Consistency is less influential; pedestrians' expectations on future preferences are diverse
  - Better capture heterogeneity for large samples

# Model Estimation

- Each of the three prototype models is specified for each of the four decisions and estimated against data.



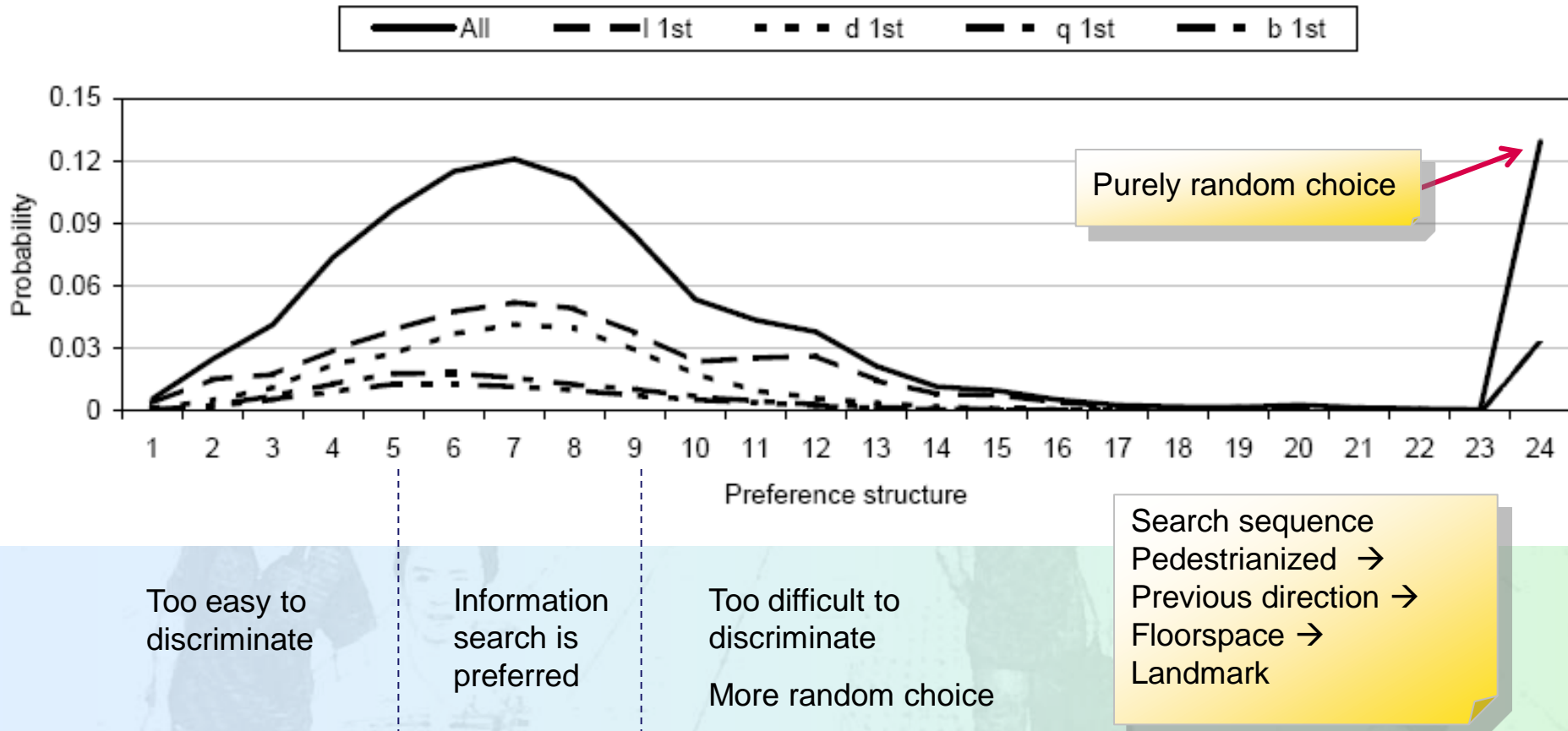
# Model Estimation

- Models are compared in terms of Log-likelihood statistics and Consistent Akaike Information Criterion.
- In general, heuristic models are better than MNL models, suggesting pedestrians using simplifying decision strategies.

Decision	WFS		ENR	
	Best LL	Best CAIC	Best LL	Best CAIC
Go-home	LEX	CONJ	HHM	MNL logged
Direction choice	LEX	LEX	HHM	HHM
Rest	CONJ	LEX	HHM	MNL logged
Store patronage	LEX	LEX	HHM	HHM

# Model Estimation

- The major advantage of HHM is to estimate the probabilistic use of heuristics.





# Conclusion

1

## BR model

- The advantage of using BR models to modeling pedestrian decision processes is partially justified, suggesting a promising new line of behavior / decision modeling.

2

## Heterogeneity

- HHM provides a potential framework for modeling the formation and choice of heuristics, which may contribute to decision research at large.

3

## Time

- Including temporal factors is valuable for capturing dynamic pedestrian behavior. However, temporal change in behavior was not estimated.



# MODEL OF MENTAL REPRESENTATION AND ACTIVATION



# Assumptions

Individuals construct and activate a mental model

This representation involves causal mechanisms, linking decision problem and situational variables to outcomes

It involves a subjective representation of the environment and beliefs

It involves an assessment of size of benefits

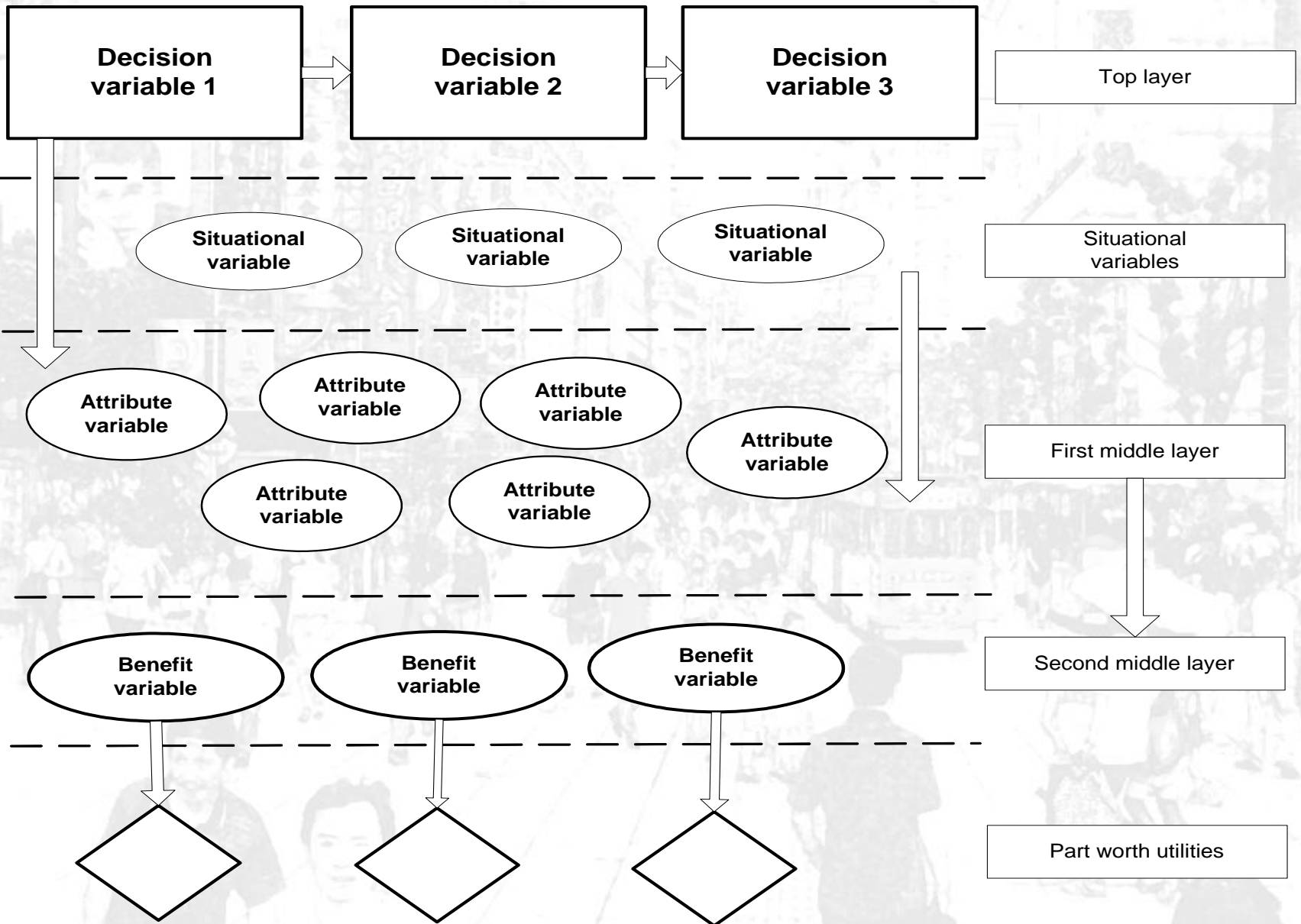


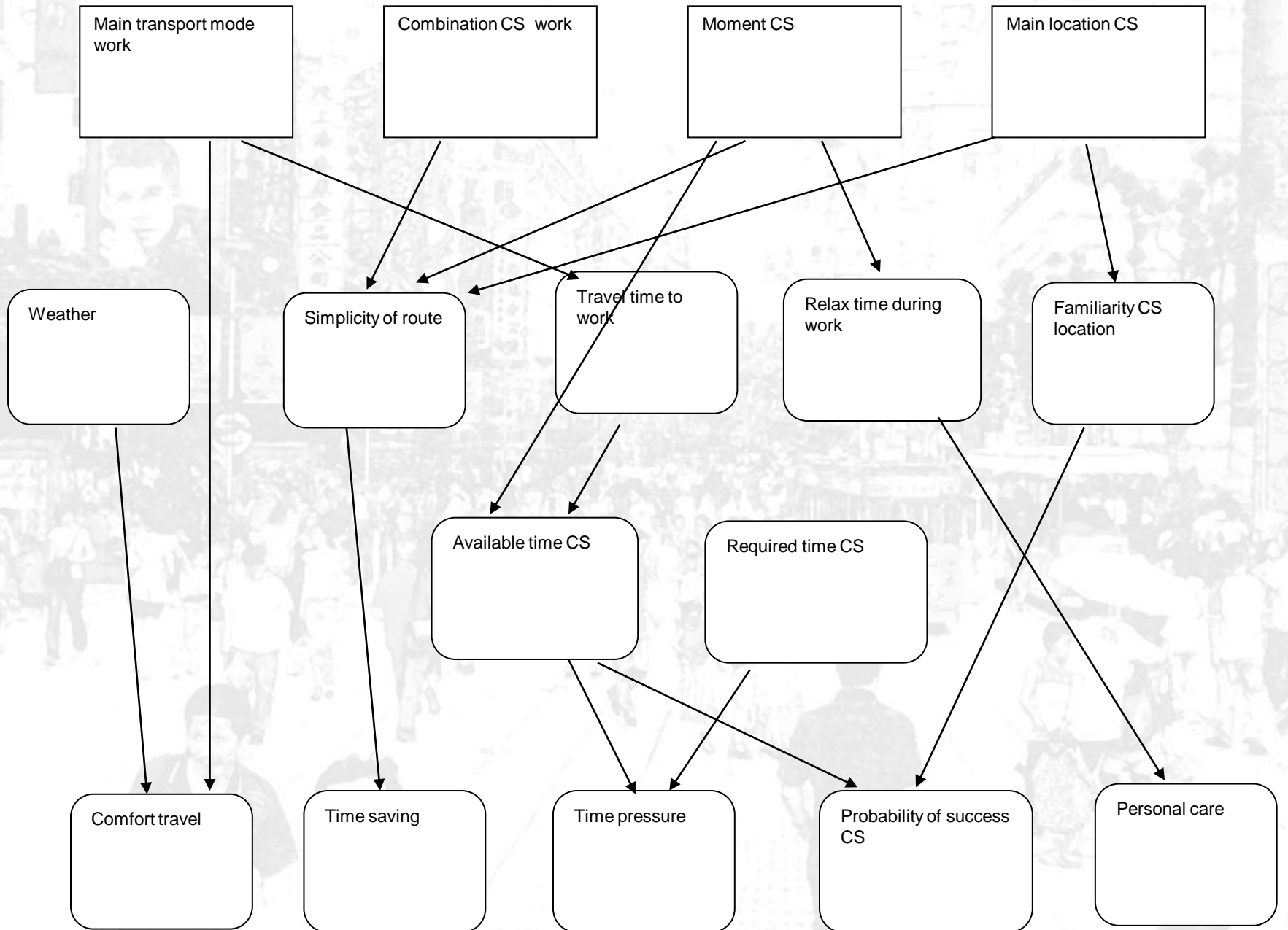
# Theory

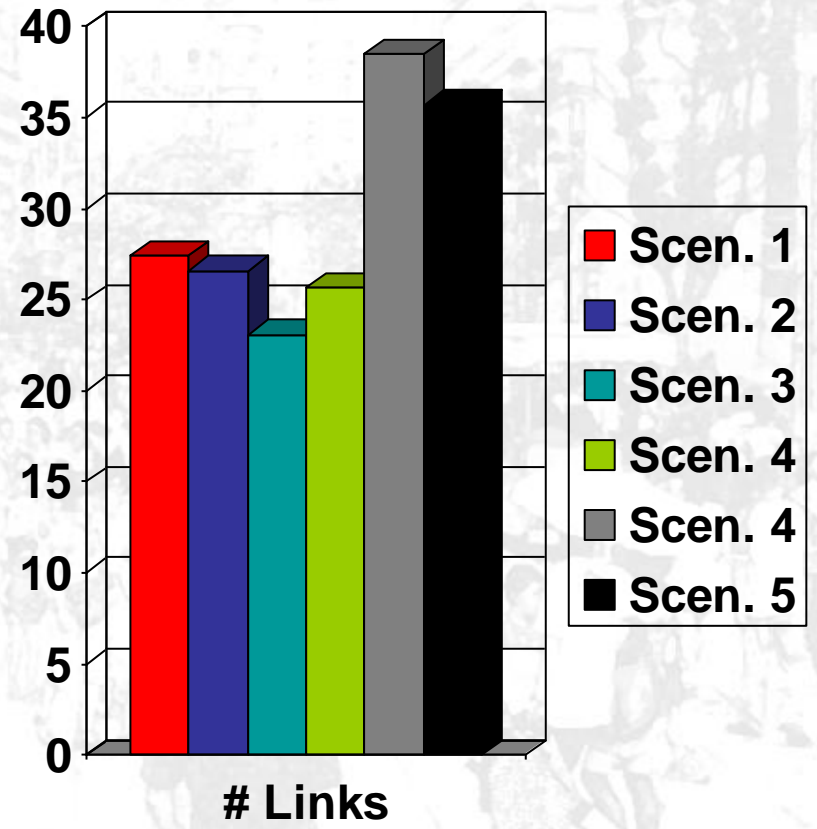
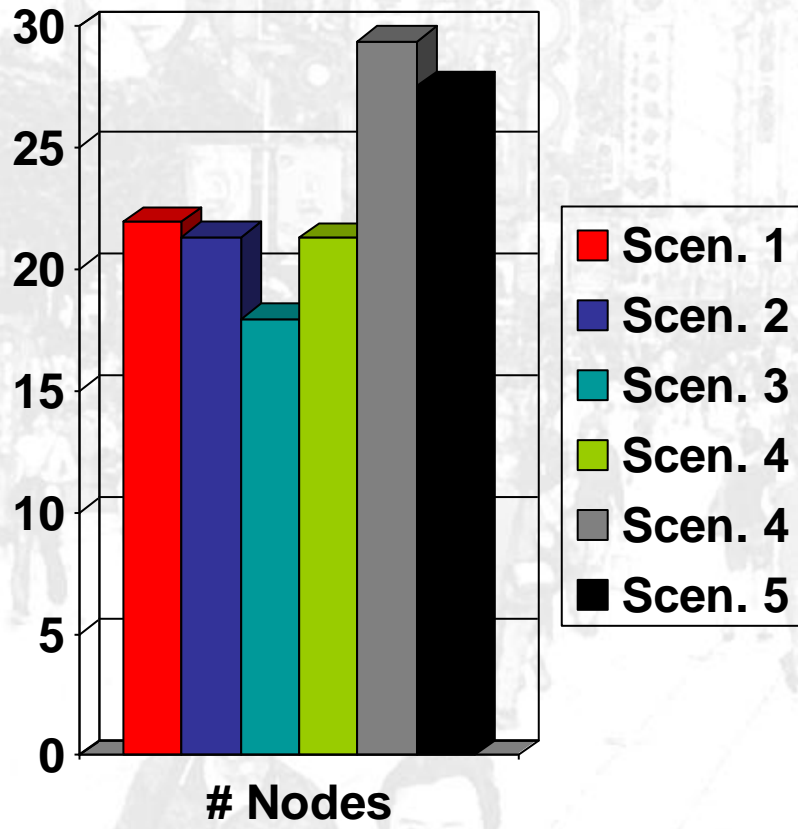
Mental model is a temporary and active cognitive structure, tailored to the specific settings of the task

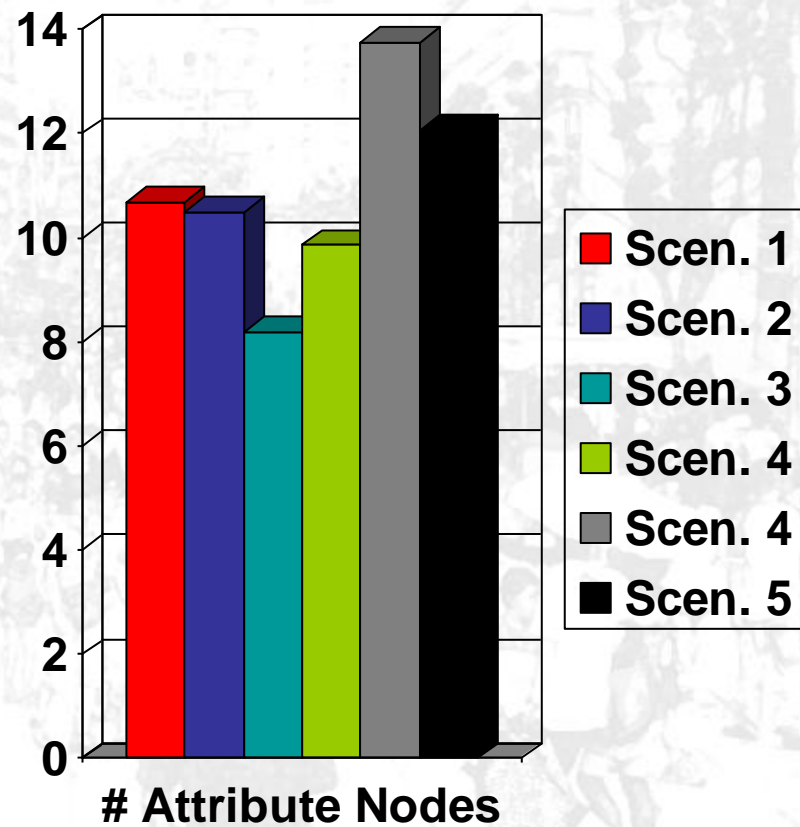
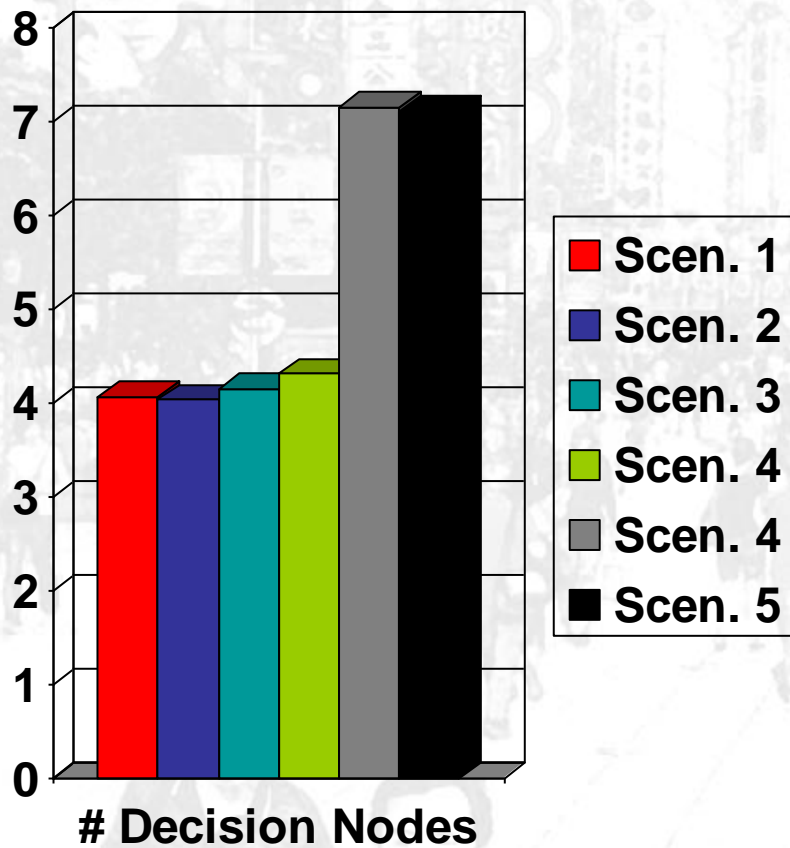
It serves to reduce the complexity of the decision task

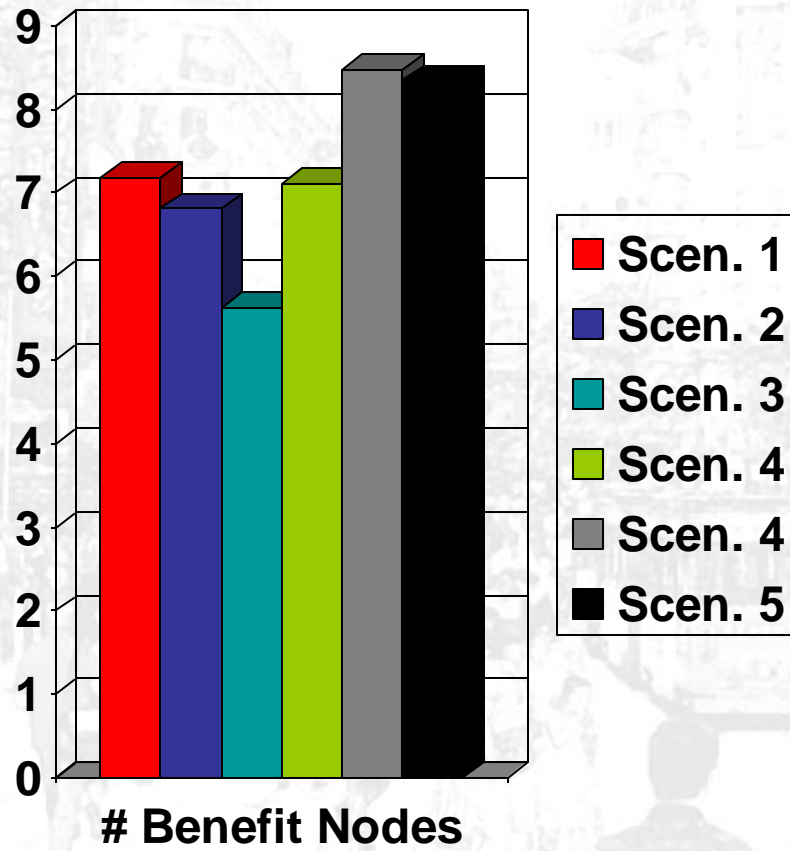
It allows individual to solve the problem within the boundaries of his rationality













Dependent variable	Grouping variable	F	Sig,
Number of nodes (total)	Scenario	37,263	0,000
	Interviewer	7,371	0,001
	Scenario x interviewer	0,883	0,883
Number of links	Scenario	35,572	0,000
	Interviewer	5,613	0,004
	Scenario x interviewer	0,452	0,918
Decision nodes	Scenario	322,904	0,000
	Interviewer	0,586	0,558
	Scenario x interviewer	0,846	0,585
Number of attribute nodes	Scenario	15,431	0,000
	Interviewer	2,189	0,115
	Scenario x interviewer	0,825	0,606
Number of benefit nodes	Scenario	11,319	0,000
	Interviewer	15,596	0,000
	Scenario x interviewer	0,653	0,766

# Model

$$r_{ij}(x_{jkg}) = \beta_{kg}^{ij}$$

where

$x_{jkg}$  is an (expected) outcome of alternative  $g$  of decision variable  $k$  on attribute  $j$ .

$r_{ij}$  is an evaluation of the extent to which this outcome matches the most desired outcome given the need associated with benefit  $i$ .

$\beta_{kg}^{ij}$  is a corresponding systematic utility value.



# Model

A perceived gain of a DAB chain evaluation is defined as the size of utility difference it reveals compared to the case where the chain is not inspected

$$Z_{ijk} = SD(\beta_{k\bullet}^{ij})$$

Utility values are based on expectations that the individual derives from broader knowledge about the world and his or her own needs. A key distinction in this knowledge structure must be made between knowledge about relevant attributes and benefit components and the causal network connecting these components and how they relate to alternatives and the individual's own needs

$$\alpha_i \cdot s_{ij}^1 \cdot s_{jk}^2 \cdot r'_{ij}(x_{jkg}) = \beta_{kg}^{ij}$$

# Model

$$SD[r'_{ij}(x_{jk\bullet})] \equiv 1$$

$$Z_{ijk} = SD[\alpha_i \cdot s_{ij}^1 \cdot s_{jk}^2 \cdot r'_{ij}(x_{jkg})]$$

$$= \alpha_i \cdot s_{ij}^1 \cdot s_{jk}^2 \cdot SD[r'_{ij}(x_{jkg})]$$

$$= \alpha_i \cdot s_{ij}^1 \cdot s_{jk}^2$$

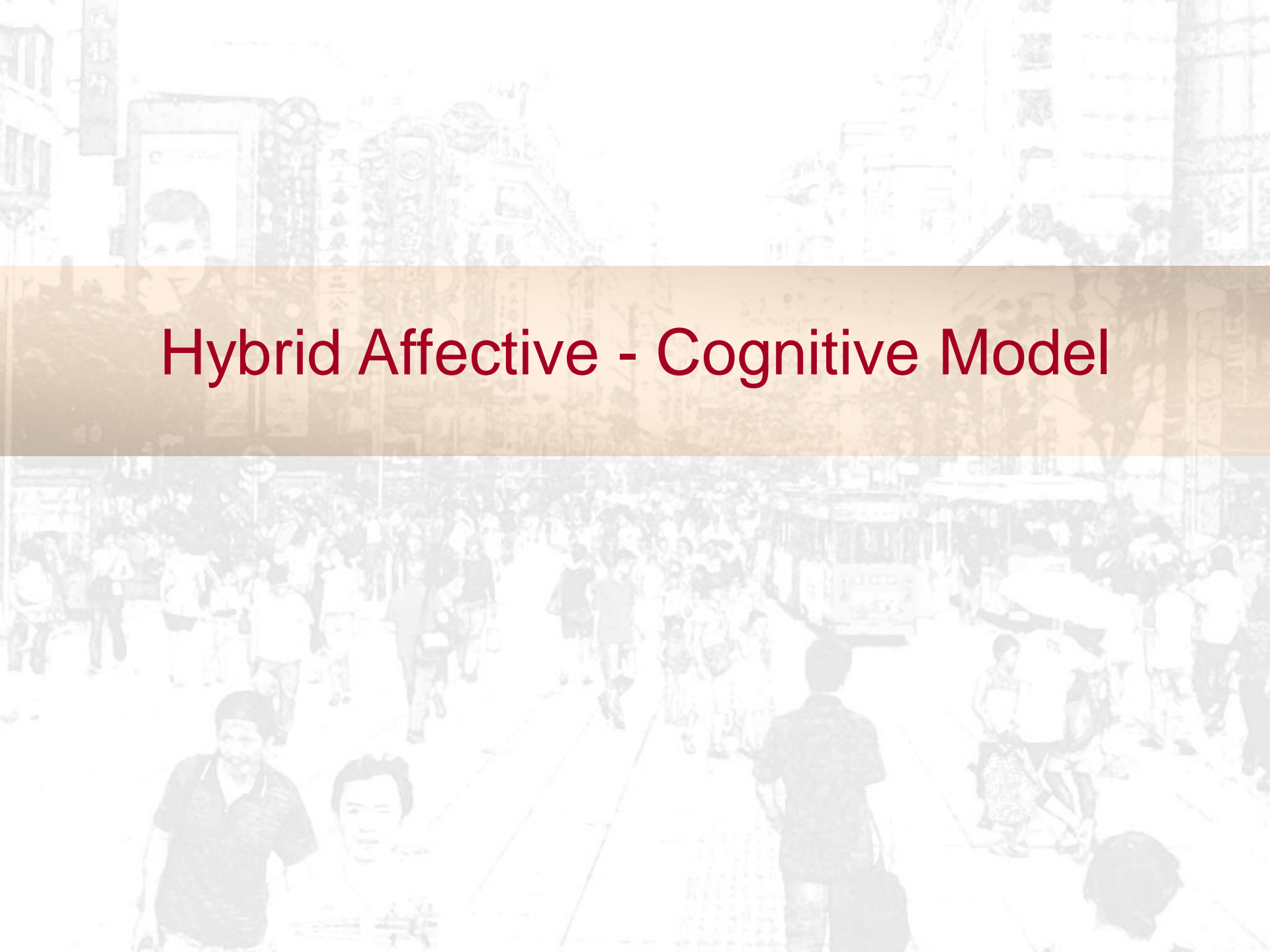
# Model

## Mental Costs

$$C_{ijk} = c_{ij} + c_{jk}$$

$$U_{ijk} = Z_{ijk} - C_{ijk}$$

$$P[(i, j, k) \in MR] = P(U_{ijk} > 0)$$



# Hybrid Affective - Cognitive Model

# ENVIRONMENT

Physical

Stationary attributes

Transportation system

Semi-stationary attributes

Institutional context

Non-stationary attributes (endogenous)

Uncertainty

# COGNITIVE ENVIRONMENT

Context-dependent,  
time-varying

Beliefs, based on incomplete, imperfect perception

Differential awareness

# JUDGMENT and CHOICE

Context-dependent,  
time-varying

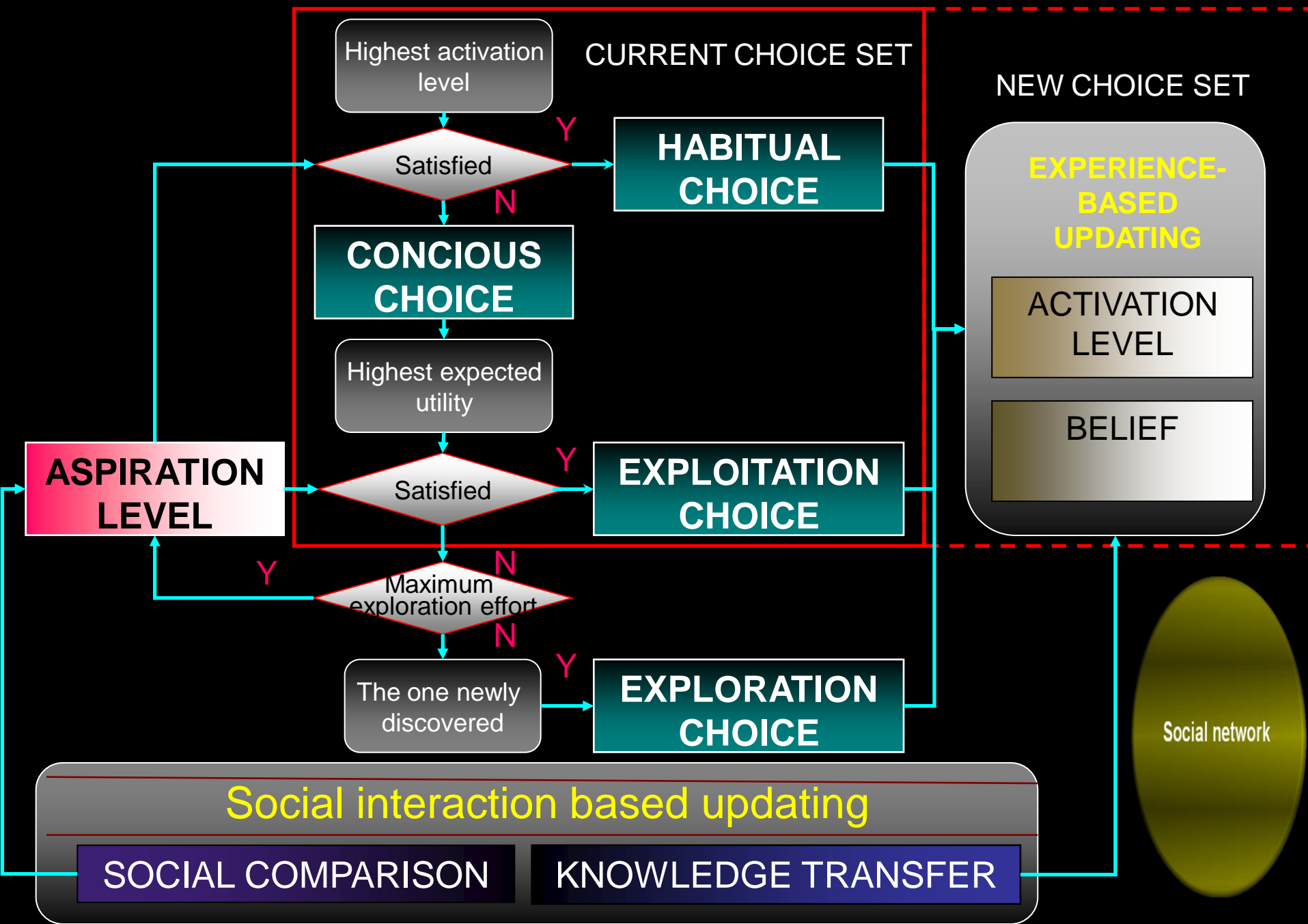
Aspiration level, mental effort and expected utility

Constraints and resources

Scripts, routines and heuristics



# Process Model





- Associate with each alternative under specific context conditions
- Indicate memory strength
- Determine whether or not the alternative stays in the choice set
- Habit developing by repeated choices
- ▶ Degree of awareness

NEW CHOICE SET

EXPERIENCE-BASED UPDATING

ACTIVATION LEVEL

BELIEF

CHOICE

Highest expected utility

ASPIRATION LEVEL

Satisfied

EXPLOITATION CHOICE

- Individual reference for the outcome
- Defined at attribute levels
- Context dependent
- Having predefined tolerance range
- Link with social network
- ▶ Willingness to change

- Reflect current knowledge of environment
- Attributes of alternative (static & dynamic)
- ▶ Evaluation given current knowledge

LORA

CHOICE

update

EDGE



# SOCIAL NETWORK

Social network

Social network

Ego

Alter

similarity  
strength of link

**EXCHANGE**

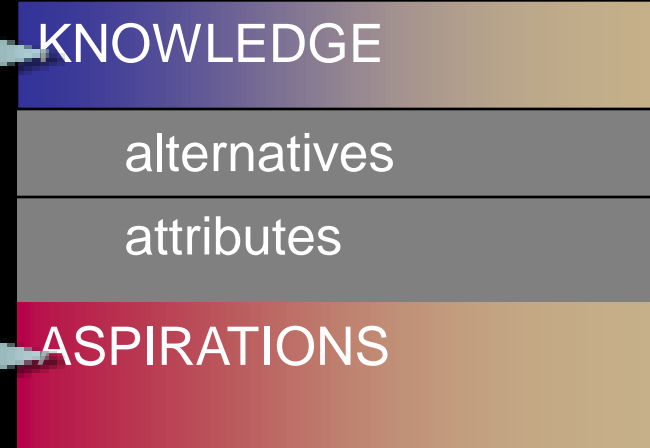
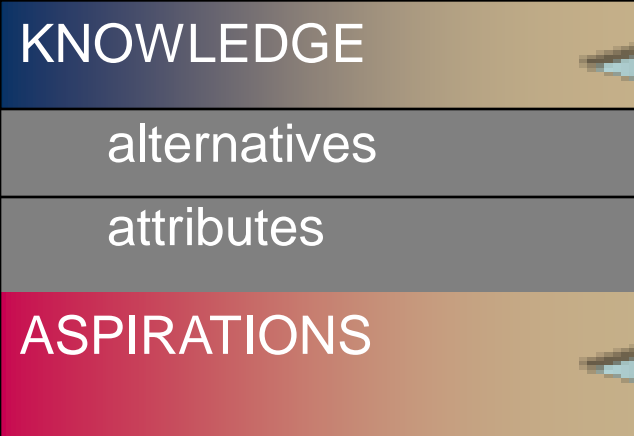
acceptance of  
information

social deviation  
tolerance

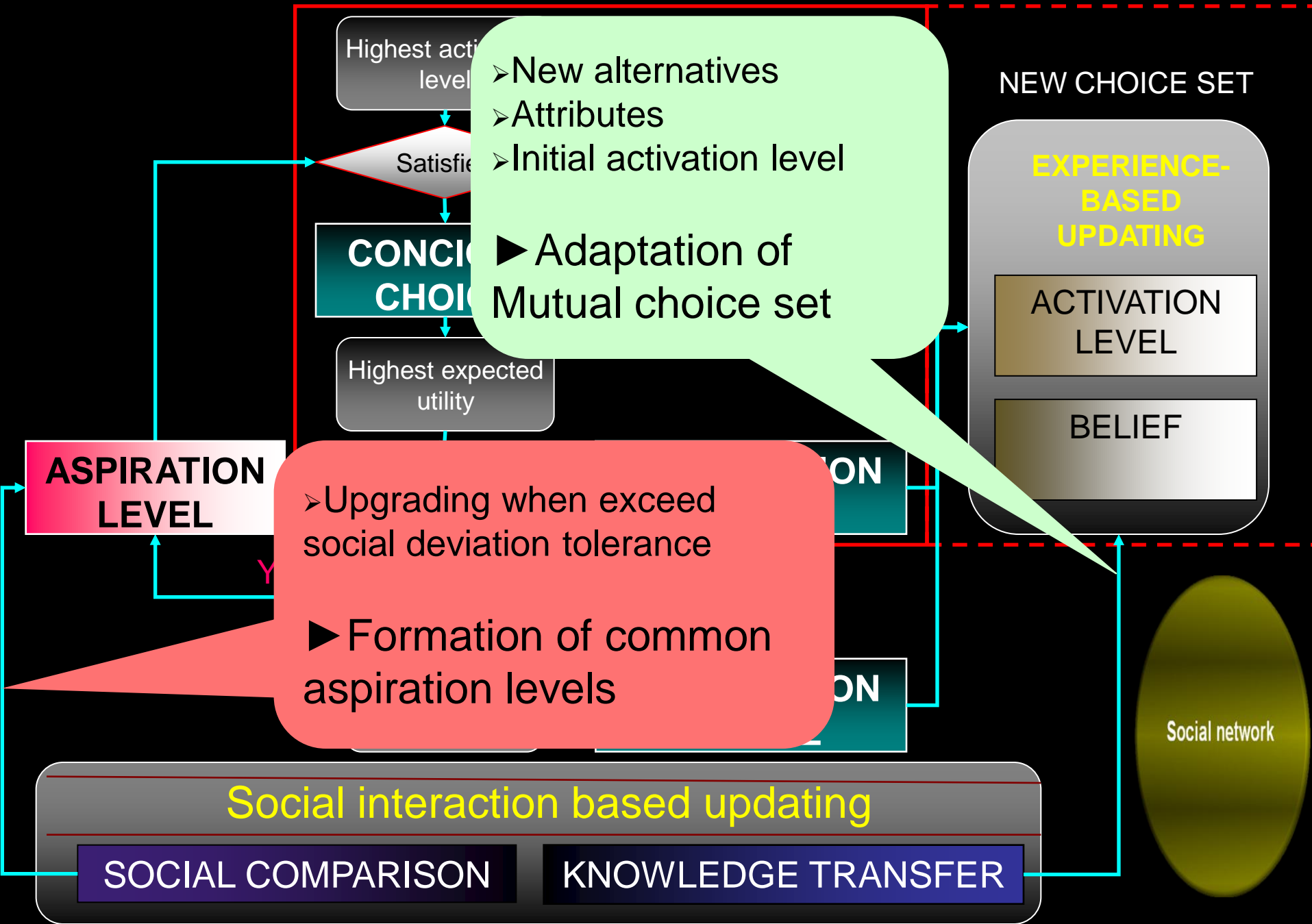
**UPDATING PROCESS**

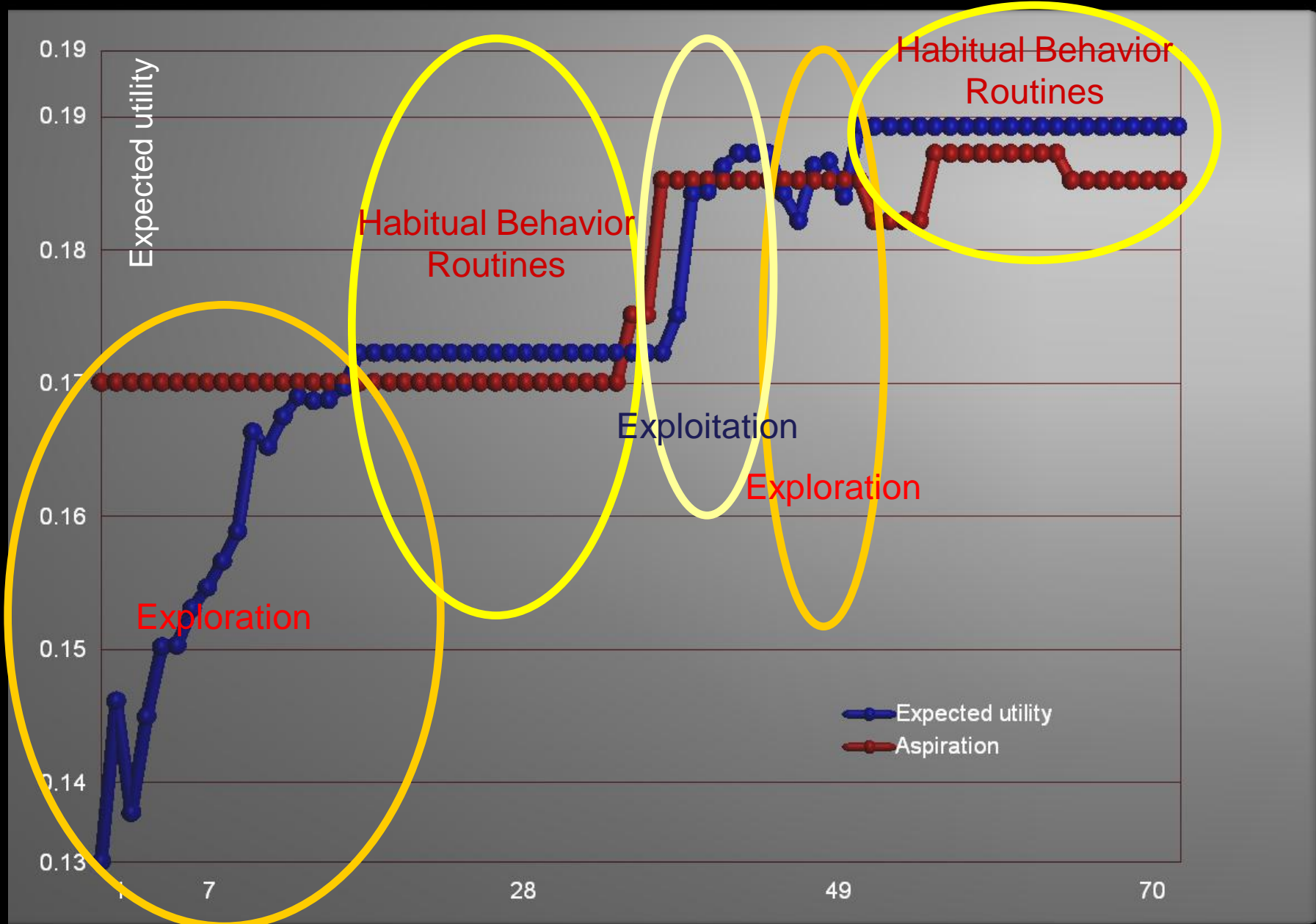
Include in consideration set if

expected utility after exchange + threshold resistance to change >  
current expected utility



# Process Model





Days

# Simulation settings

- 100x100 cells with 100mx100m
- 6 agents, 72 days
- 1 activity a day – a shopping trip
- 8 context condition profiles
  - Origin of the trip (work/home)
  - Day of the week (weekday/weekend)
  - Time of the day (rush hour/non-rush hour)
- 12 shopping locations
  - 6 small, 4 medium, 2 big
  - 6 static attributes (Yes/no)
  - 1 dynamic attribute (crowdedness with 4 levels)

# Simulation settings

- Initial knowledge
  - Alternatives
  - Aspirations
- Cognitive learning
  - Conditional updating
  - Boltzmann model
- Social learning
  - One-way directed contact
  - 8-day interval contact
- Average 100 simulation run

# Simulation settings

- Cognitive learning parameters
  - Minimum activation level
  - Maximum exploration effort
  - Aspiration dissatisfaction tolerance
- Social learning parameters
  - Social deviation tolerance
  - Information acceptance
- Social contact scenarios

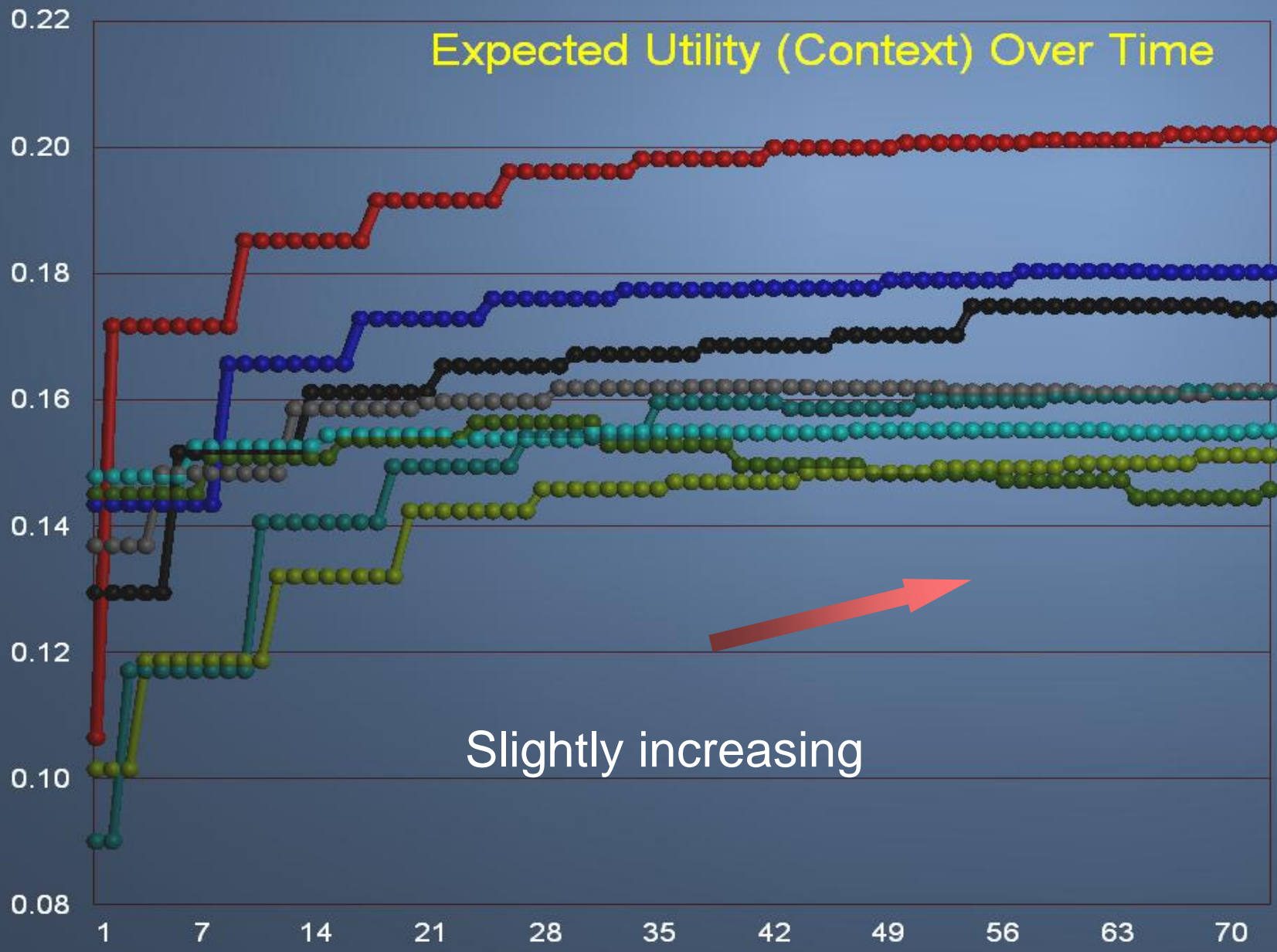
Properties

Dynamics



# Expected Utility (Context) Over Time

Expected utility

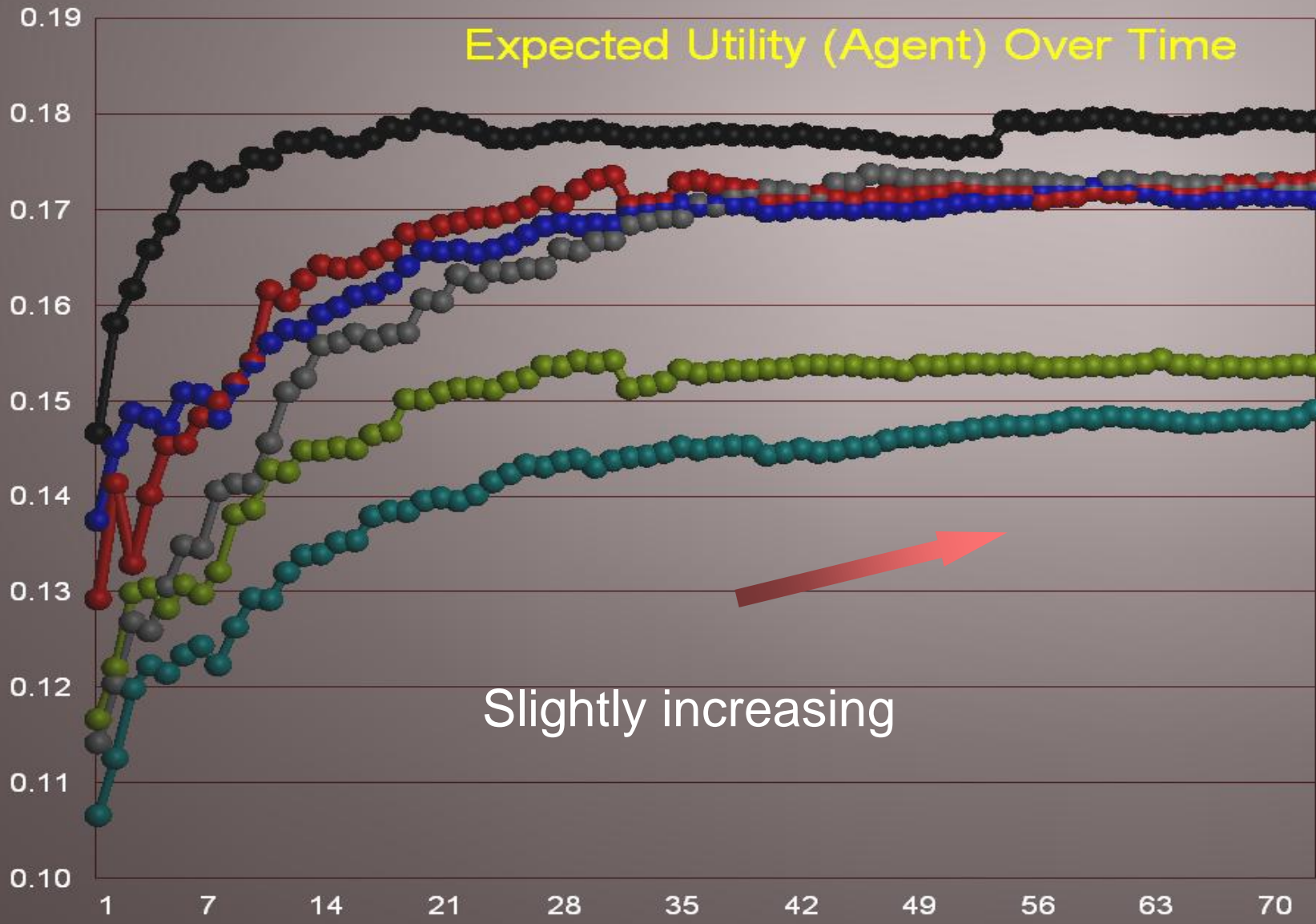


Slightly increasing

Days

# Expected Utility (Agent) Over Time

Expected utility



Slightly increasing

Days

# Choice Set Size (Context) Over Time

First decrease a bit,  
then slightly increase

Expected utility



Days

# Choice Set Size (Agent) Over Time

Expected utility

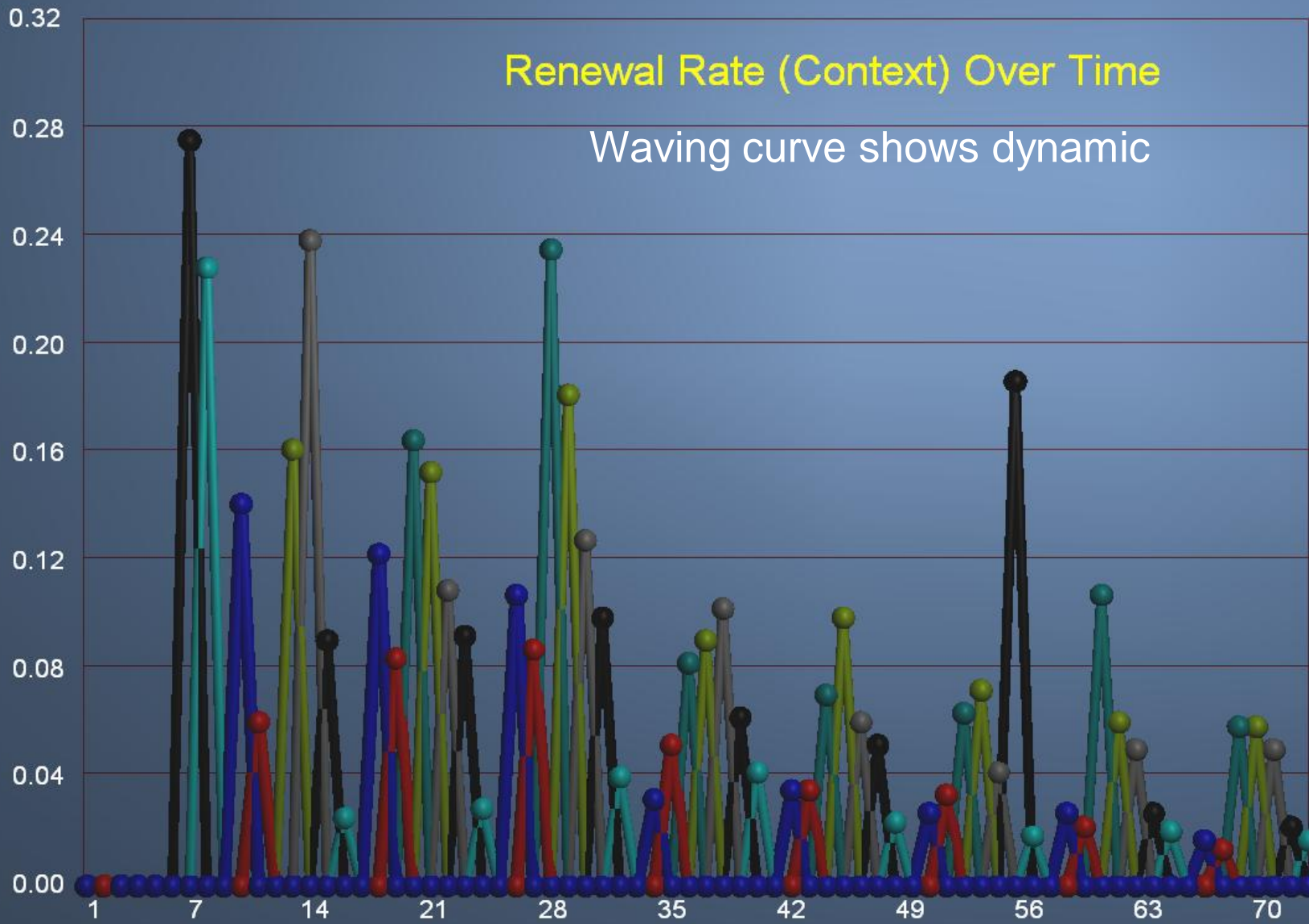
First decrease a bit,  
then slightly increase



Days

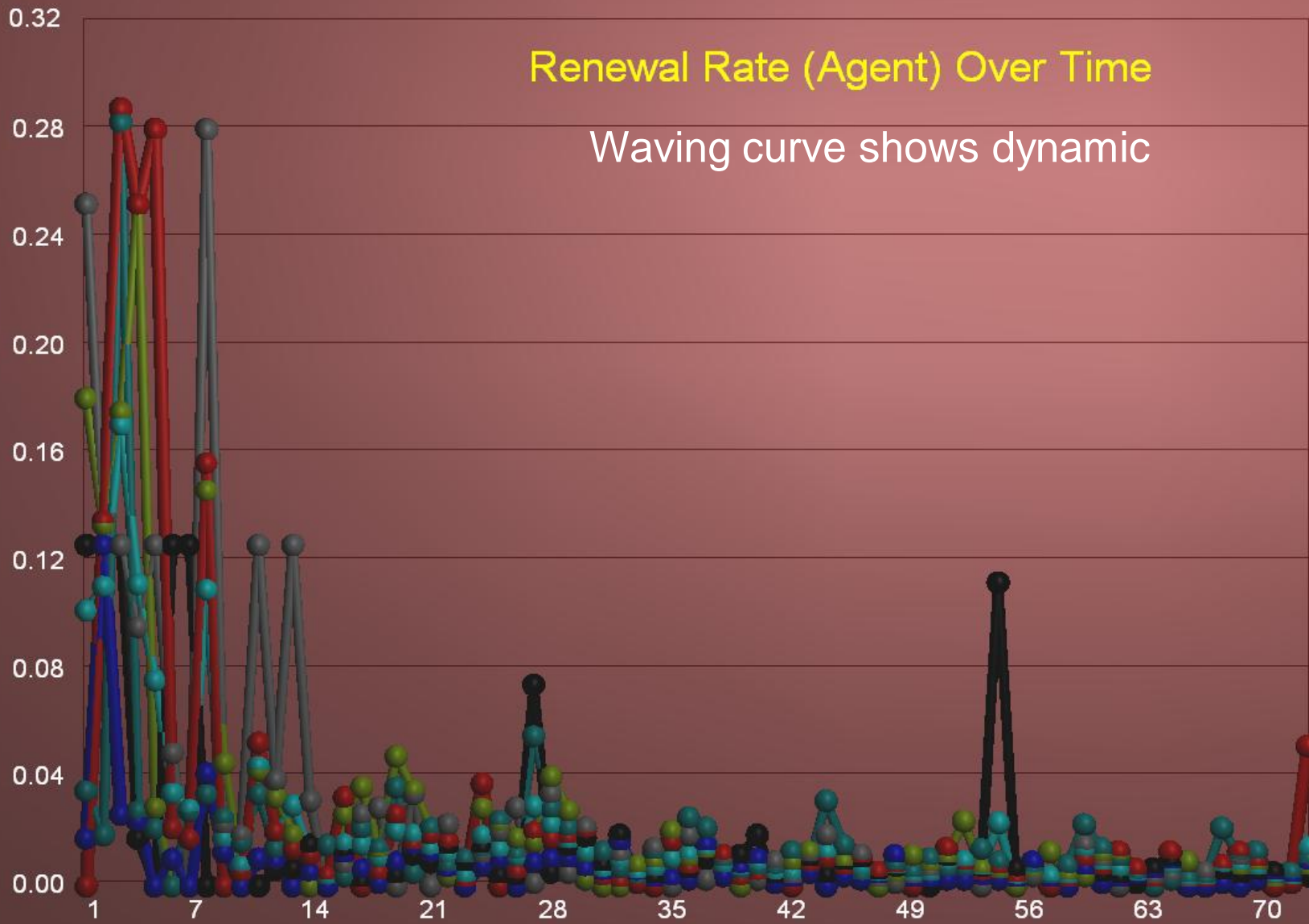


Renewal rate



Days

Renewal rate



### Renewal Rate (Agent) Over Time

Waving curve shows dynamic

Days

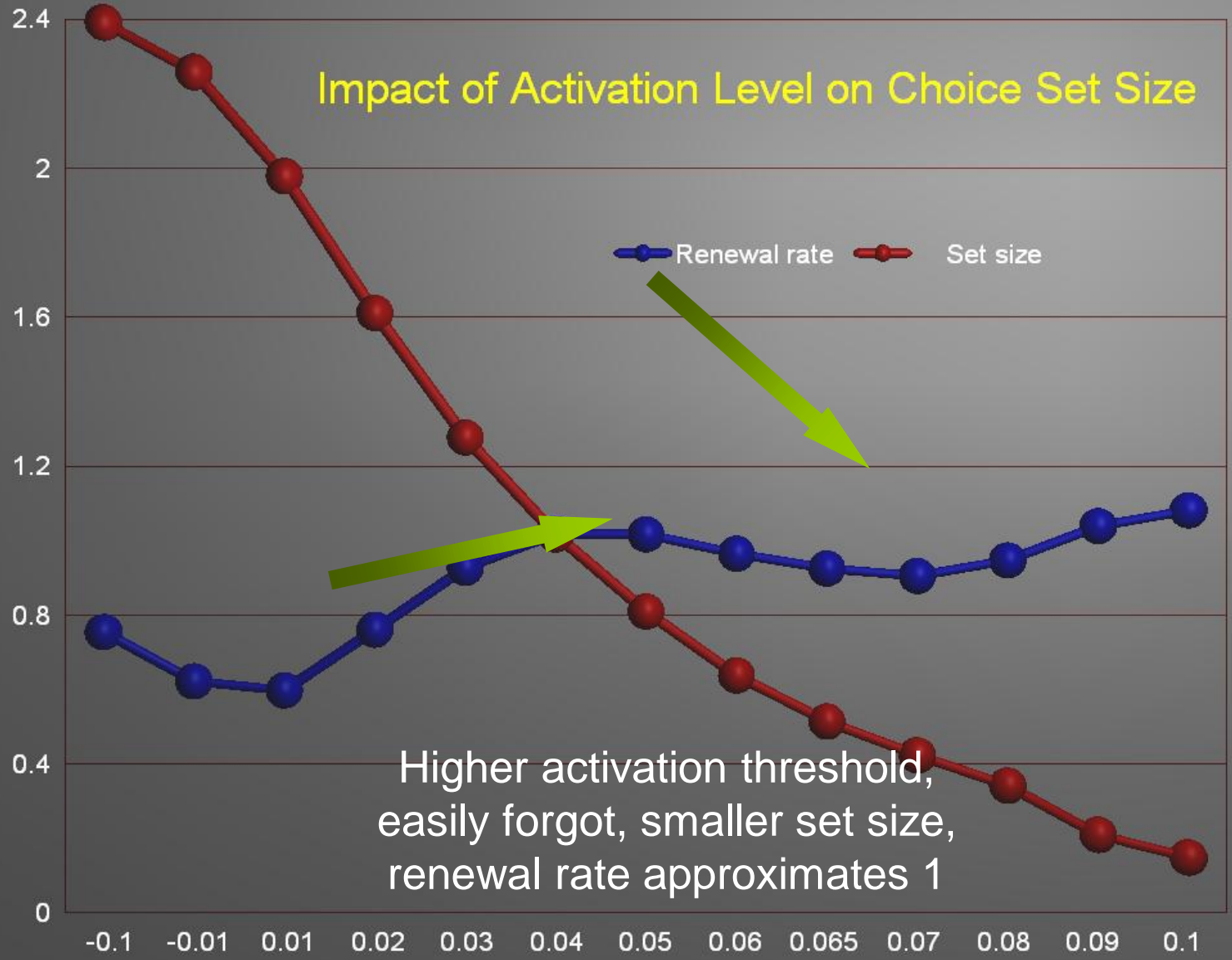
# Properties

Impact of activation level



Choice set size

### Impact of Activation Level on Choice Set Size

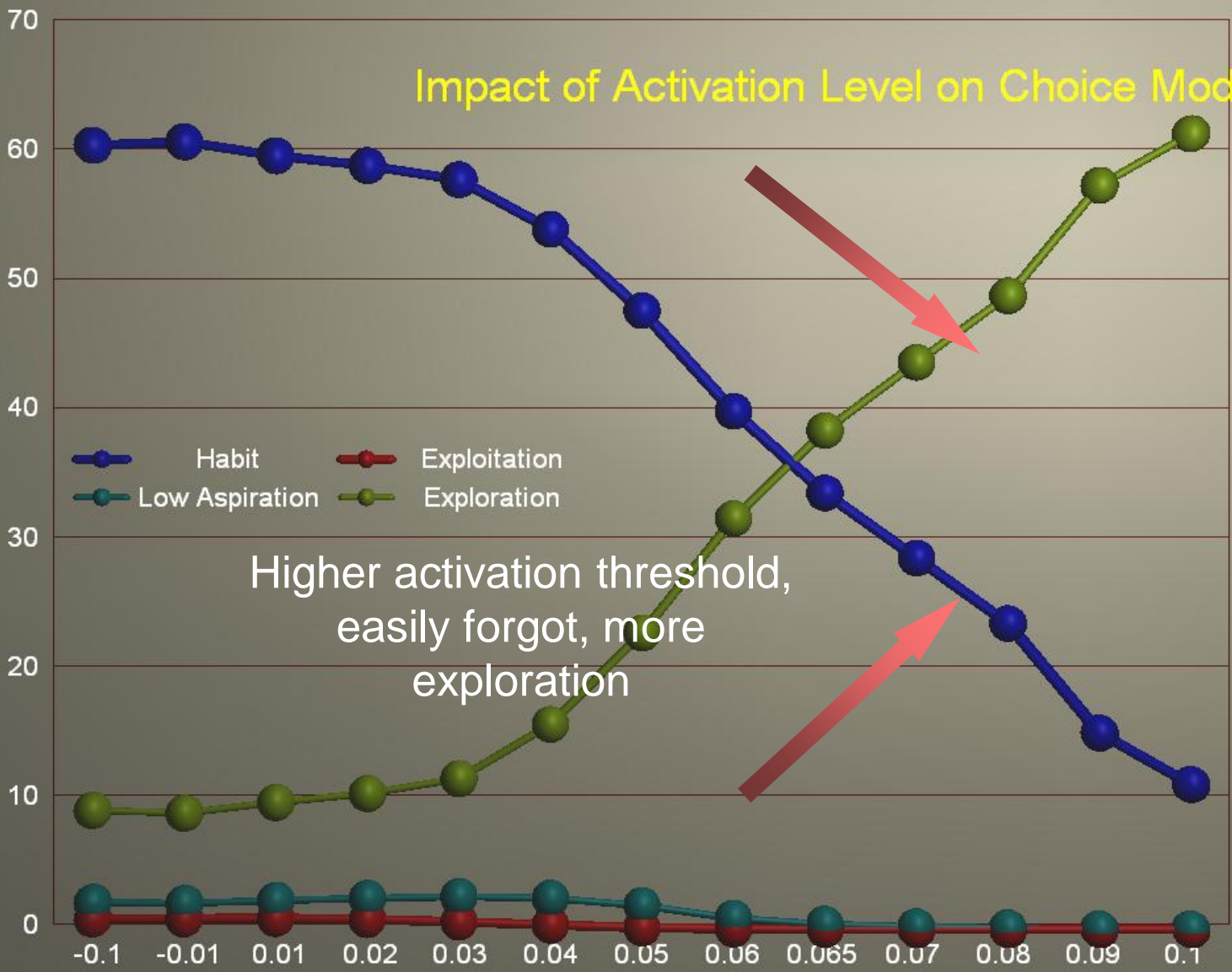


Higher activation threshold,  
easily forgot, smaller set size,  
renewal rate approximates 1

Activation level threshold

Number of choices

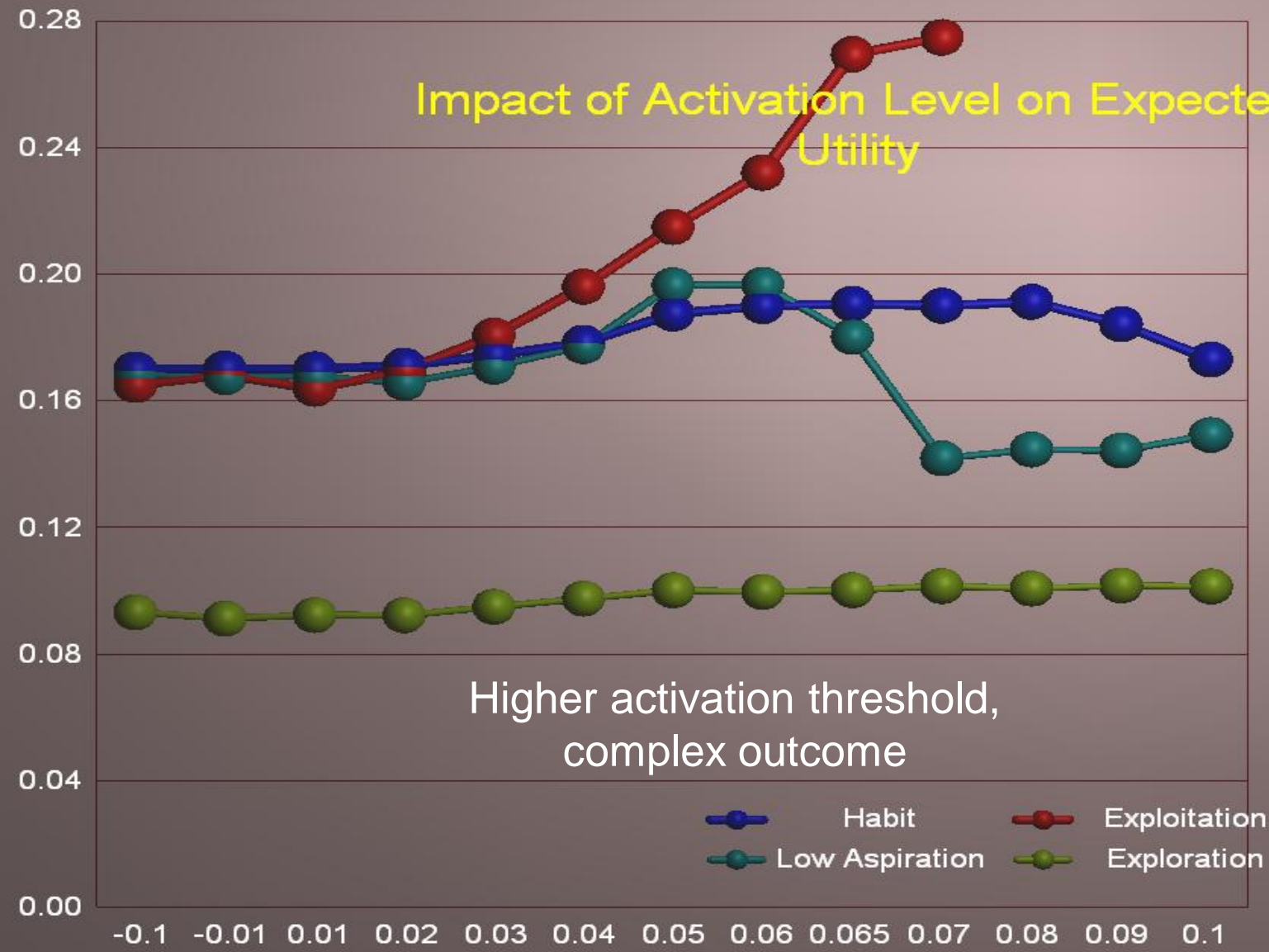
### Impact of Activation Level on Choice Mode



Higher activation threshold,  
easily forgot, more  
exploration

Activation level threshold

Expected utility



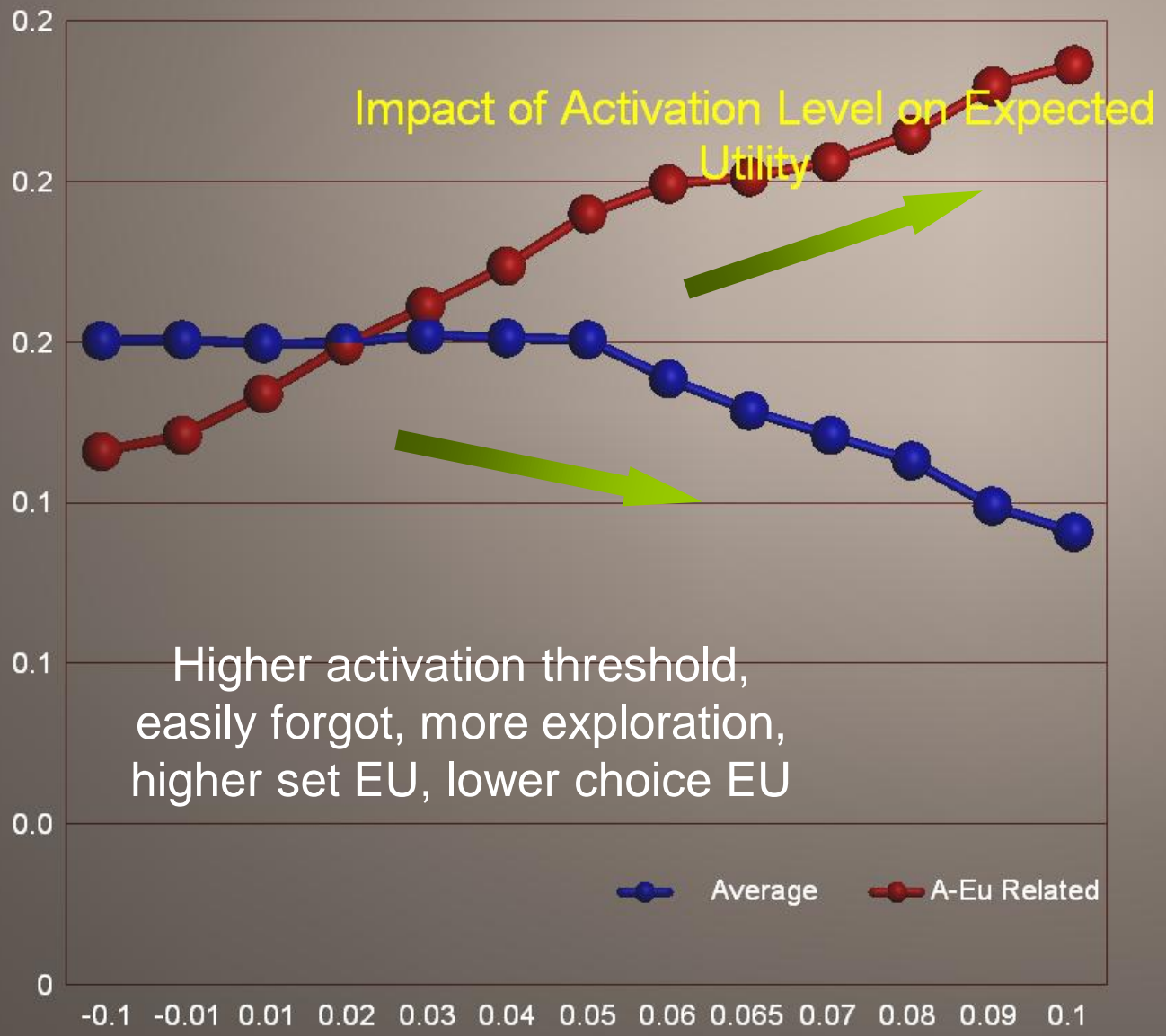
Impact of Activation Level on Expected Utility

Higher activation threshold, complex outcome

- Habit
- Exploitation
- Low Aspiration
- Exploration

Activation level threshold

Expected utility



Impact of Activation Level on Expected Utility

Higher activation threshold, easily forgot, more exploration, higher set EU, lower choice EU

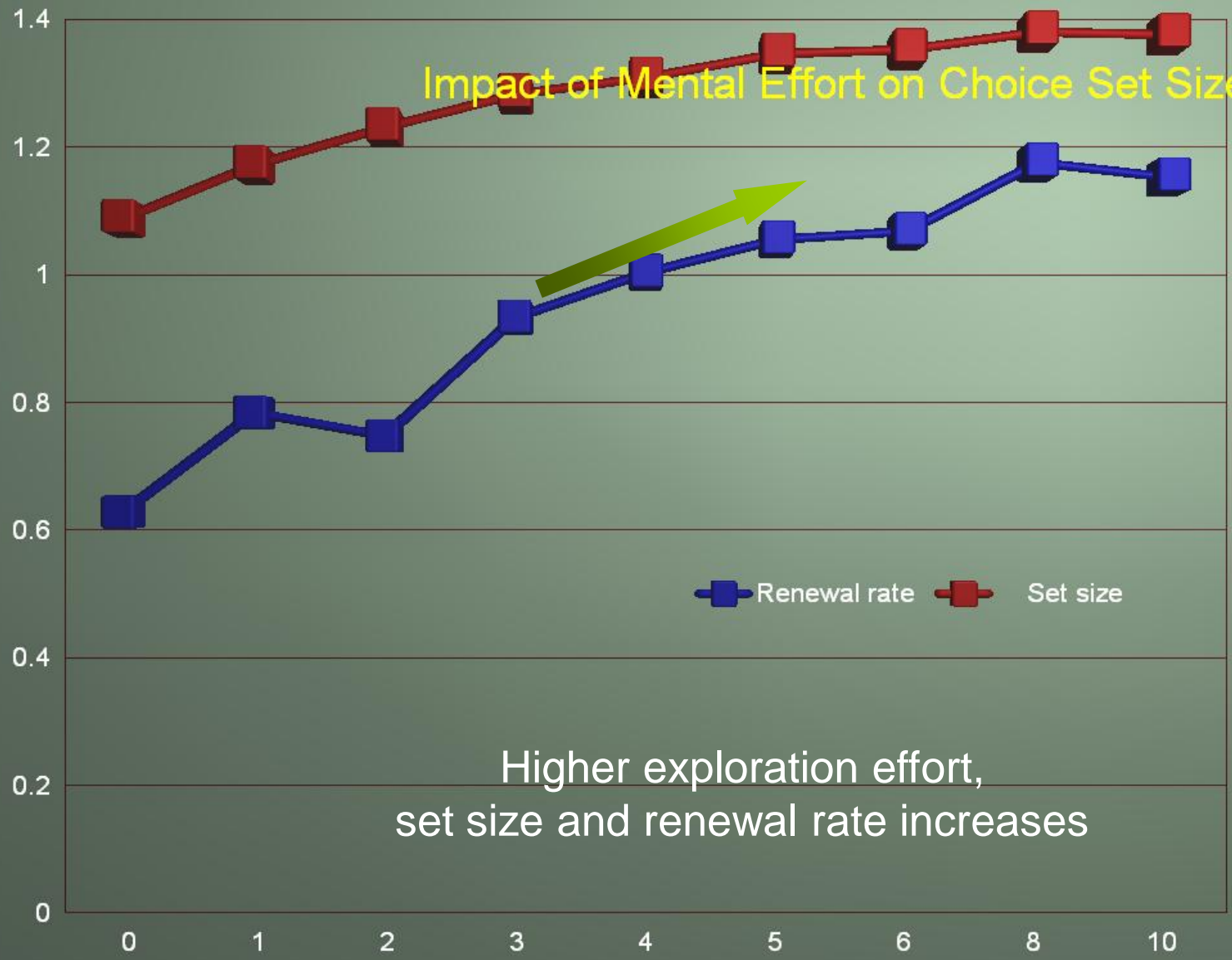
Average A-Eu Related

Activation level threshold

# Properties

Impact of mental effort

Number of alternatives



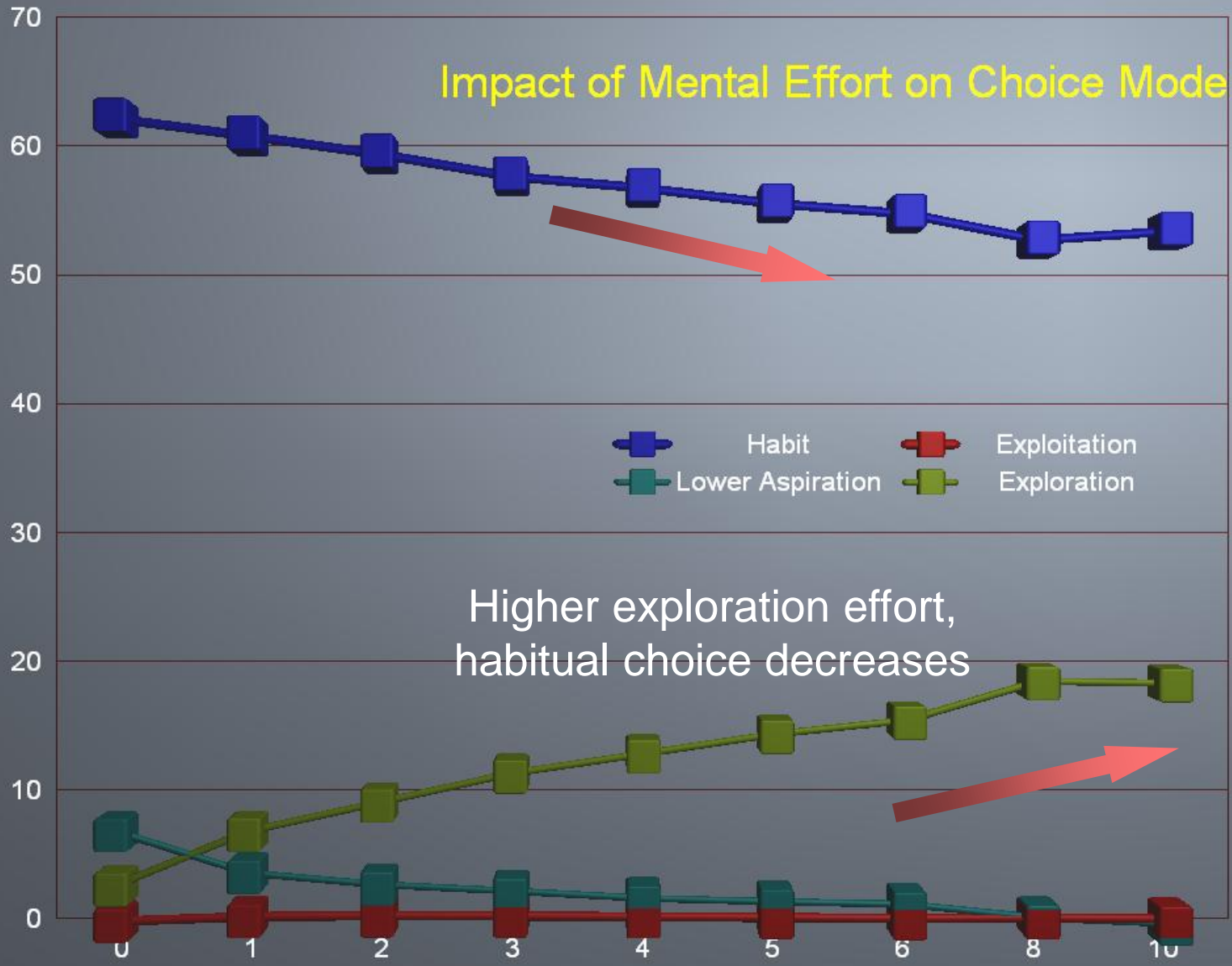
Impact of Mental Effort on Choice Set Size

Renewal rate Set size

Higher exploration effort,  
set size and renewal rate increases

Maximum exploration effort

Number of alternatives

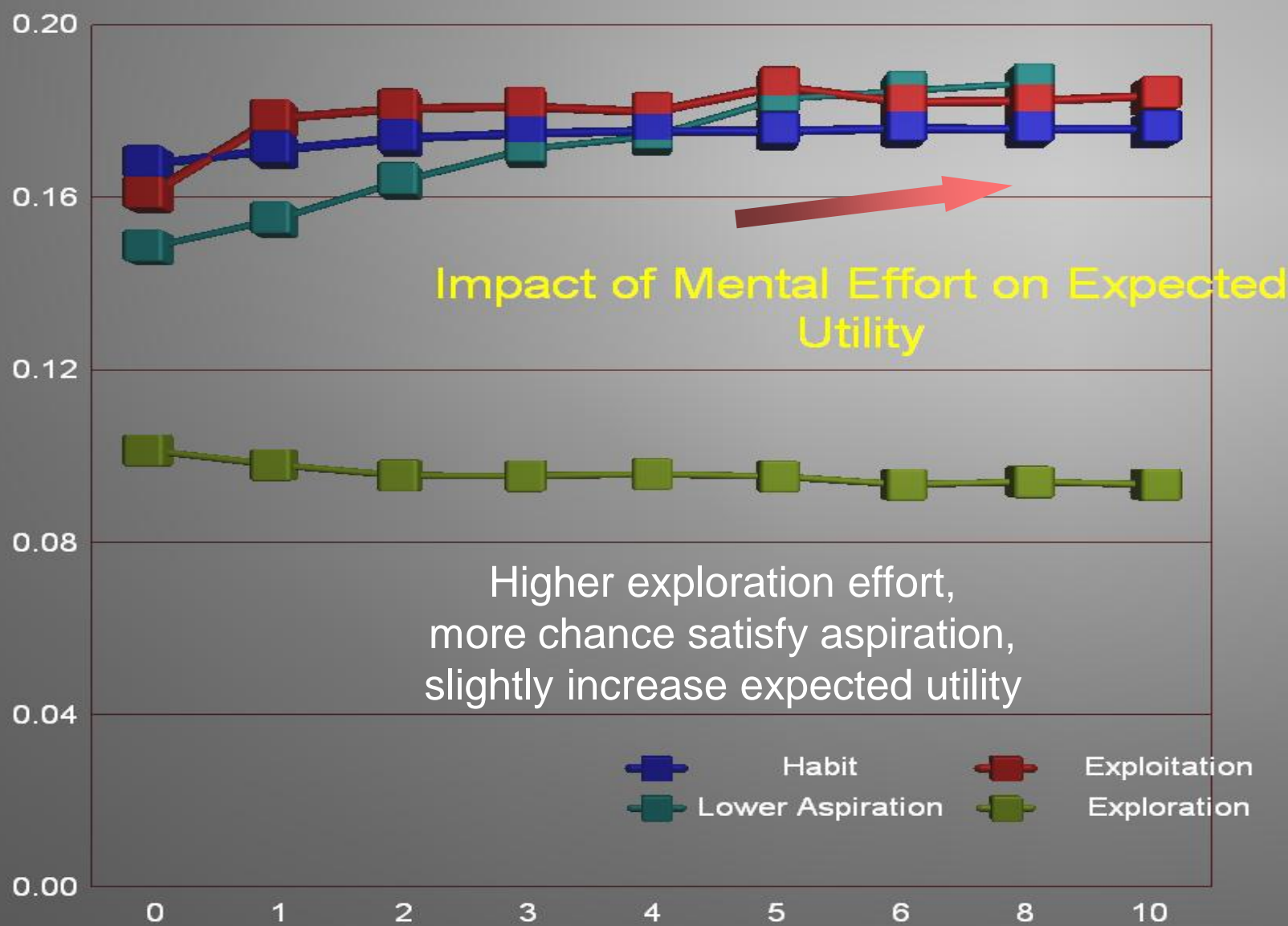


Higher exploration effort,  
habitual choice decreases

Maximum exploration effort



Expected utility



Impact of Mental Effort on Expected Utility

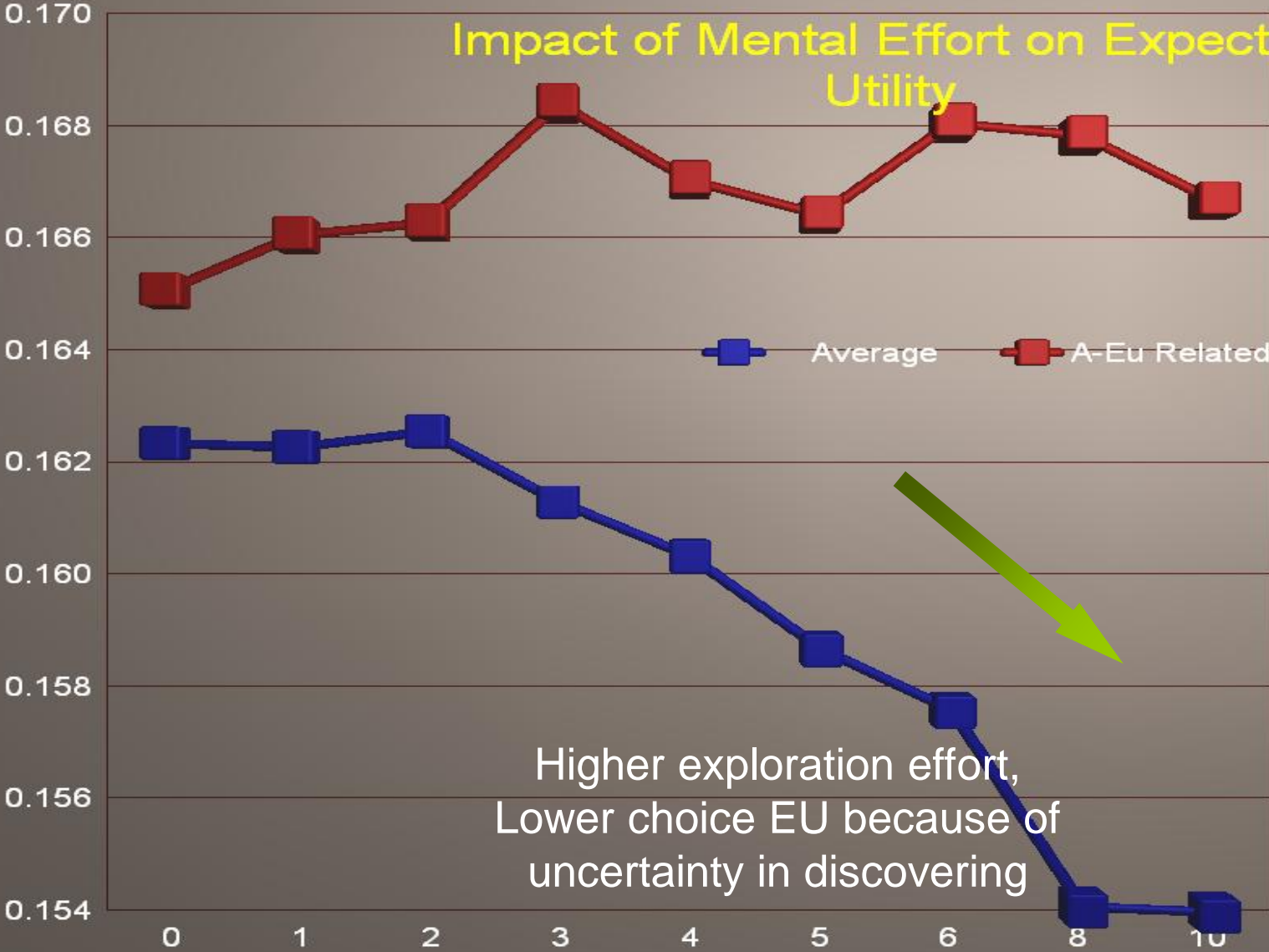
Higher exploration effort, more chance satisfy aspiration, slightly increase expected utility

Habit      Exploitation  
Lower Aspiration      Exploration

Maximum exploration effort

Expected utility

# Impact of Mental Effort on Expected Utility



Average

A-Eu Related

Higher exploration effort,  
Lower choice EU because of  
uncertainty in discovering

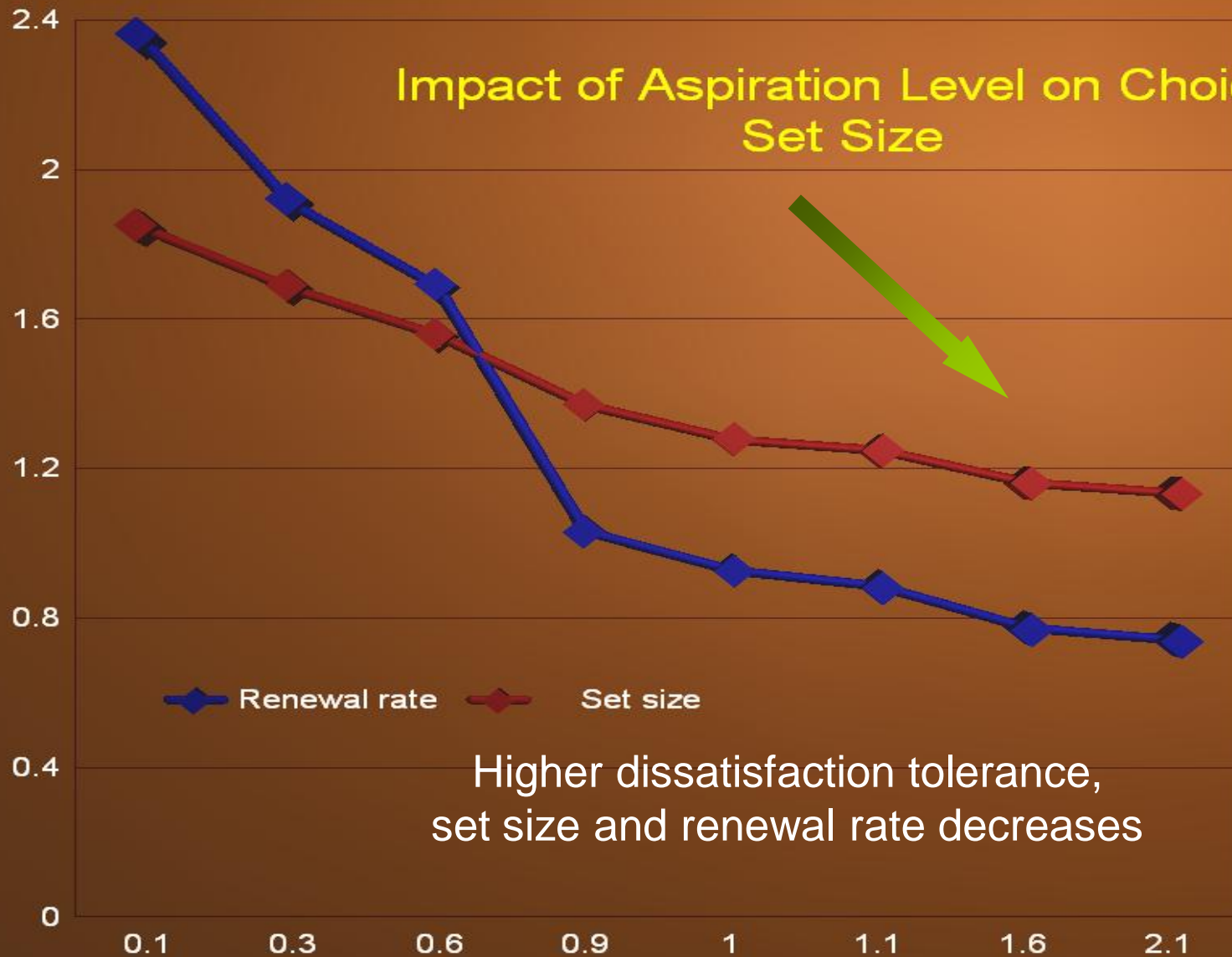
Maximum exploration effort

# Properties

Impact of aspiration level

Number of alternatives

## Impact of Aspiration Level on Choice Set Size

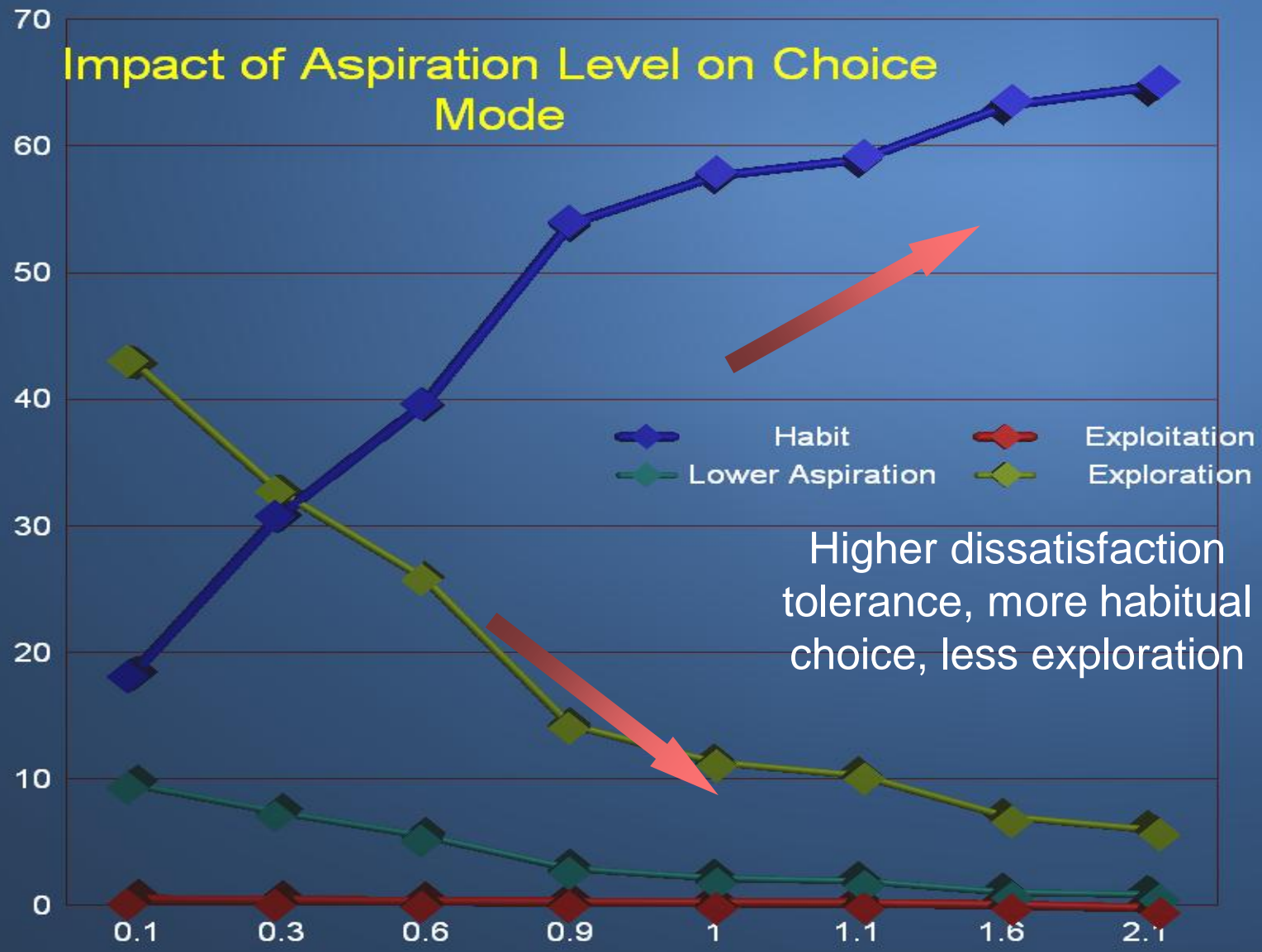


Higher dissatisfaction tolerance,  
set size and renewal rate decreases

Aspiration dissatisfaction tolerance

# Impact of Aspiration Level on Choice Mode

Number of alternatives



Habit      Exploitation  
Lower Aspiration      Exploration

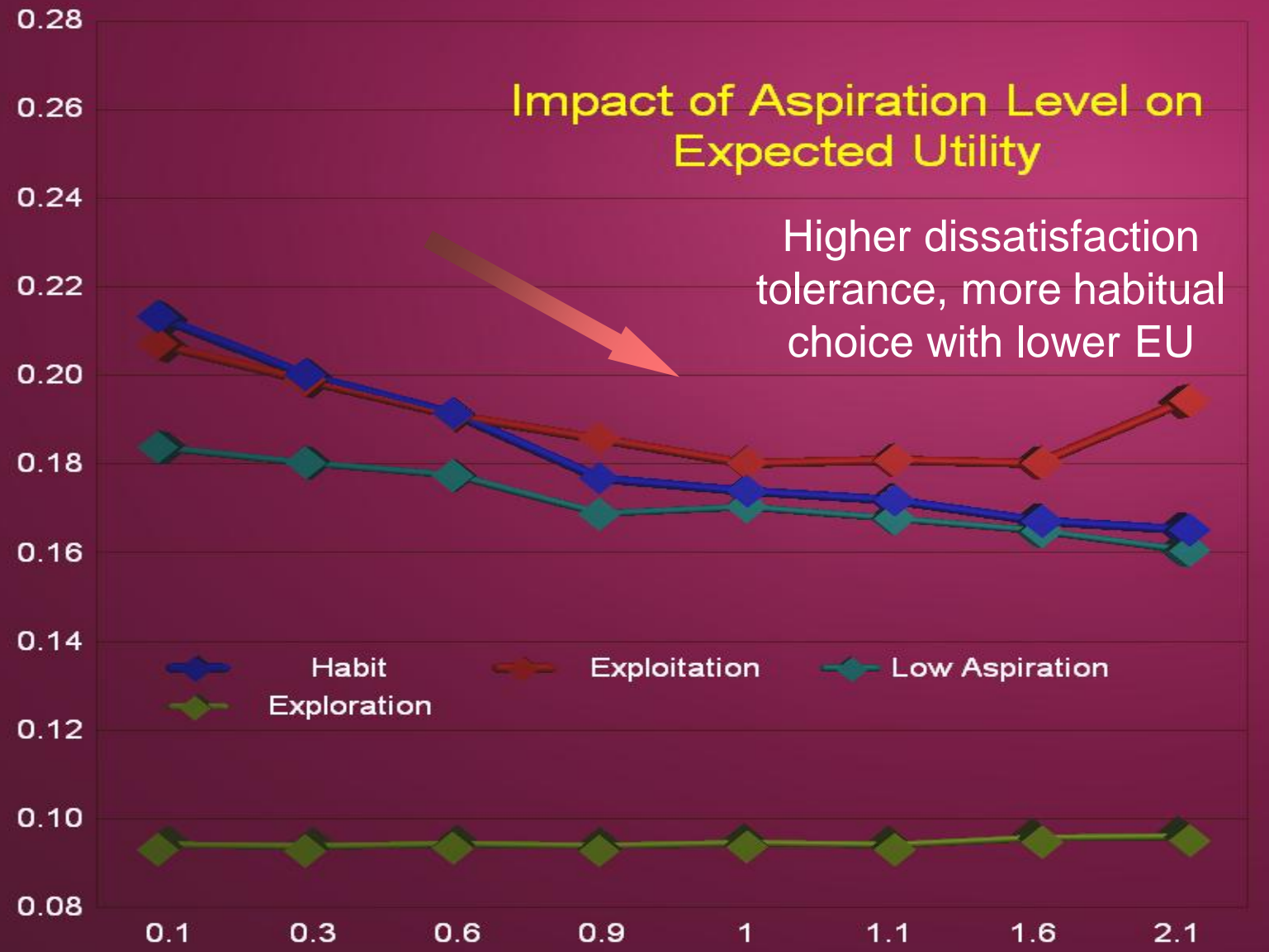
Higher dissatisfaction tolerance, more habitual choice, less exploration

Aspiration dissatisfaction tolerance

Expected utility

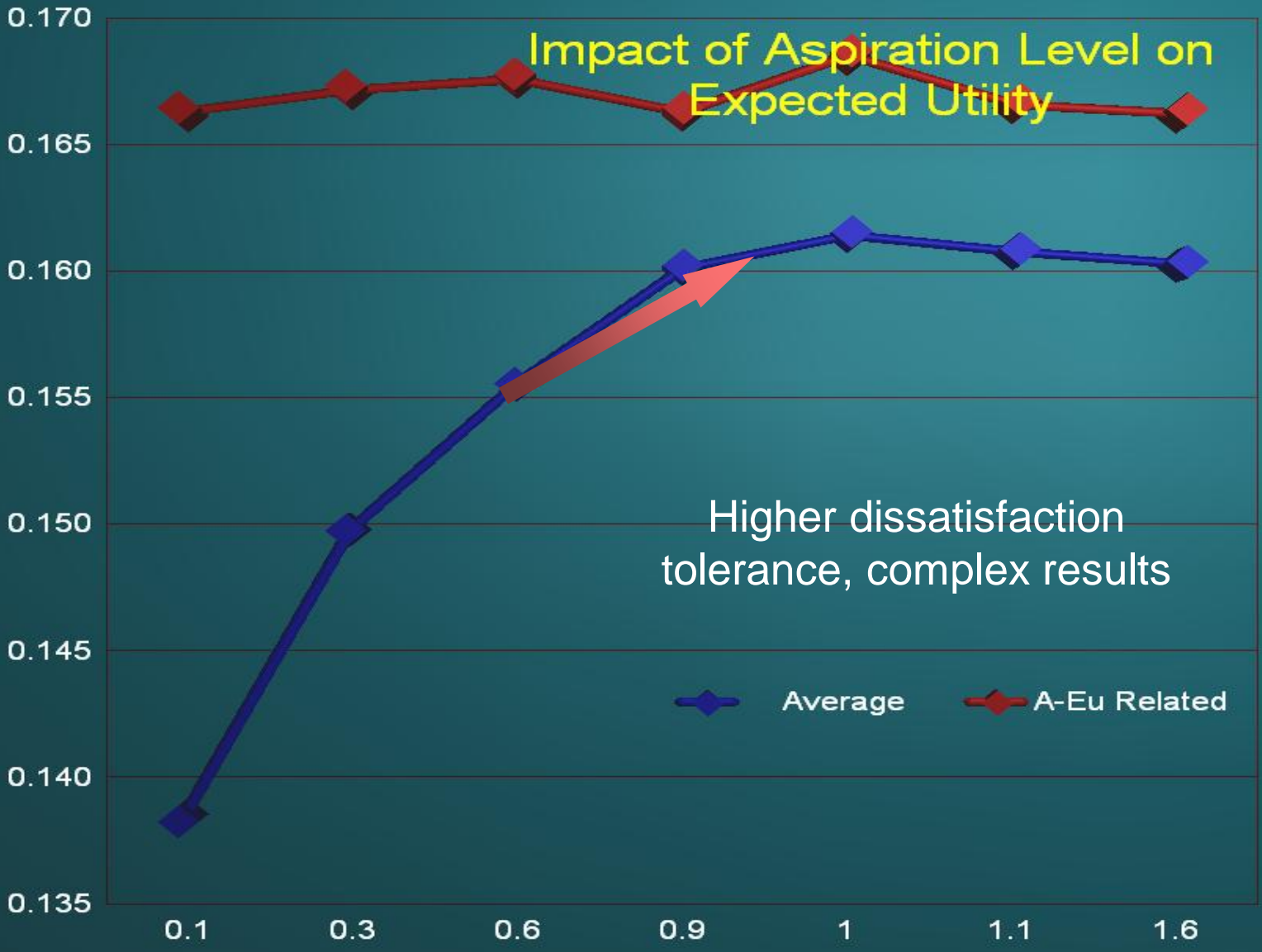
### Impact of Aspiration Level on Expected Utility

Higher dissatisfaction tolerance, more habitual choice with lower EU



Aspiration dissatisfaction tolerance

Expected utility



Aspiration dissatisfaction tolerance



# Properties

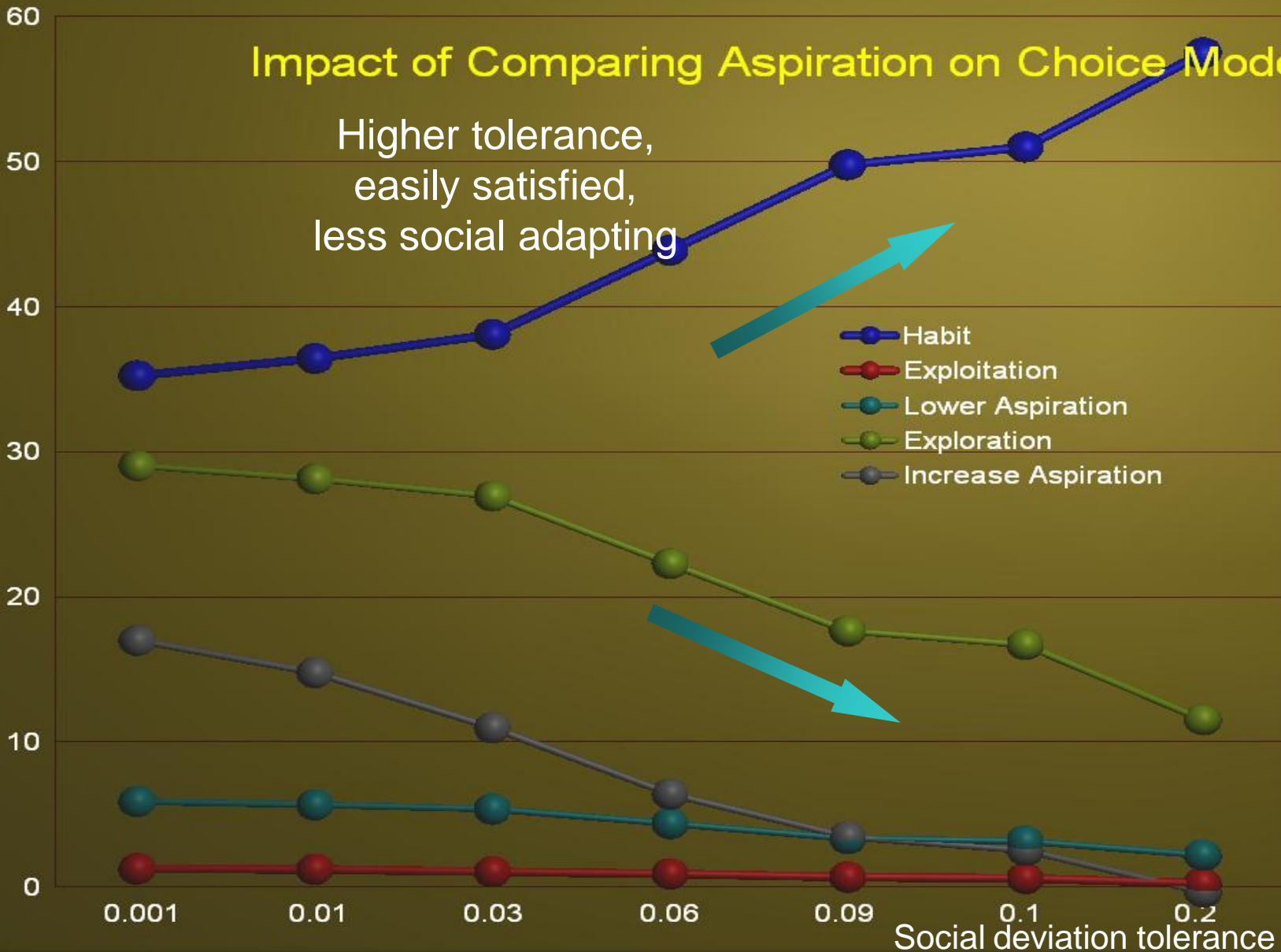
Impact of social deviation  
tolerance

# Impact of Comparing Aspiration on Choice Mode

Higher tolerance,  
easily satisfied,  
less social adapting

Number of choices

- Habit
- Exploitation
- Lower Aspiration
- Exploration
- Increase Aspiration



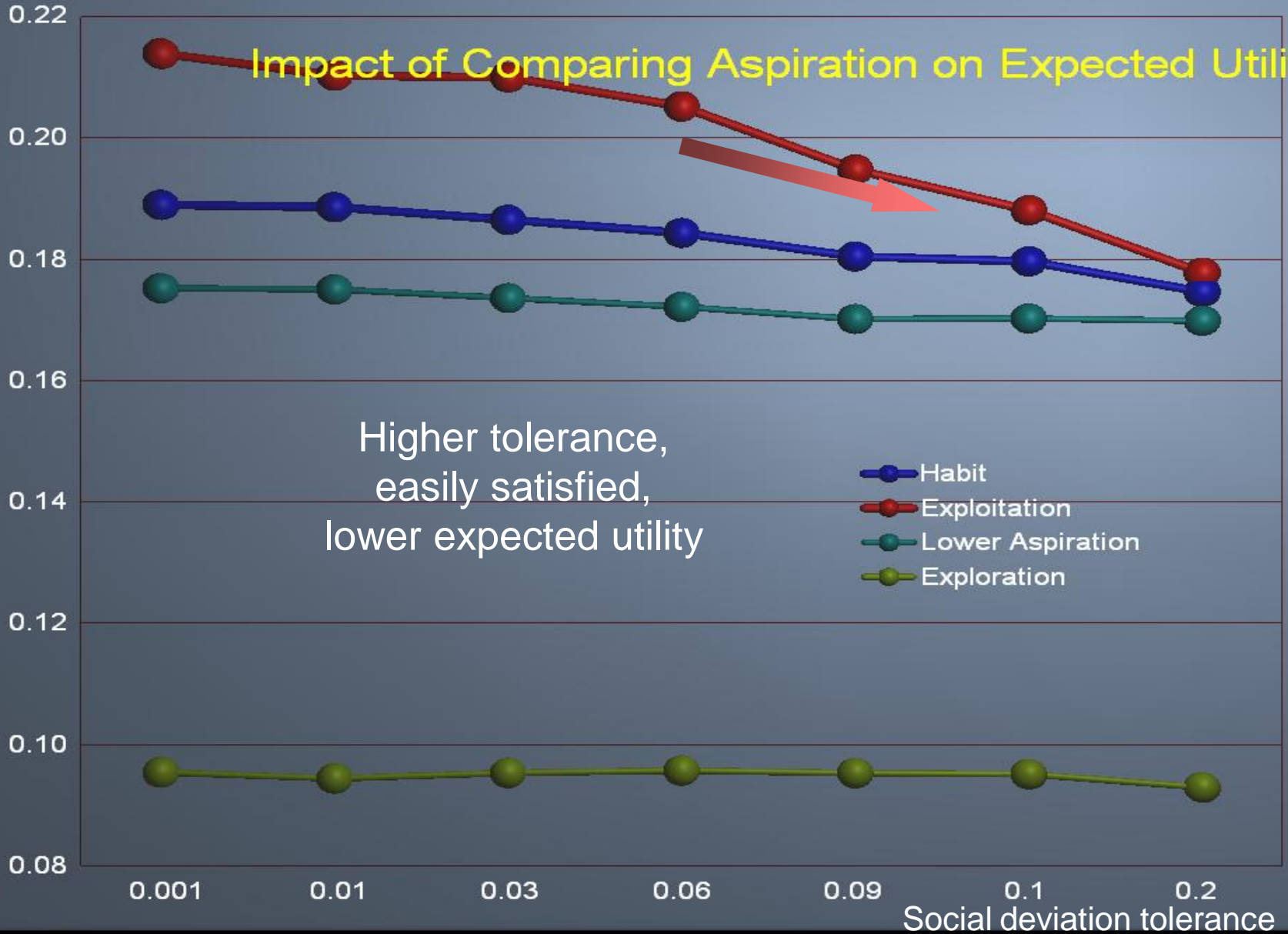
Social deviation tolerance

# Impact of Comparing Aspiration on Expected Utility

Expected utility

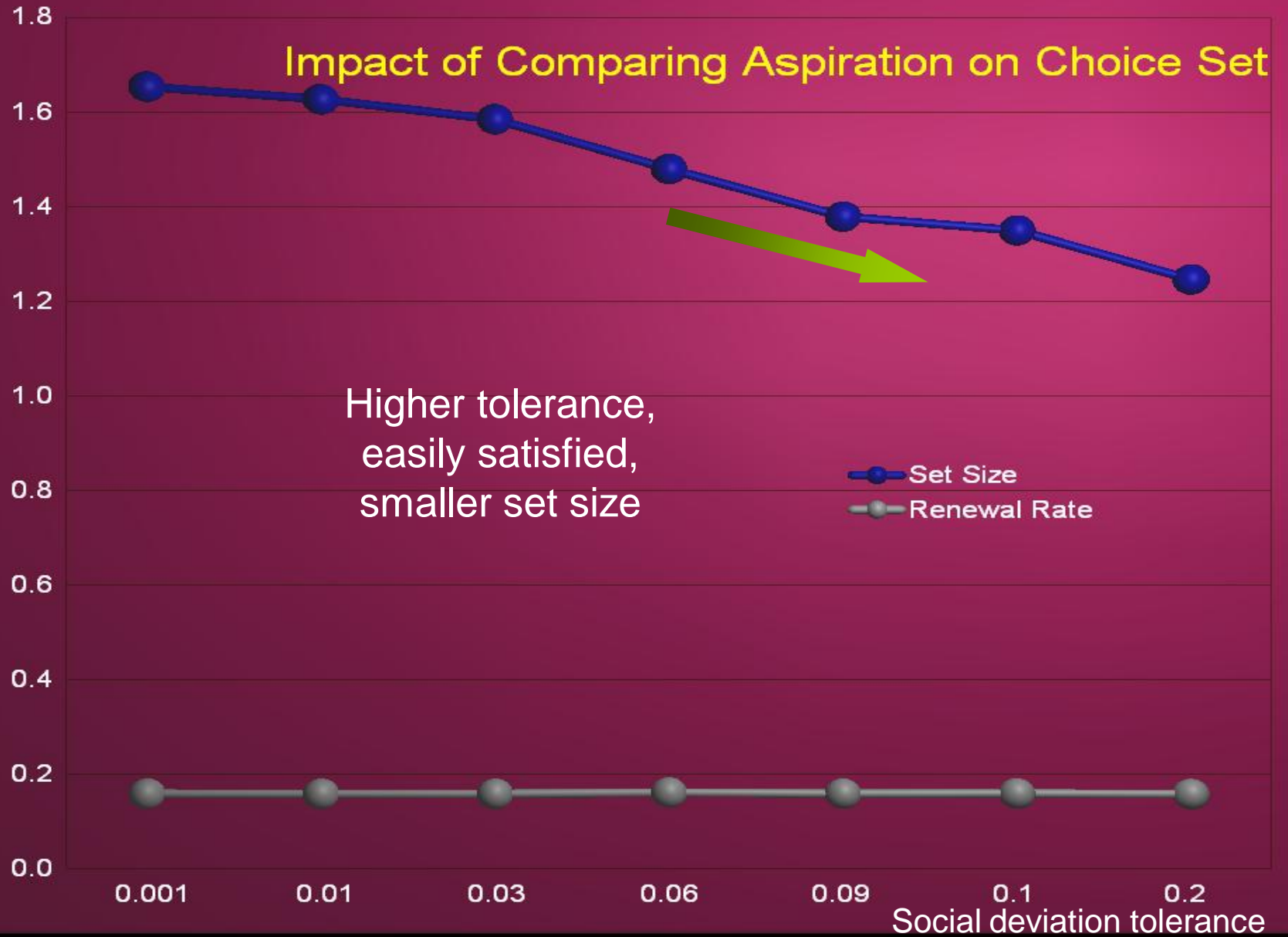
Higher tolerance,  
easily satisfied,  
lower expected utility

- Habit
- Exploitation
- Lower Aspiration
- Exploration



# Impact of Comparing Aspiration on Choice Set

Number of alternatives

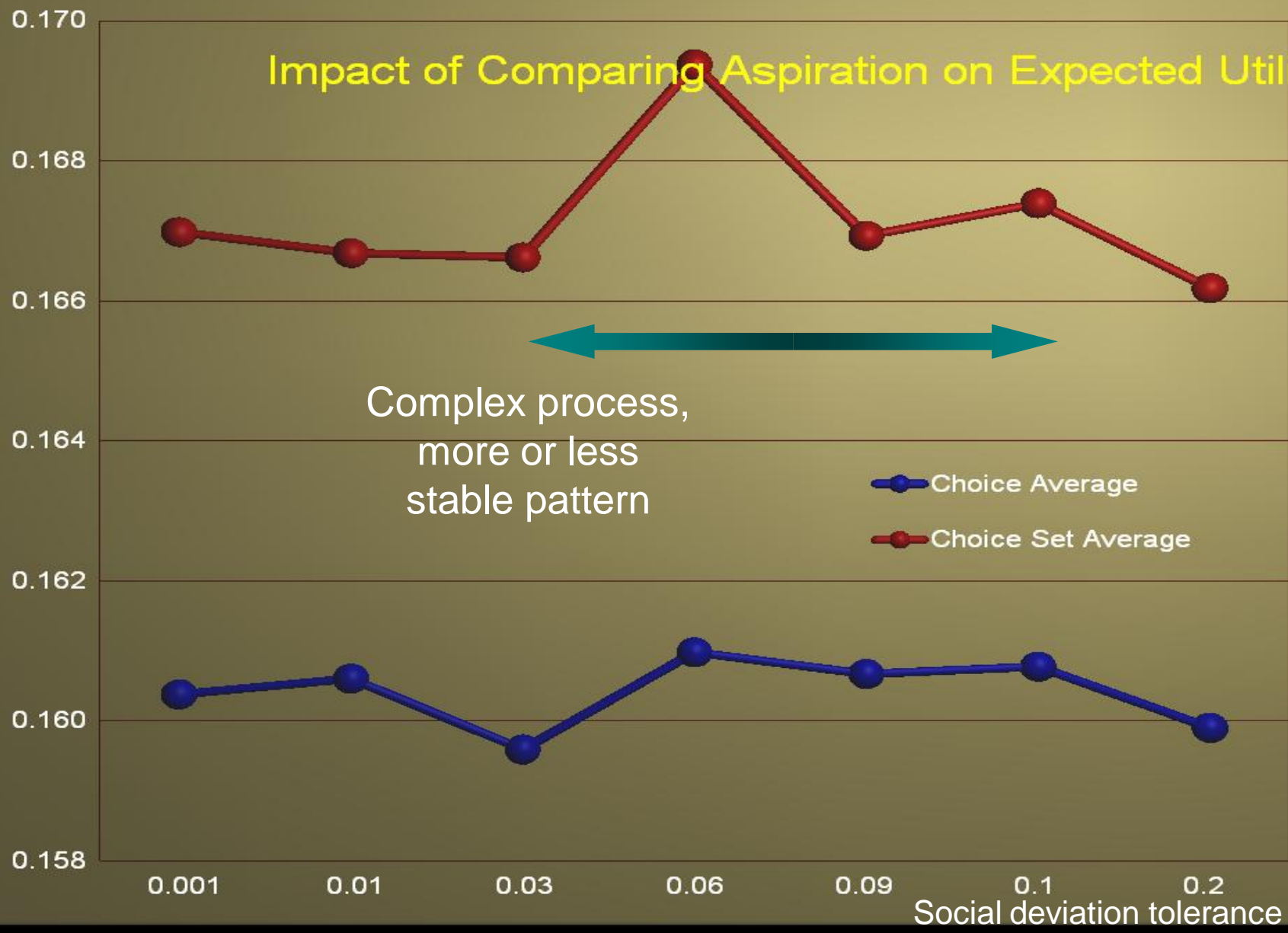


Higher tolerance,  
easily satisfied,  
smaller set size

Set Size  
Renewal Rate

# Impact of Comparing Aspiration on Expected Utility

Expected utility



Complex process,  
more or less  
stable pattern

Choice Average  
Choice Set Average

Social deviation tolerance

# Properties

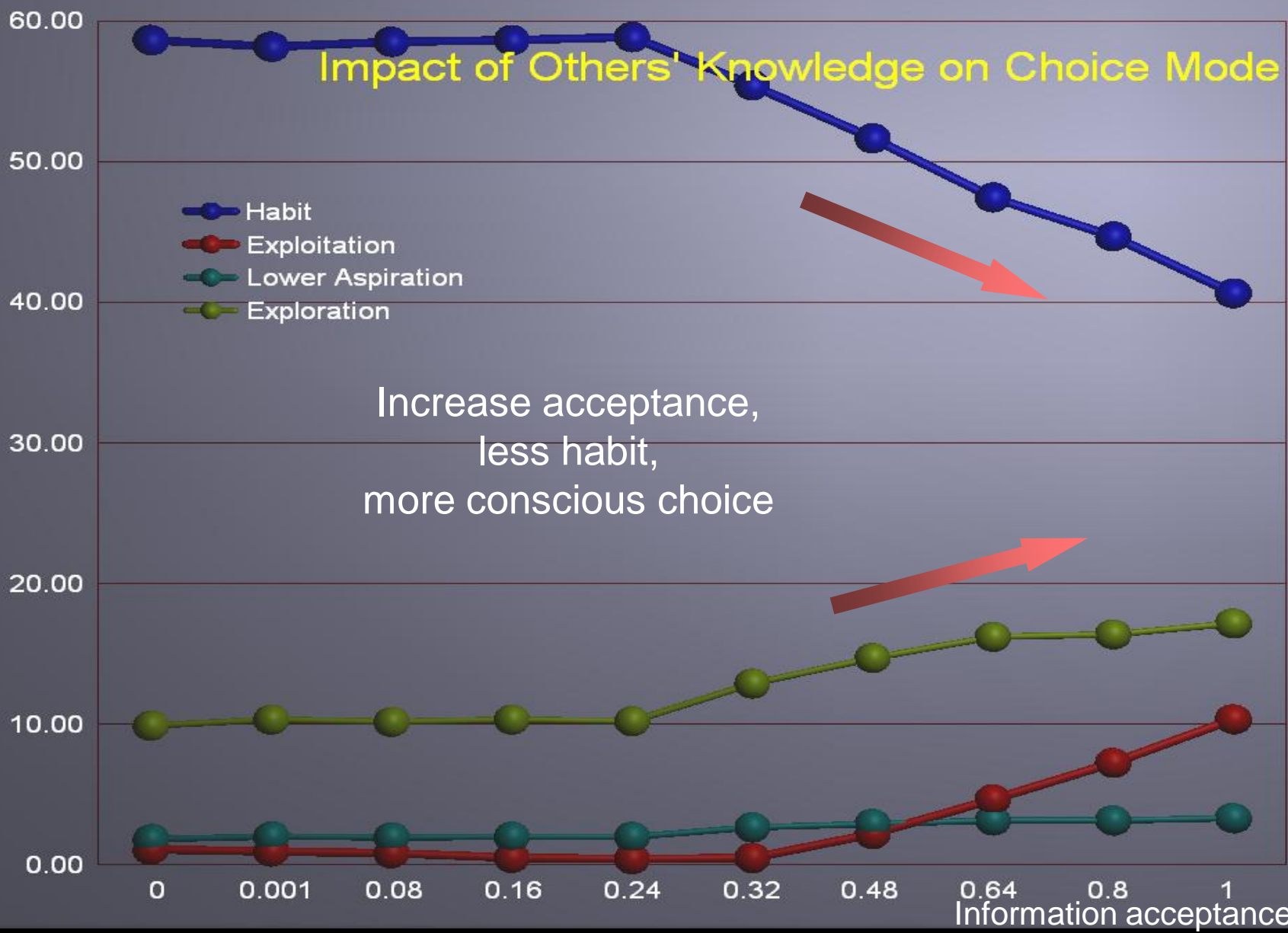
Impact of acceptance of  
others' information

Number of choices

### Impact of Others' Knowledge on Choice Mode

- Habit
- Exploitation
- Lower Aspiration
- Exploration

Increase acceptance,  
less habit,  
more conscious choice

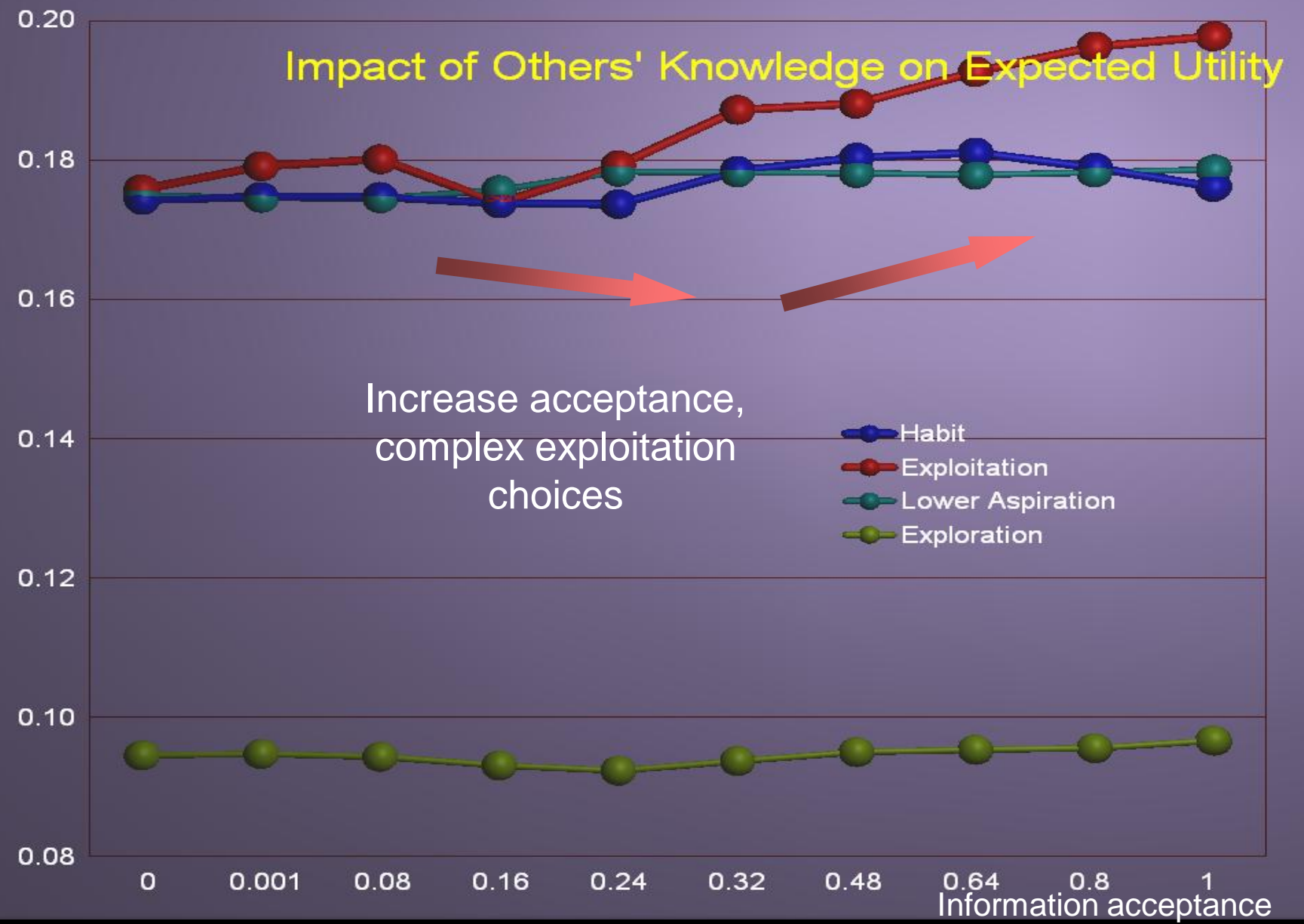


Information acceptance



# Impact of Others' Knowledge on Expected Utility

Expected utility



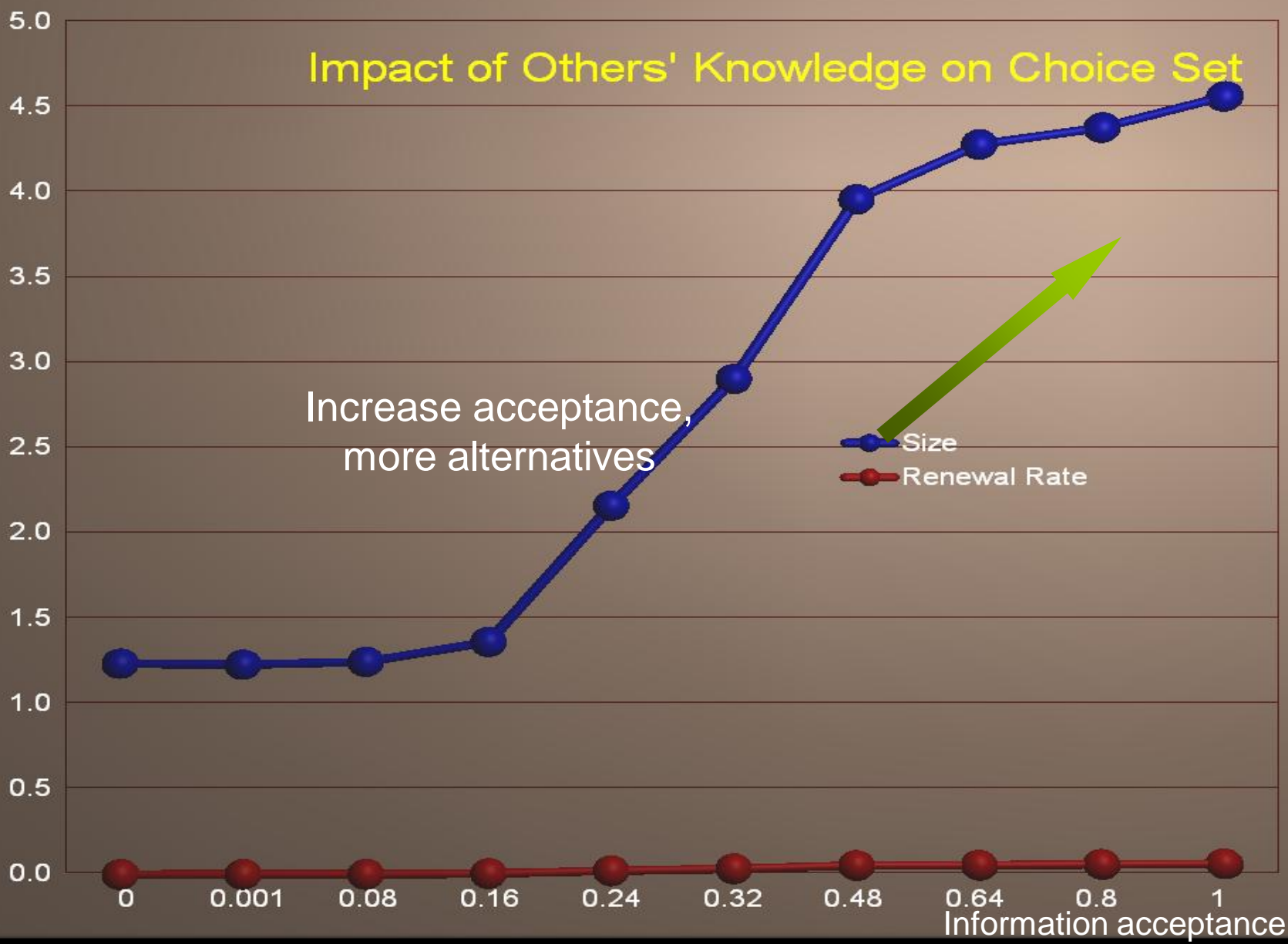
Increase acceptance,  
complex exploitation  
choices

- Habit
- Exploitation
- Lower Aspiration
- Exploration

Information acceptance

# Impact of Others' Knowledge on Choice Set

Number of alternatives



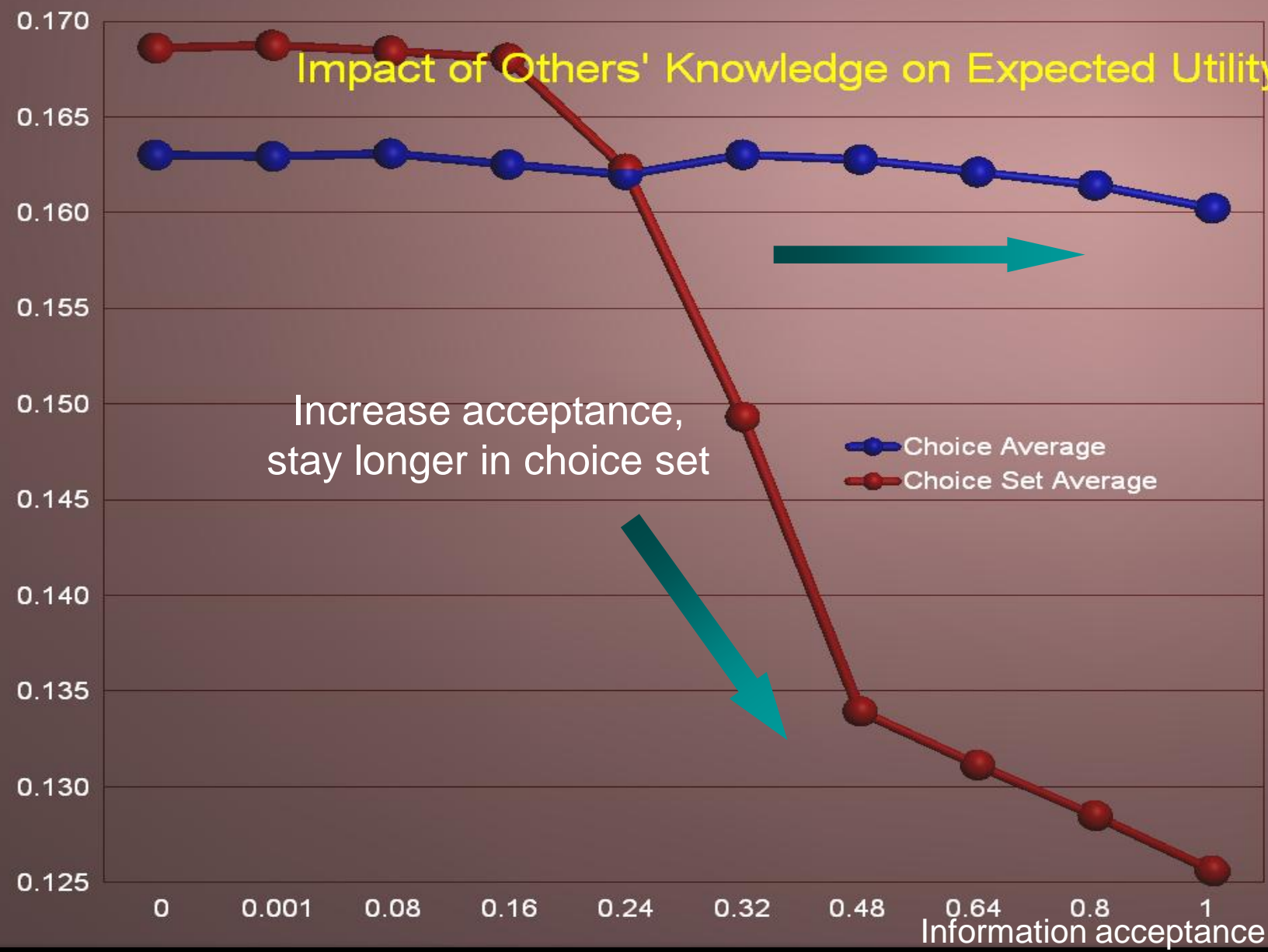
Increase acceptance,  
more alternatives

Size  
Renewal Rate

Information acceptance

Expected utility

### Impact of Others' Knowledge on Expected Utility

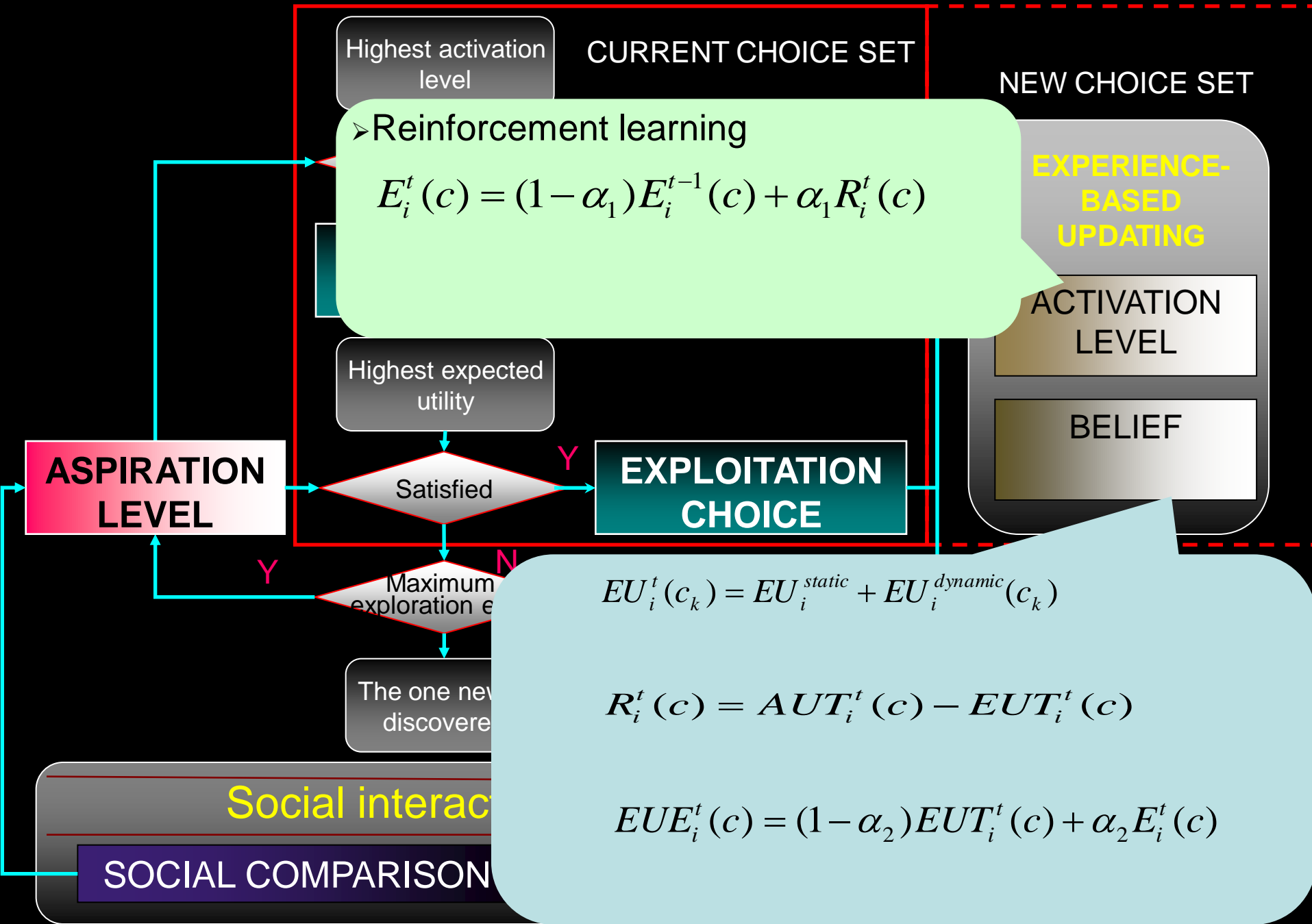


Increase acceptance,  
stay longer in choice set

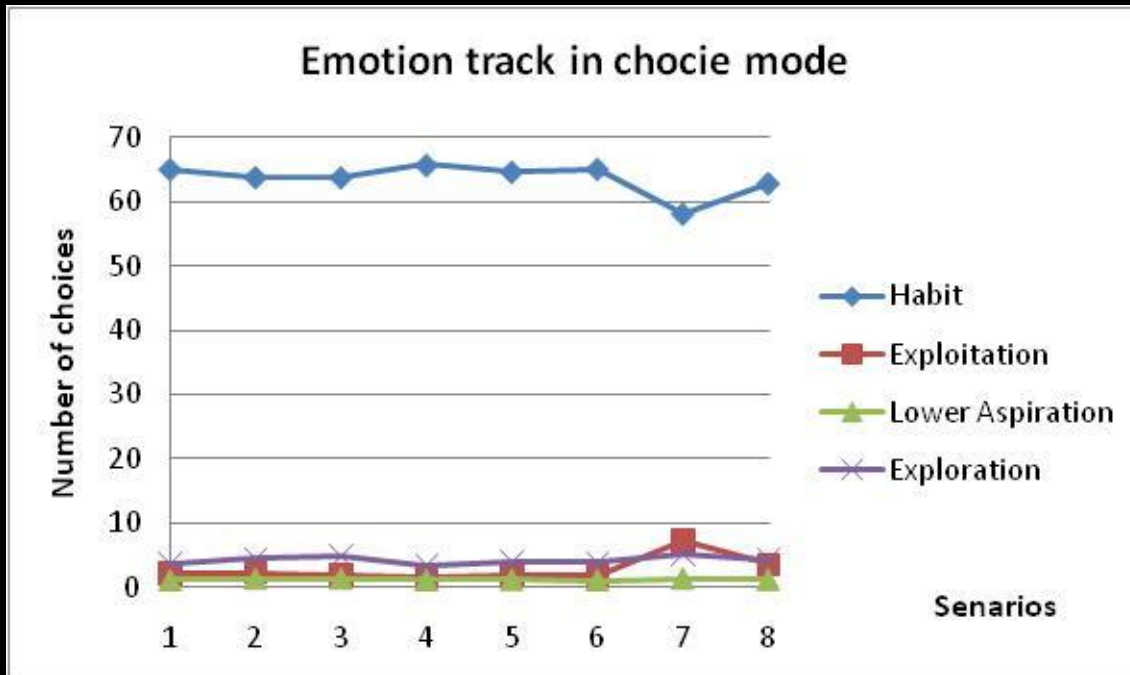
Choice Average  
Choice Set Average

Information acceptance

# Process Model Affective Responses



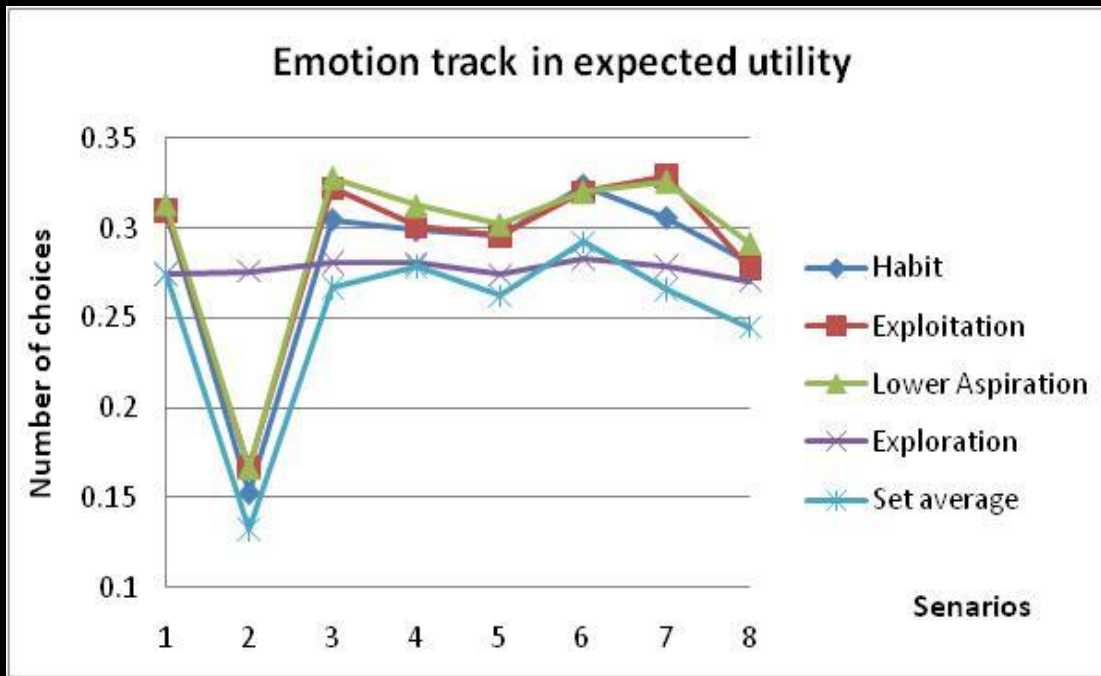
# The impact of affective responses 1



## Scenarios:

1. Baseline case
2. Emotional decision
3. Recent emotions
4. Short memory
5. Negative surprises
6. Positive surprises
7. Higher fluctuate surprises
8. Negative mean surprises

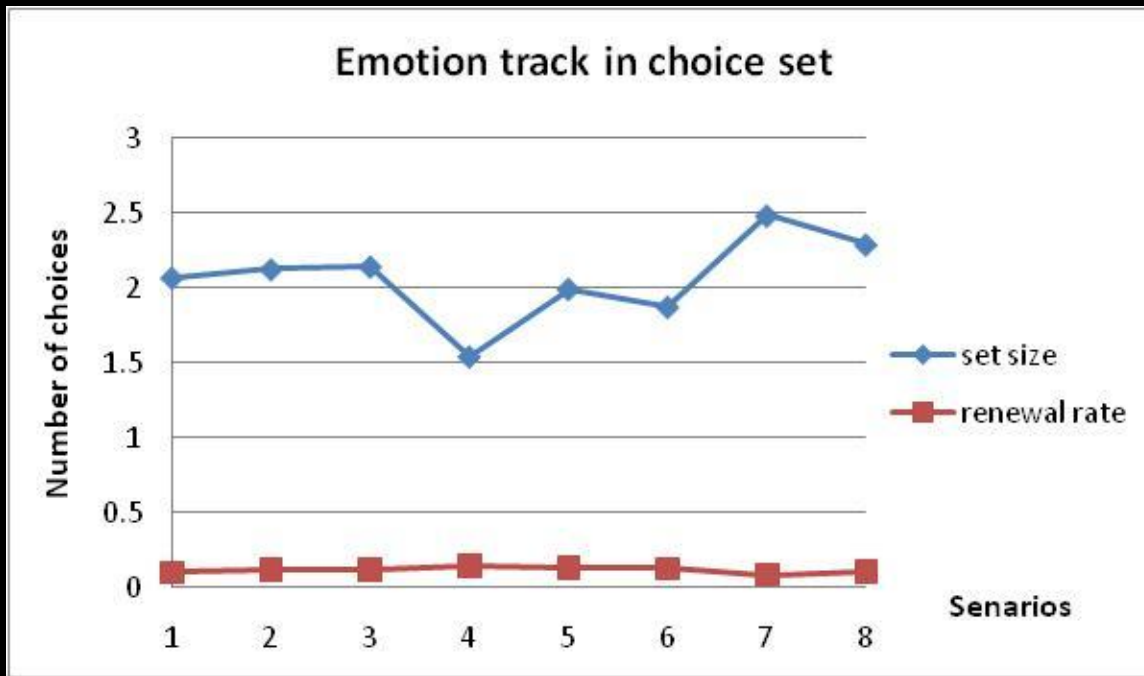
# The impact of affective responses 2



## Scenarios:

1. Baseline case
2. Emotional decision
3. Recent emotions
4. Short memory
5. Negative surprises
6. Positive surprises
7. Higher fluctuate surprises
8. Negative mean surprises

# The impact of affective responses 1

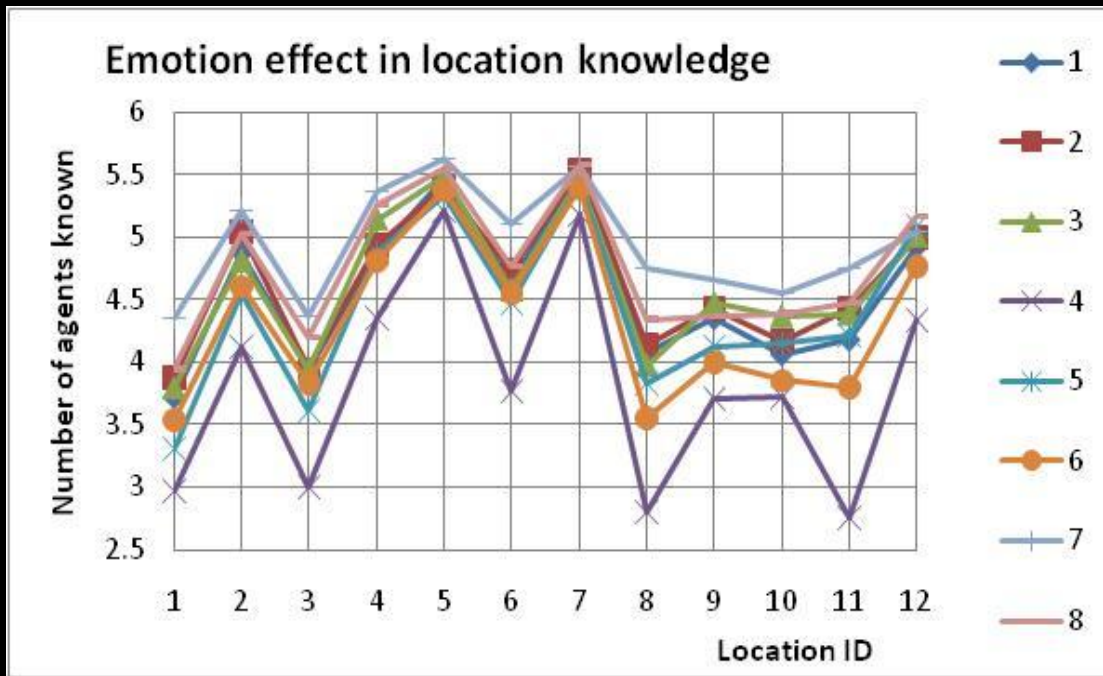


## Scenarios:

1. Baseline case
2. Emotional decision
3. Recent emotions
4. Short memory
5. Negative surprises
6. Positive surprises
7. Higher fluctuate surprises
8. Negative mean surprises



# The impact of affective responses 1



## Scenarios:

1. Baseline case
2. Emotional decision
3. Recent emotions
4. Short memory
5. Negative surprises
6. Positive surprises
7. Higher fluctuate surprises
8. Negative mean surprises

# Conclusion and discussion

- System indicators respond in unique ways to proposed parameters
- Capable of distinguishing habitual, exploitation and exploration choices
- Competent in simulating habit formation and adaptation under uncertain environment (cognitive and affective response)





Thank you